# Robust fault detection and clustering in semiconductor manufacturing processes

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# Introduction

Semiconductor Manufacturing Processes

- Semiconductor manufacturing consists of many processes; each process is also composed of many sequential steps
- Some manufacturing steps are performed continuously without any intermission (e.g., etching and lithography)
- A sequence of continuous steps is called a *run*, and is performed in a series of black box-like equipment





#### □ Fault Detection and Classification (FDC) [7,13]

- Even if a fault has occurred in any run step, it can only be detected when the entire run has been finished
- Various sensors are attached to manufacturing equipment
- Values read periodically from each sensor collectively constitute a (streaming) time-series data
- Multiple time-series data are input to sophisticated algorithms based on statistics, expert systems, and data mining

#### Contributions of this study

- We propose an algorithm for fault detection in semiconductor manufacturing processes
   A modification of discord detection algorithm called HOT SAX [9]
- We propose an algorithm for clustering runs using the result of our fault detection algorithm

#### Evaluation of our algorithms

- We used the experiment data obtained from real-world semiconductor etching processes
- Our fault detection algorithm accurately distinguishes the normal and the perturbed (faulty) runs

Achieved 100% accuracy without false positive or false negative

 Our clustering algorithm generated good clusters of runs having similar sources of faults

# **Related Work**

#### Representation of time-series

- Compressed representation for efficient storage and computation of time-series
- Discrete Fourier Transform (DFT), Piecewise Aggregate Approximation (PAA), etc.
- Symbolic representation
  - Transforms continuous real values in time-series into a finite number of discrete symbols

#### Symbolic Aggregation approXimation (SAX) [11,12]

- A symbolic representation
- Given two parameters w and a, a time-series X of length n is transformed into a sequence  $\hat{X}$  of length w, where each symbol in  $\hat{X}$  is obtained from a symbol set of size a



#### Applying SAX to time-series data mining

- Discord detection using SAX [9, 17]
- Finding motifs (the patterns appearing very frequently in a time-series) [3, 14]
- Minimizing the number of parameters [10]
- *iSAX*: efficient disk-based indexes for large-scale timeseries databases [16]

# **Fault Detection Algorithm**

#### Stream sequences

- While a run is being performed, the sequence of values from each sensor is assigned to a *variable*
- Example: a run which consists of 11 steps (s<sub>1</sub> ~ s<sub>11</sub>) and collects stream sequences for 55 variables (v<sub>5</sub> ~ v<sub>59</sub>)



#### Our fault detection algorithm

- Given a set of runs, it finds the runs that produced perturbed wafers
- 2 run groups: model runs and experimental runs
  - All the model runs produced normal wafers, while a few of experimental runs produced perturbed ones
- We employ the idea and terms introduced by the discord detection algorithm called HOT SAX [9]

#### Decision of fault

For every combination (variable v, step s), our algorithm checks:

 $\square \min\{D(S'_{\nu,s}, M_i)\} > \max\{D(M_i, M_j)\}$ 

• Discord ratio 
$$R_D = \frac{D_{exp}}{D_{mod}} = \frac{\min\{D(S'_{v,s},M_i)\}}{\max\{D(M_i,M_j)\}}$$

■ *M<sub>i</sub>* is a stream subsequence for (*v*, *s*) from a model run *R<sub>i</sub>* 

**\Box**  $S'_{v,s}$  is a stream subsequence from an experimental run to test

- If R<sub>D</sub> > 1.0, our algorithm takes it as an evidence of fault occurred in the corresponding step s.
- If any combination in a certain experimental run reports a fault, the whole run is regarded as perturbed.



#### Adopting SAX transformation

**D** Actually, we use an estimate  $\hat{R}_D$  ( $\geq$  o) instead of  $R_D$ 

# Adopting SAX transformation cont'd R̂<sub>D</sub> > 1.0 does not necessarily imply R<sub>D</sub> > 1.0 We define fault probability function F(R̂<sub>D</sub>)

$$\square F(\hat{R}_D) = \begin{cases} 0 & \text{if } \hat{R}_D \le 1\\ 1 - \exp\left\{-\frac{(\hat{R}_D - 1)^2}{2\sigma^2}\right\} & \text{otherwise} \end{cases}$$

□ If  $F(\hat{R}_D)$  is close to 1.0, it is regarded that a fault has occurred in the corresponding step

### ■ Adopting SAX transformation *cont'd* ■ $F(\hat{R}_D)$ graphs for a few $\sigma$ values



#### Differences of our algorithm from HOT SAX

- While HOT SAX requires the length *l* of discord subsequence as an input, our algorithm derives the length from a run step
- Our algorithm checks whether a stream subsequence S'<sub>v,s</sub> is the discord subsequence or not, while HOT SAX finds a discord subsequence that may be located at any position

