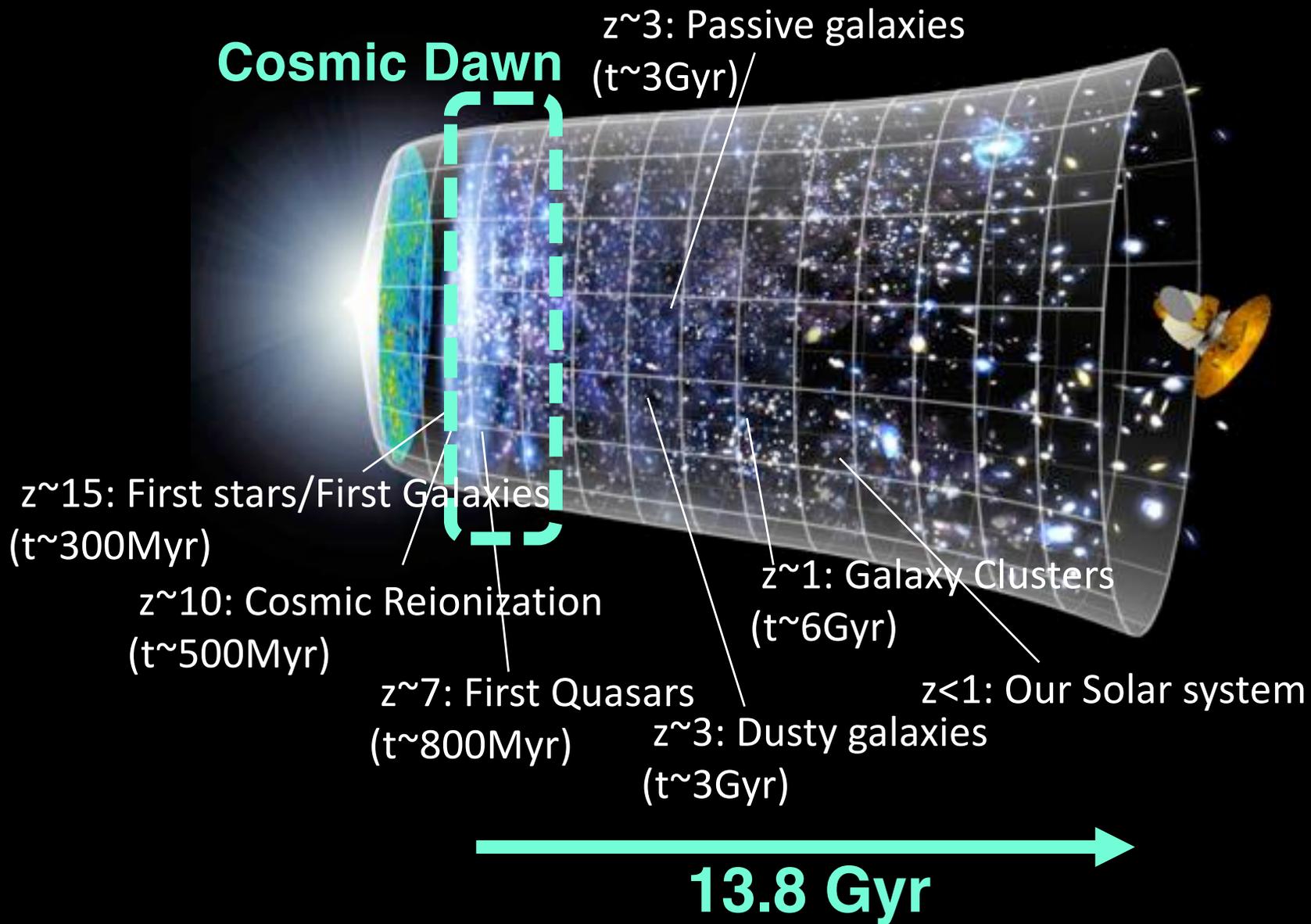


Simulations of galaxy formation with radiative transfer and its application for near-infrared bio-imaging

Hidenobu Yajima
(CCS, University of Tsukuba)

History of our Universe



NASA/WMAP team

Theoretical astrophysics group

Large-scale structure



Inter-galactic medium



7 faculty
8 pos-docs
23 students

Galaxy



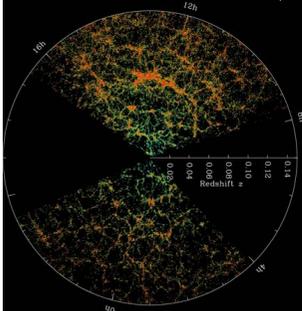
Black hole



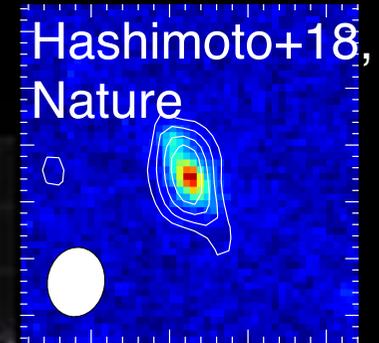
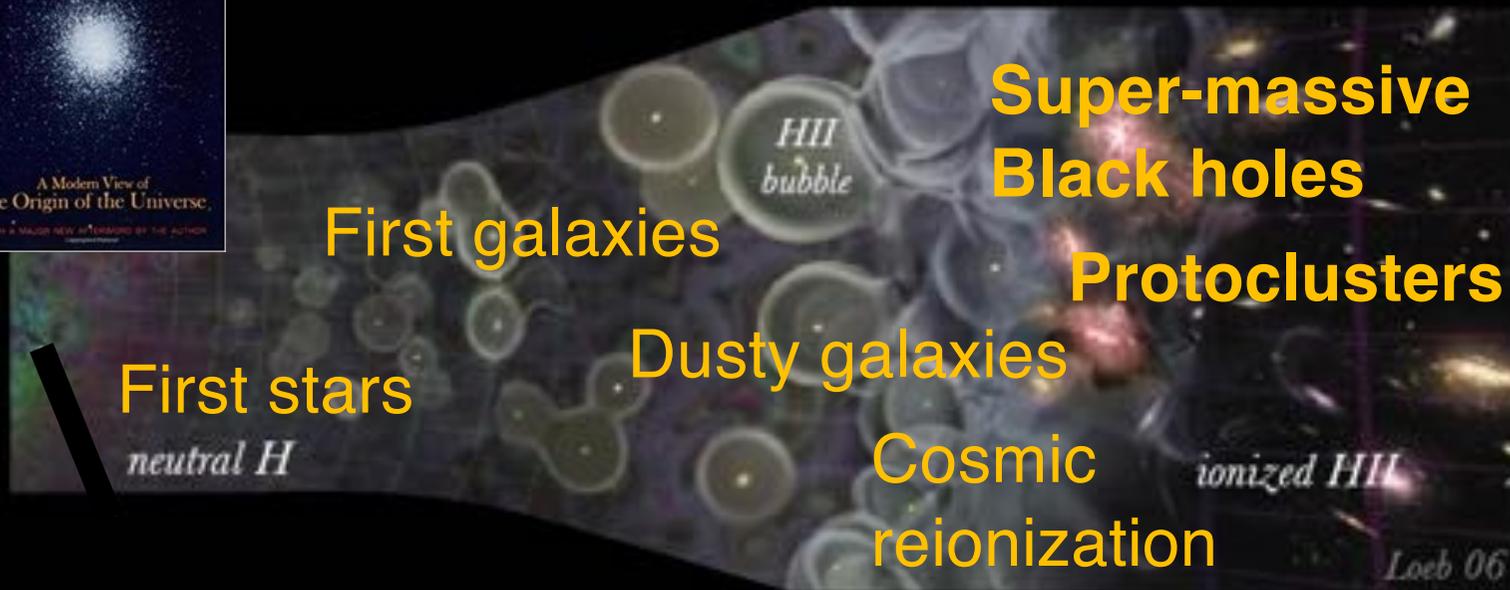
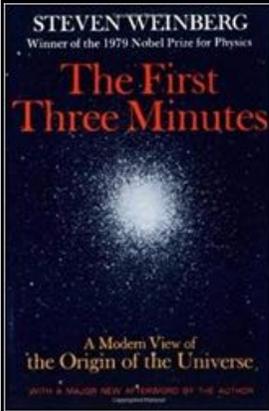
Planet/Dust

Large scale
~10²⁰ km

Small scale
~0.1 μm



First billion years

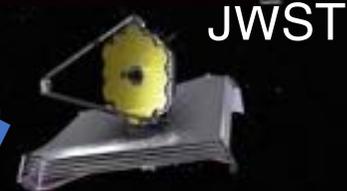
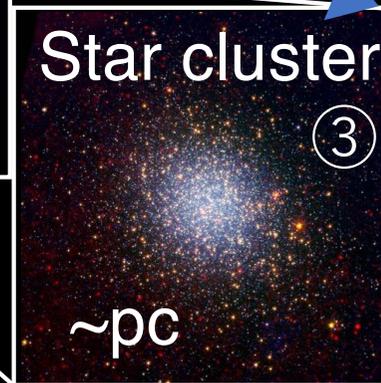
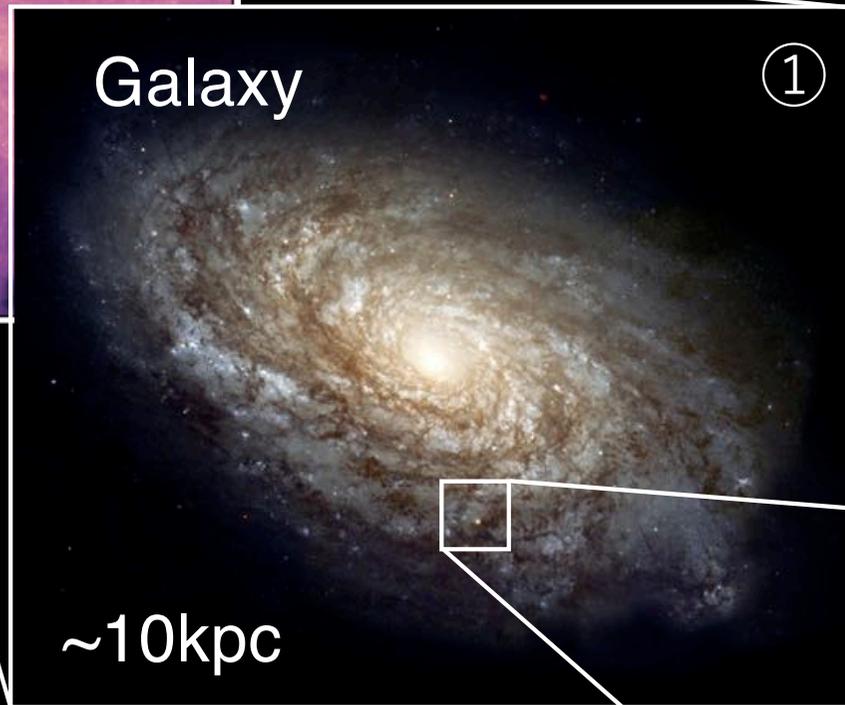
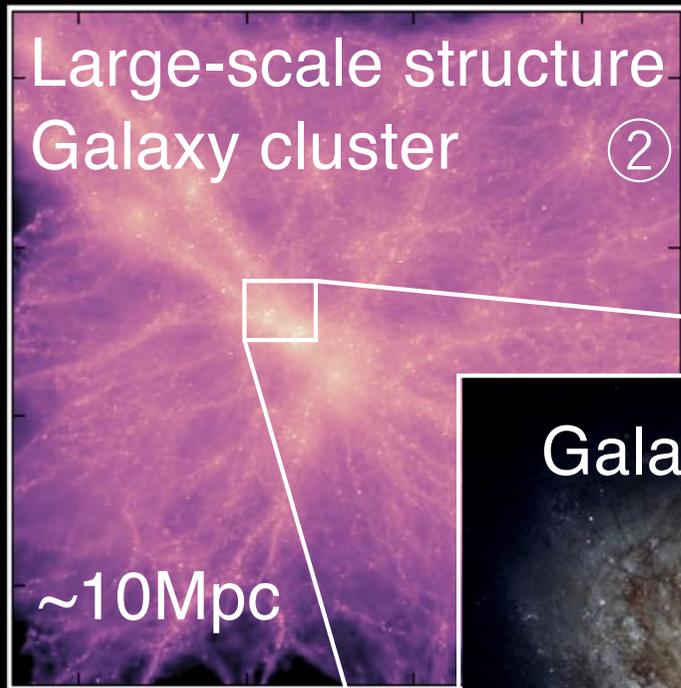


- How first galaxies form and evolve?
- What star formation history?
- How radiation properties change with the galaxy evolution?
- How massive BHs form?
- How reionization proceeds?