#### Rationale of adopting SAX transformation

- SAX reduces the size of stream data dramatically
  - Given a parameter w, the SAX-transformed sequence has w/(n\*8) (<< 1.0) times the size of original data, where n is the length of original data

SAX helps improve the performance of our algorithm

For computing MINDIST() between two SAX-transformed sequences of length w, we need only w (< n) arithmetic operations</p>

# **Variable Selection Method**

#### Variable selection

- Selecting the minimal number of variables that assure accurate results of our fault detection algorithm
- By using smaller number of variables, we can achieve higher performance of our algorithm
- Our variable selection method is based on *Dempster-ShaferTheory (DST*), which is a mathematical theory of probability
- DST has been used for various applications of real-time malfunction diagnosis

#### DST compared with traditional probability theory

- DST calculates probabilities based on 'evidences'
  - E.g., when a coin is tossed, the probability (support) of having a head up is o, if there is no evidence
- The probability of a proposition A in DST is represented with two measures support s(A) and plausibility pl(A)
  0.0 ≤ s(A) ≤ pl(A) ≤ 1.0

 $\square pl(A) = 1 - s(A')$ 

- DST provides a *rule of combination* for combining probability measures (evidences) from multiple 'independent' sources
  - E.g., a semiconductor manufacturing process where two sensors generate fault alert independently with their own probabilities

#### Outline of our variable selection method

- Computes a goodness measure for each variable in an experimental run
  - Probability (support) that the variable correctly contributes for detecting faults in a certain experimental run
  - Calculated for each of experimental runs independently
- Joint goodness measure for each variable is calculated using DST's rule of combination
- Variables with the highest joint goodness measures are selected for our fault detection algorithm

#### Goodness measure $g(v_i)$ for a variable $v_i$

 $g(v_i) = \begin{cases} 1 - \max\{F(\hat{R}_D)\} & \text{if } R \text{ is a normal run} \\ \max\{F(\hat{R}_D)\} & \text{if } R \text{ is a perturbed run} \end{cases} \\ \max\{F(\hat{R}_D)\} & \text{is the maximum } F(\hat{R}_D) \text{ across all the steps} \end{cases} \\ \end{tabular}$ 

$$\square s\langle v_1, \dots, v_N, \theta \rangle = \left\langle \frac{1}{N} g(v_1), \dots, \frac{1}{N} g(v_N), 1 - \frac{1}{N} \sum g(v_i) \right\rangle$$

*N* is the number of variables, *θ* indicates `any' variable
 Calculated for each of experimental runs

# Combination of support values Using DST's rule of combination

$$s_{joint}(v_i) = \frac{1}{k} \sum_{v_A \cap v_B = v_i} s_1(v_A) s_2(v_B)$$
$$k = \sum_{v_A \cap v_B = \emptyset} s_1(v_A) s_2(v_B)$$

- s<sub>1</sub> and s<sub>2</sub> are support values calculated in any two different experimental runs
- DST's rule of combination is commutative and associative; hence the joint goodness value can be calculated in any order of runs

# **Clustering Algorithm**

#### Our clustering algorithm

- It forms clusters of experimental runs using the result of our fault detection algorithm
  - It uses the fault steps of experimental runs, i.e., the experimental runs with the same fault steps are gathered
- Even in case we do not know the source of faults in a certain experimental run, we can estimate it by investigating the experimental runs in the same cluster

#### Representation of runs

- A bitmap  $B = b_1 b_2 \dots b_S$  is used to represent the fault steps for each experimental run (S = the number of steps)
- A bit b<sub>i</sub> is set to 1, if a fault has occurred in the corresponding step; the bit is reset to 0, otherwise.

#### Clustering procedure

- Initially, for each experimental run R<sub>i</sub>, a cluster C<sub>i</sub> containing the R<sub>i</sub> only is created
- Our algorithm merges the clusters containing the two experimental runs R<sub>i</sub> and R<sub>j</sub> (i ≠ j), if it holds:
  Onebit(B<sub>i</sub>⊕B<sub>i</sub>) ≤ ε
- Onebit() function returns the number of 1 bits in a bitmap, the sign ⊕ represents XOR operator, and ɛ is a prespecified parameter

# **Evaluation – settings**

#### Experiment data

- Real-world semiconductor etching process data
- 2 run groups
  - model run group: 10 normal runs
  - experimental run group: 3 normal and 7 perturbed runs
- Each run consists of 11 steps, and real-time stream data of 55 variables were collected at 10Hz