← ~2020s-2030s

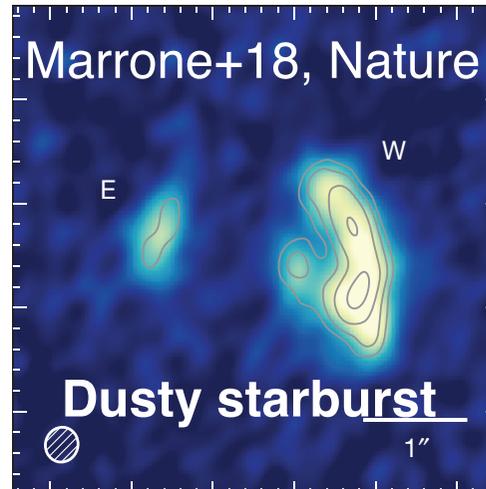
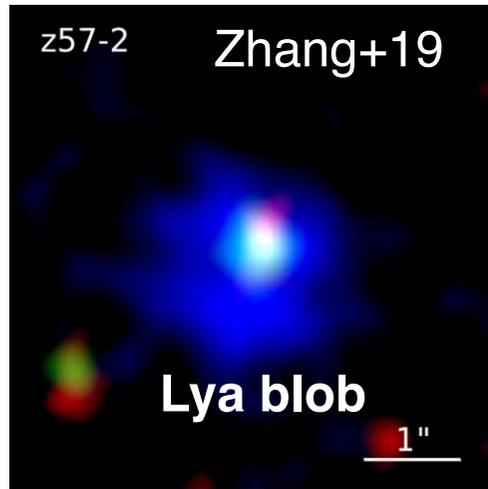
Hierarchical structure



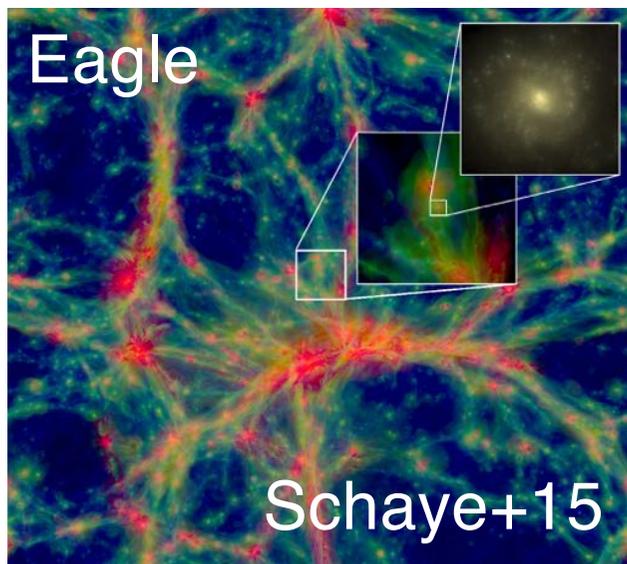
Gas accretion, feedback, merger?

Diversity in observed galaxies

Various radiative properties of high-redshift galaxies



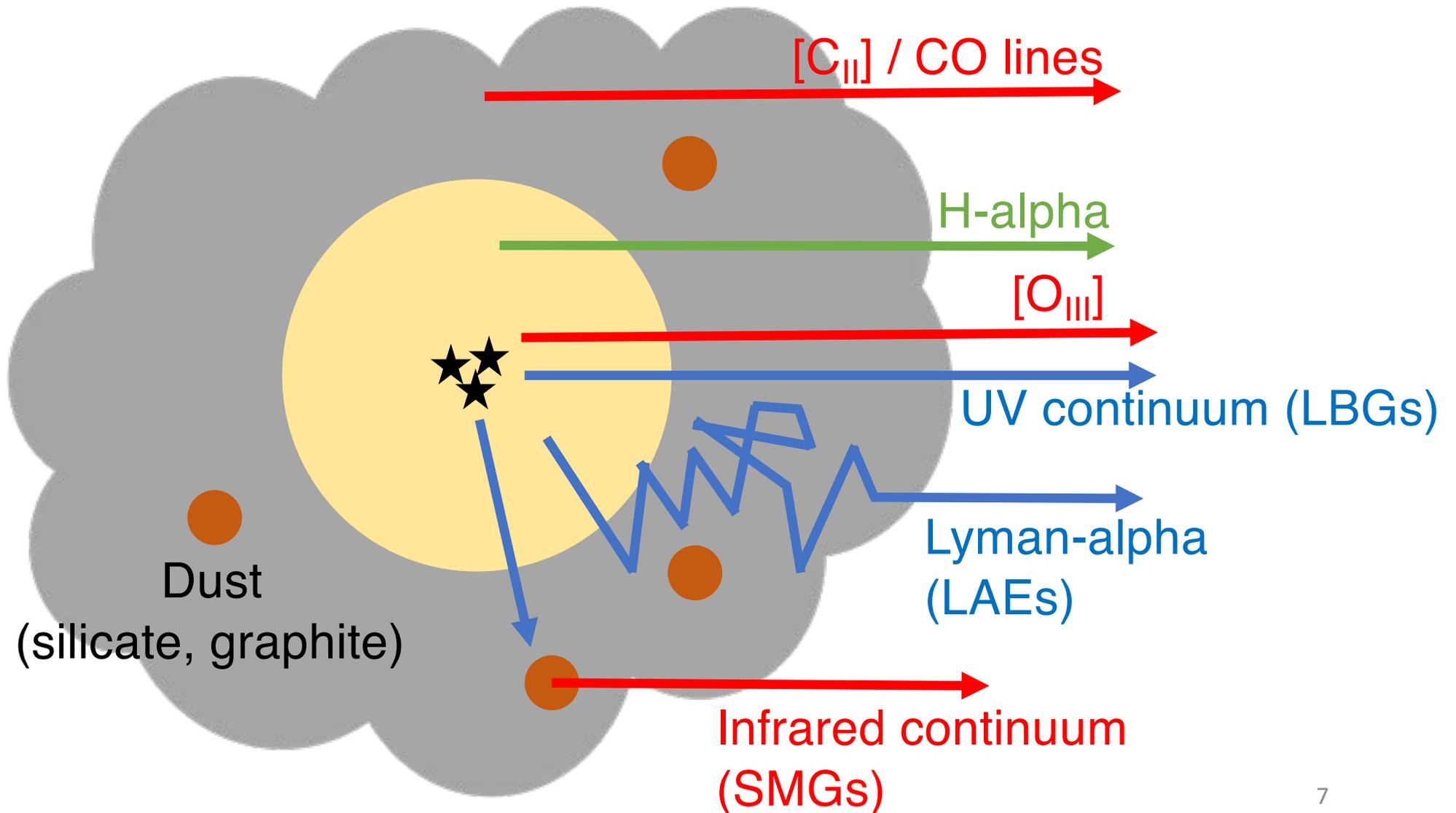
Numerical simulations



- ✓ Sub-grid models
- ✓ Feedback
- ✓ Statistics
- △ High-resolution



Radiative processes



Simulations

Cosmological hydrodynamics simulations

Gadget-3 (Springel+05; Johnson+13)

$$\frac{\partial \rho}{\partial t} + \nabla \cdot (\rho \mathbf{v}) = 0$$

$$\rho \left[\frac{\partial v}{\partial t} + (v \cdot \nabla)v \right] = -\nabla p + F_{\text{rad}} + F_{\text{grav}}$$

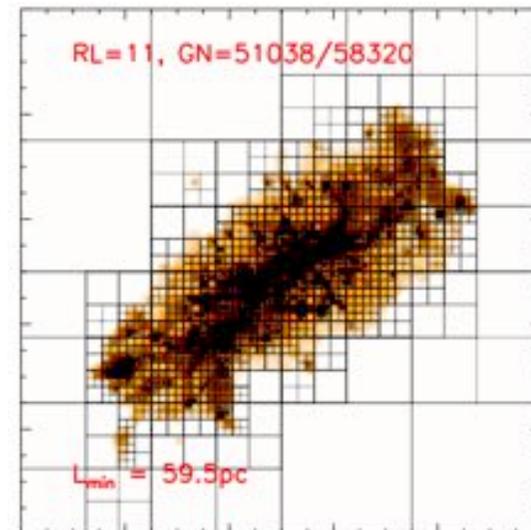
$$\rho \left[\frac{\partial e}{\partial t} + (v \cdot \nabla)e \right] = -p \nabla v + \Gamma - \Lambda$$



Dark matter
Star formation
Feedback
Chemistry

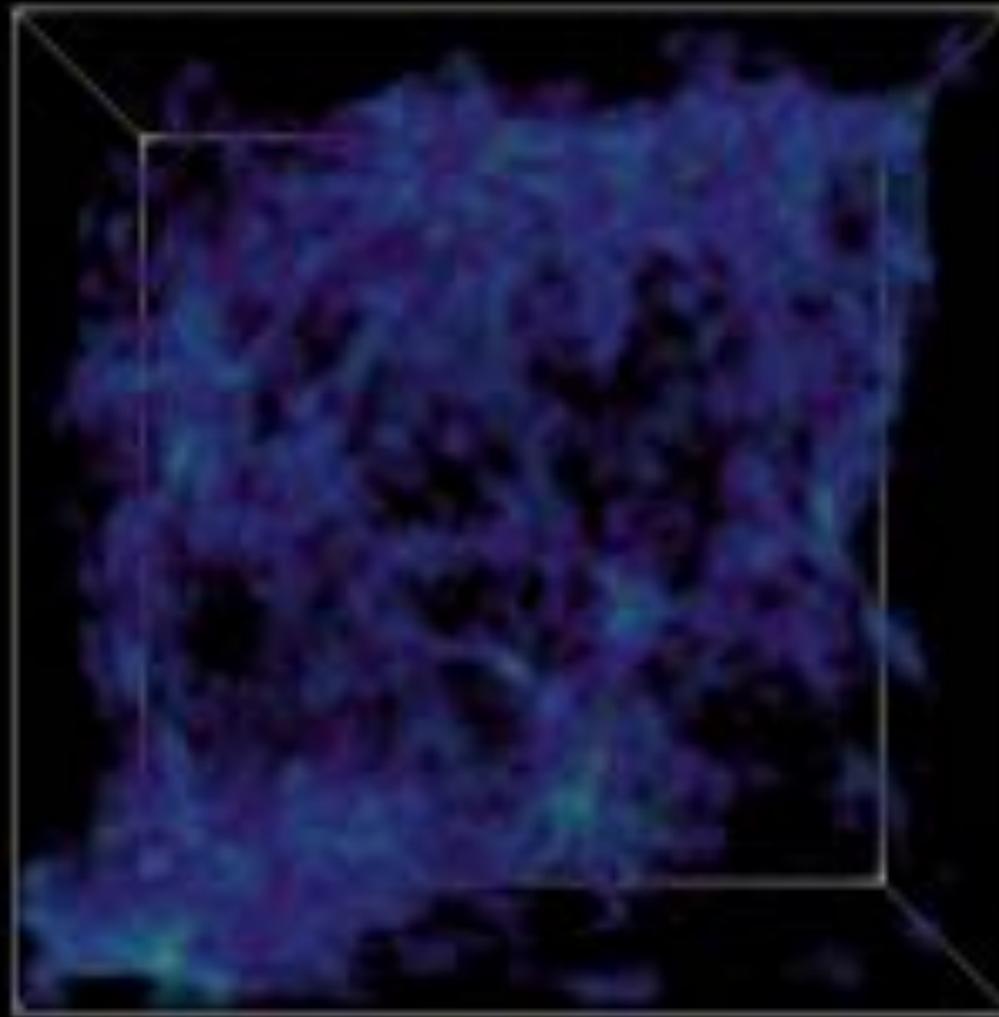
Multi-wavelength radiative transfer
ART² (Li+08; Yajima+12)

$$\frac{\partial I}{c \partial t} + n \cdot \nabla I = -\alpha I + \epsilon + \oint \phi(\Omega', \Omega) I d\Omega'$$