#### Experiment data cont'd

Baseline runs	Experiment runs					
Run#	Run#	Description				
FDA_12	FDA_14	Unperturbed control run				
FDA_16	FDA_15	–o.5mT change to base pressure				
FDA_19	FDA_17	+0.5mT change to base pressure				
FDA_21	FDA_20	–1% MFC conversion shift				
FDA_24	FDA_23	+1% MFC conversion shift				
FDA_28	FDA_25	Source RF cable: loss simulation				
FDA_32	FDA_31	Unperturbed control run				
FDA_37	FDA_34	Bias RF cable: power delivered				
FDA_39	FDA_38	Unperturbed control run				
FDA_44	FDA_43	Added chamber leak rate by 1.3mT/min				

# **Evaluation – result**

#### First experiment

- We used the 11 variables selected by principal component analysis (PCA) in [7]
- Our algorithm caused false positive on FDA\_20 and FDA\_23 and false negative on FDA\_31

Table 5 max{r (ND)} values obtained in the first experiment.												
	1	2	3	4	5	6	7	8	9	10	11	Decision
FDA_14	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000	normal
FDA_15	0.000	<u>1.000</u>	1.000	0.927	0.000	0.000	0.000	0.000	0.000	0.000	0.000	perturbed
FDA_17	0.000	<u>1.000</u>	<u>1.000</u>	0.000	0.000	0.000	<u>0.986</u>	0.000	0.147	0.000	0.000	perturbed
FDA_20	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000	normal (f.p)
FDA_23	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000	normal (f.p)
FDA_25	0.000	0.000	<u>0.694</u>	<u>0.537</u>	<u>1.000</u>	1.000	<u>0.832</u>	<u>0.832</u>	1.000	1.000	0.000	perturbed
FDA_31	0.000	0.336	0.000	1.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000	perturbed (f.n)
FDA_34	0.000	0.006	<u>0.990</u>	<u>0.992</u>	0.827	1.000	1.000	1.000	0.169	1.000	0.000	perturbed
FDA_38	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000	normal
FDA_43	0.000	0.000	0.000	0.000	0.077	0.000	0.249	0.000	1.000	0.000	0.000	perturbed

**Table 3** max{ $F(\hat{R}_D)$ } values obtained in the first experiment.

#### Second experiment

- We perform K-fold cross validation (K = 10), and experimental runs are also used to select variables
- For each experimental run R ( $R \in \mathcal{E} = \{FDA_{14}, FDA_{15}, ..., FDA_{43}\}$ ), variables are selected from the model runs and the remaining experimental runs  $\mathcal{E} \{R\}$

<b>Table 4</b> $\max\{F(\hat{R}_D)\}$ values obtained in the second experiment.												
	1	2	3	4	5	6	7	8	9	10	11	Decision
FDA_14	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000	normal
FDA_15	0.000	<u>1.000</u>	<u>1.000</u>	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000	perturbed
FDA_17	0.000	1.000	1.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000	perturbed
FDA_20	0.000	0.855	0.913	<u>0.992</u>	0.998	<u>0.991</u>	0.000	0.905	0.978	0.992	0.000	perturbed
FDA_23	0.000	<u>0.759</u>	<u>0.571</u>	<u>0.957</u>	0.983	0.956	0.000	0.559	0.870	0.981	0.000	perturbed
FDA_25	0.000	0.000	<u>0.997</u>	<u>0.904</u>	<u>0.815</u>	1.000	<u>0.997</u>	<u>0.997</u>	0.985	1.000	0.000	perturbed
FDA_31	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.105	0.000	0.000	0.000	normal
FDA 34	0.000	0.125	1.000	1.000	0 504	1.000	1.000	1.000	0.855	1.000	0.000	perturbed
We achieved 100% accuracy without any false positive or false negative!												
FDA_43	0.000	0.000	0.000	0.000	0.000	0.009	0.213	0.213	<u>0.995</u>	0.024	0.000	perturbed

#### Third experiment

- We perform our clustering algorithm with  $\varepsilon = o$  (toughest)
- Experimental runs in the same cluster have similar sources of faults
- Our algorithm can be used in investigating the source of any anomaly in semiconductor manufacturing processes

Clusters	Experimental runs	Fault Classification
Cluster 1	FDA_14&31&38	Normal runs
Cluster 2	FDA_15&17	Pressure control system
Cluster 3	FDA_20&23	Gas delivery system
Cluster 4	FDA_25&34	RF power system
Cluster 5	FDA_43	Process chamber leak

# Conclusions

#### Proposed algorithms

- Fault detection algorithm, which is a modification of the discord detection algorithm called HOT SAX [9]
- A method to select minimal number of variables assuring accurate results of our fault detection algorithm based on DST
- An algorithm for clustering experimental runs using the result of our fault detection algorithm

#### Evaluation of our algorithms

- Our fault detection algorithm accurately distinguished the normal and the perturbed runs incurring no false positive or false negative
- Our clustering algorithm generated good clusters of experimental runs having similar sources of faults



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