Formation of first galaxy

([Yajima et al. 2017, ApJ, 846, 30](#))



Zoom-in simulation

$L_{\text{box}}=20\text{Mpc}$

$L_{\text{zoom}}\sim 1\text{Mpc}$

$M_{\text{halo}}=10^{11}M_{\text{sun}}$

Blue

(gas density)

Yellow

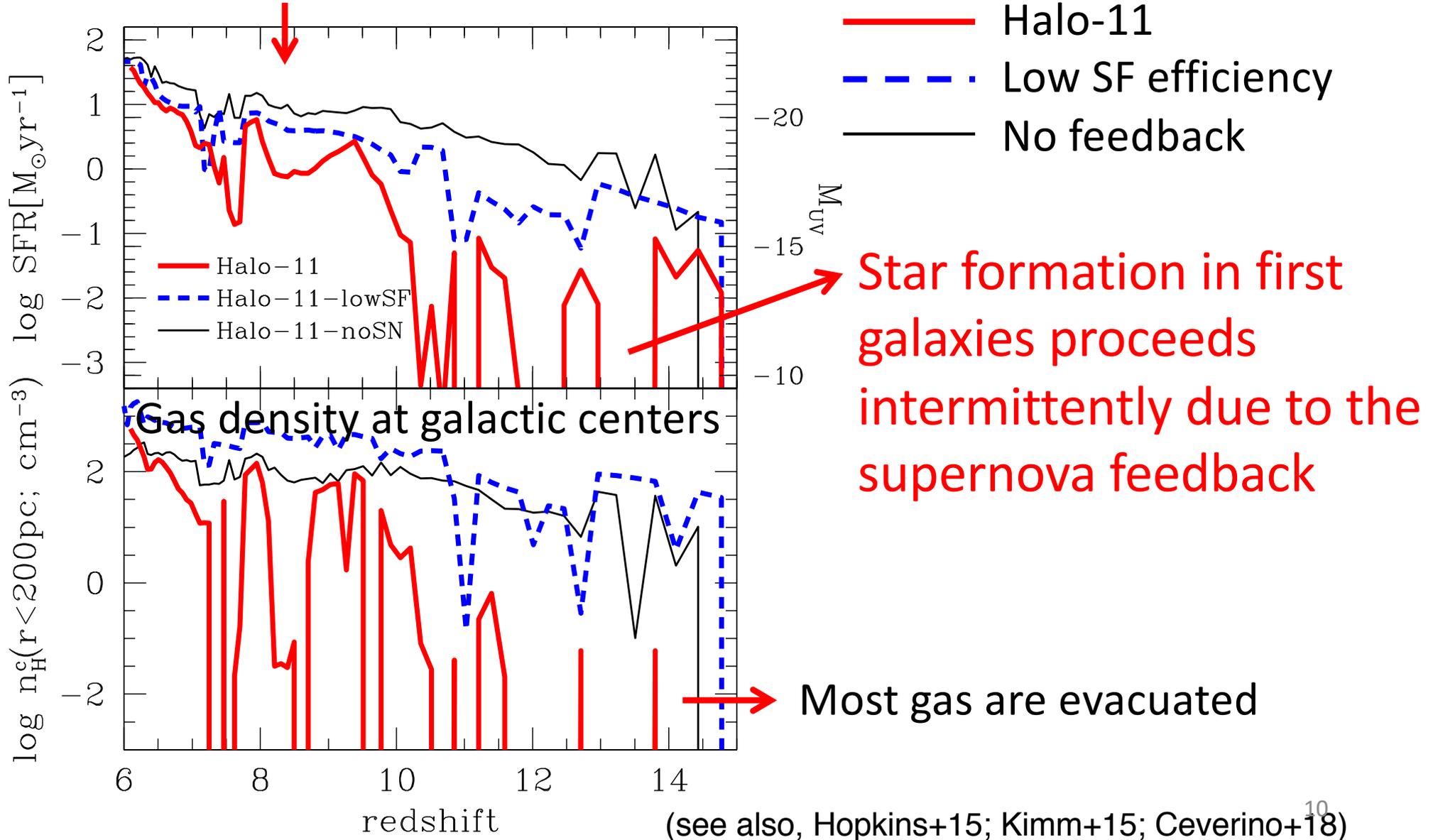
(Metal-enriched
gas)

← 250 kpc/h (comoving) →

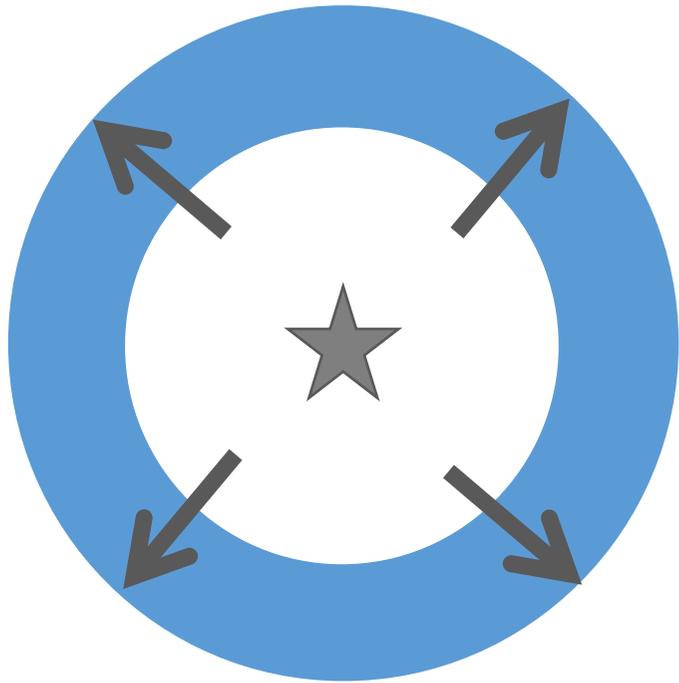
Star formation history

(Yajima et al. 2017, ApJ, 846, 30)

Stable star formation mode



Critical halo mass based on a spherical shell model



$V_{\text{outflow}} > V_{\text{esc}} ?$

$$M_{\text{gas}} V_{\text{outflow}} = \sqrt{2\eta_{\text{SN}}^0 E_{\text{SN}} M_{\text{cool}}}$$

$$\eta_{\text{SN}} = \eta_{\text{SN}}^0 \frac{M_{\text{cool}}}{M_{\text{gas}}}$$

Gas mass in cooling radius

Total gas mass

$$V_{\text{esc}} = \sqrt{\frac{2GM_{\text{h}}}{R_{\text{vir}}}}$$

$$M_{\text{h,crit}} = \underline{0.8 \times 10^{10} M_{\odot}} \left(\frac{\epsilon_{\text{SF}}}{0.1}\right)^{3/2} \left(\frac{\eta_{\text{SN}}}{0.5}\right)^{3/2} \left(\frac{1+z}{7}\right)^{-3/2}$$

Star formation efficiency

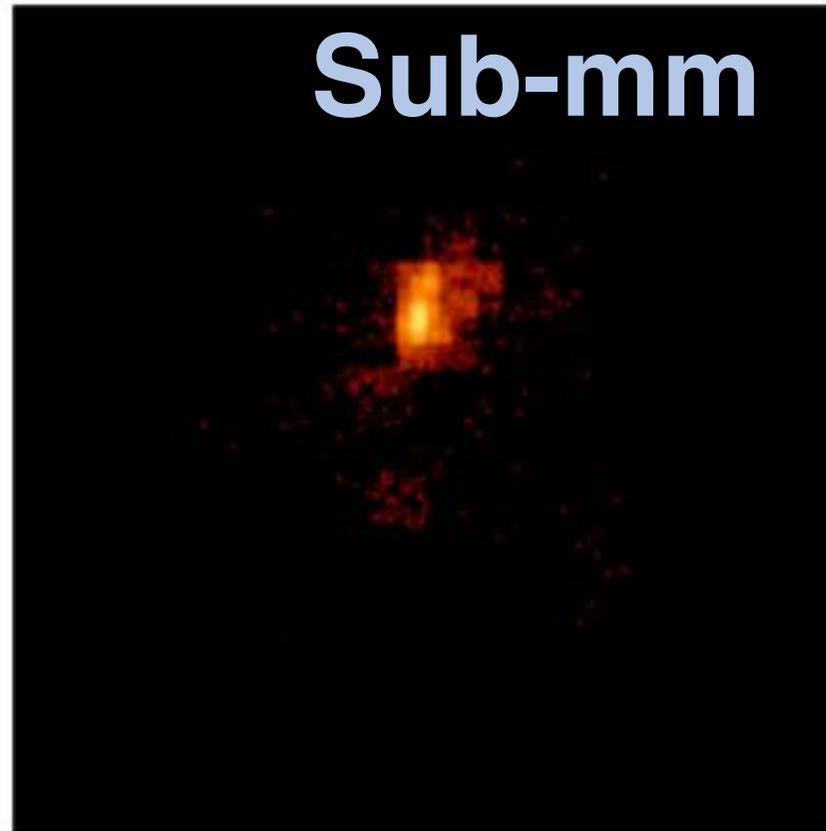
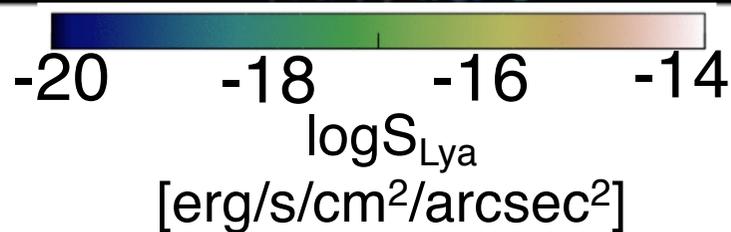
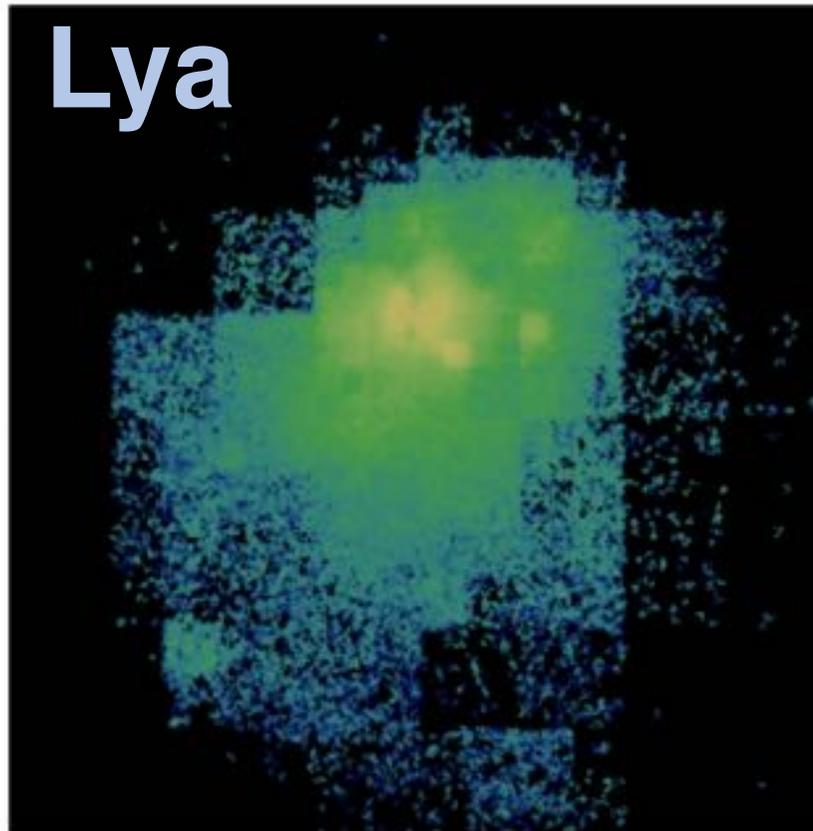
Energy conversion rate

Radiative transfer calculations

Surface brightness ($z=10 \rightarrow 6$)

Halo-11

~10-30kpc(physical)

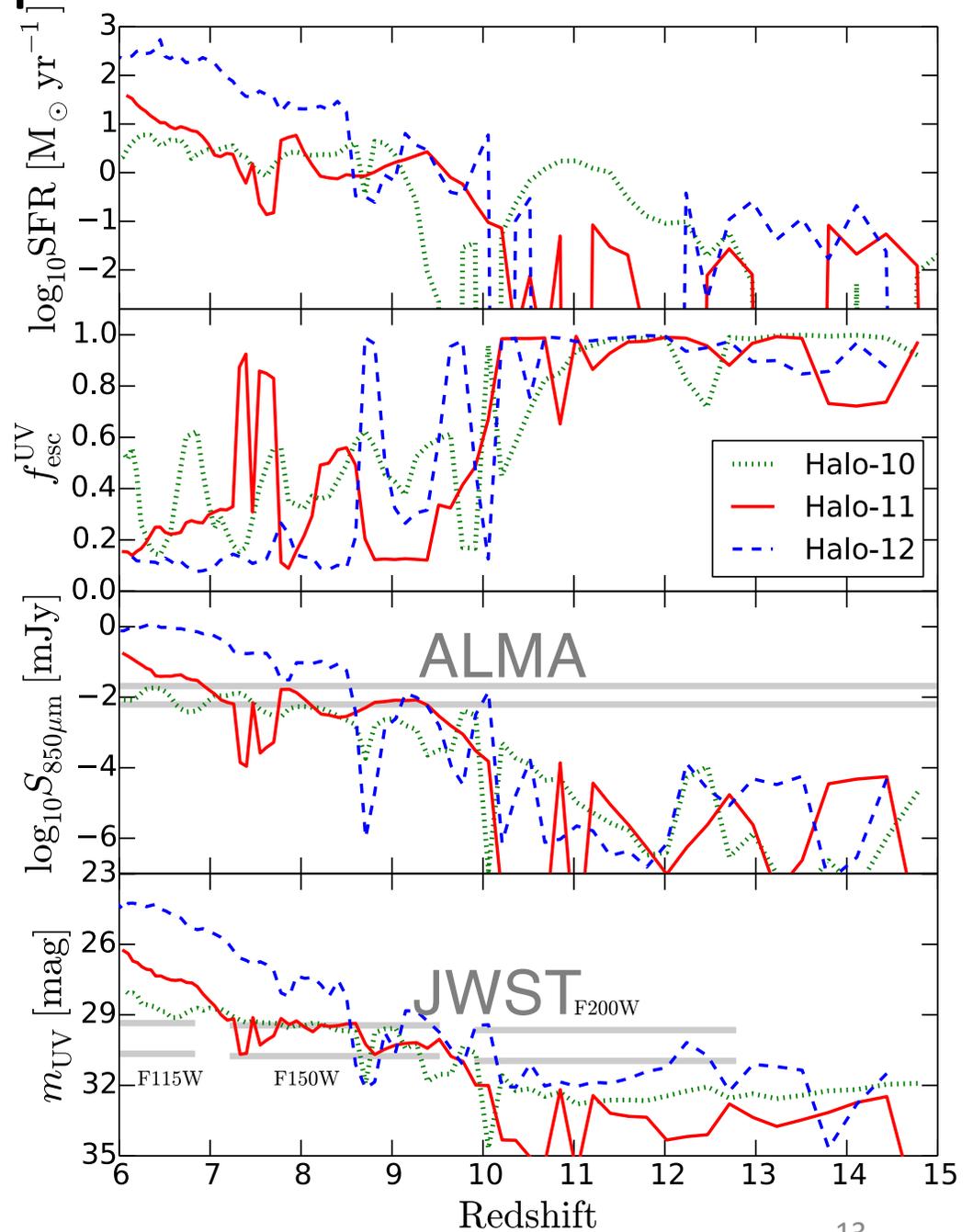


Redshift evolution of flux

Time scale of the fluctuation

$$t \sim \frac{\lambda R_{\text{vir}}}{V_c} \gtrsim 10 \text{ Myr}$$

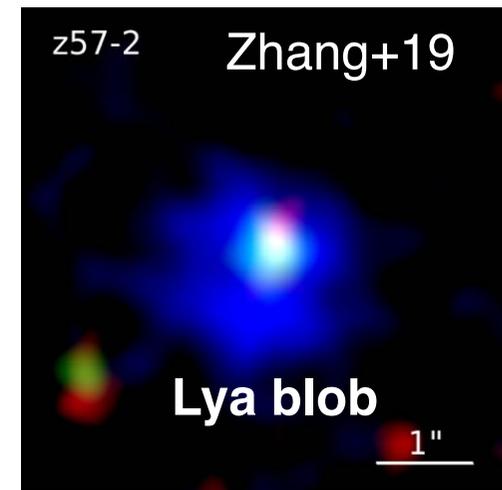
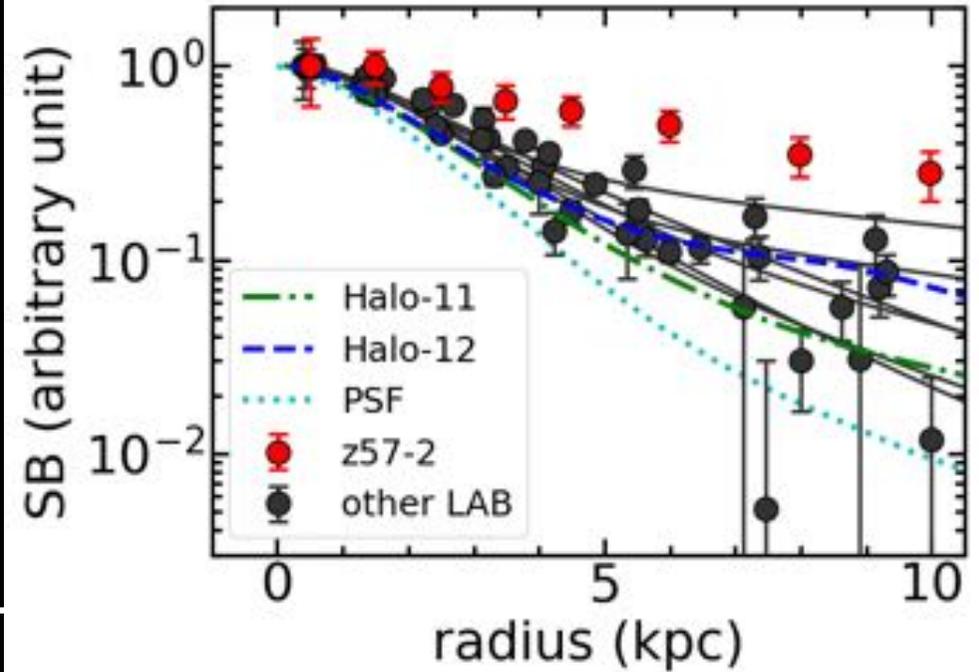
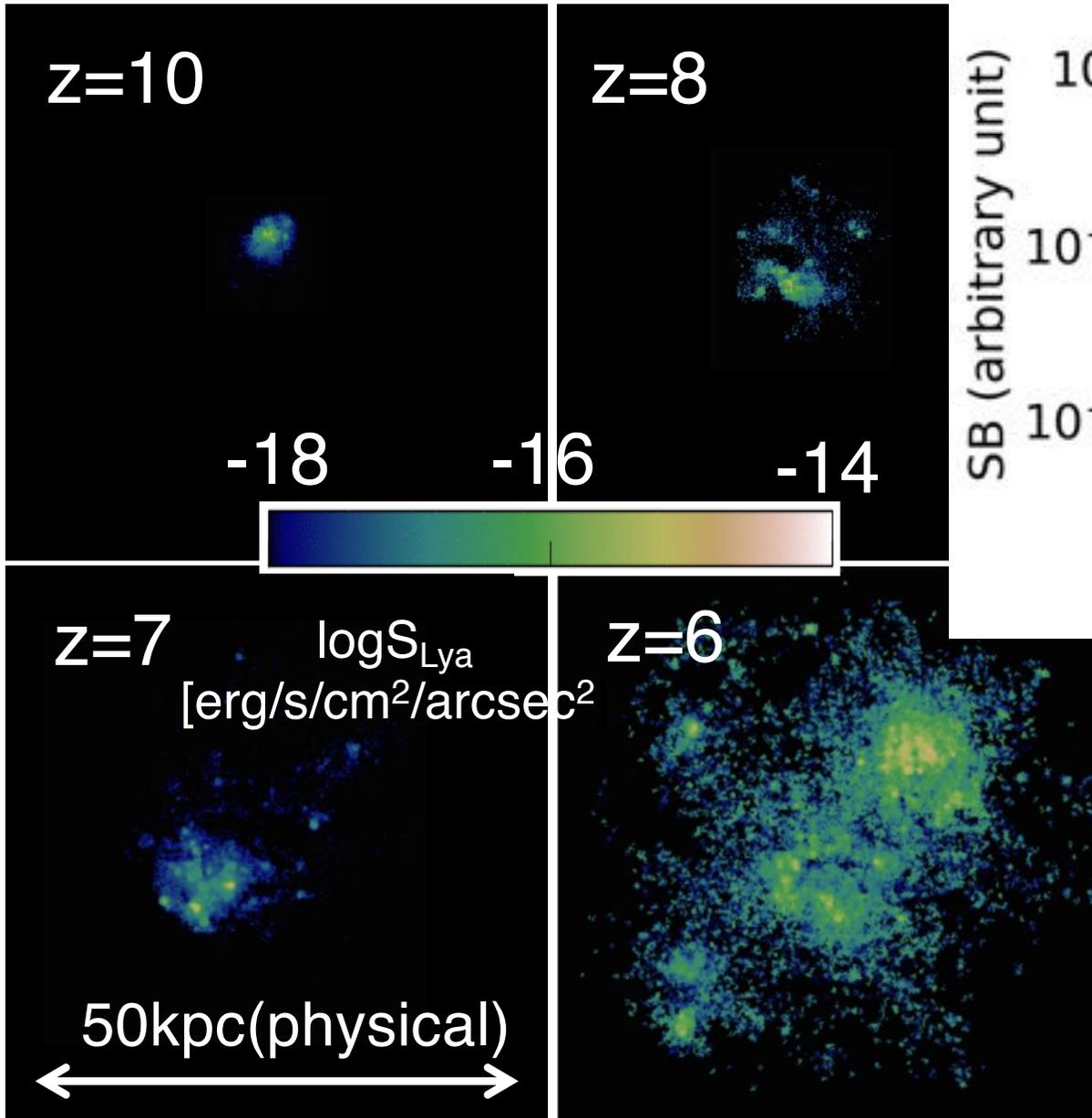
SFR
Escape fraction
Sub-mm
UV cont.



Arata, Yajima, et al. (2019)

Lya surface brightness

Zhang,, Yajima, et al. (2019)



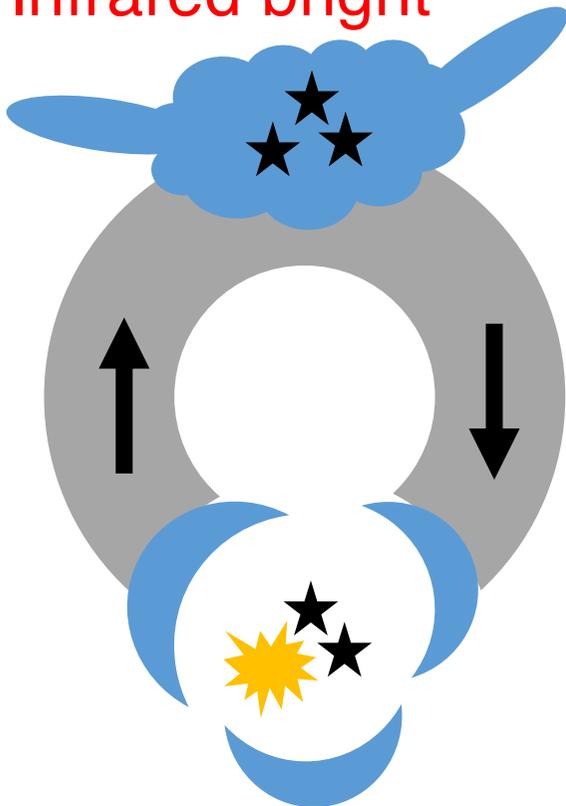
Rapid change of radiative properties

Low-mass galaxies
($M_{\text{halo}} < 10^{11} M_{\text{sun}}$)

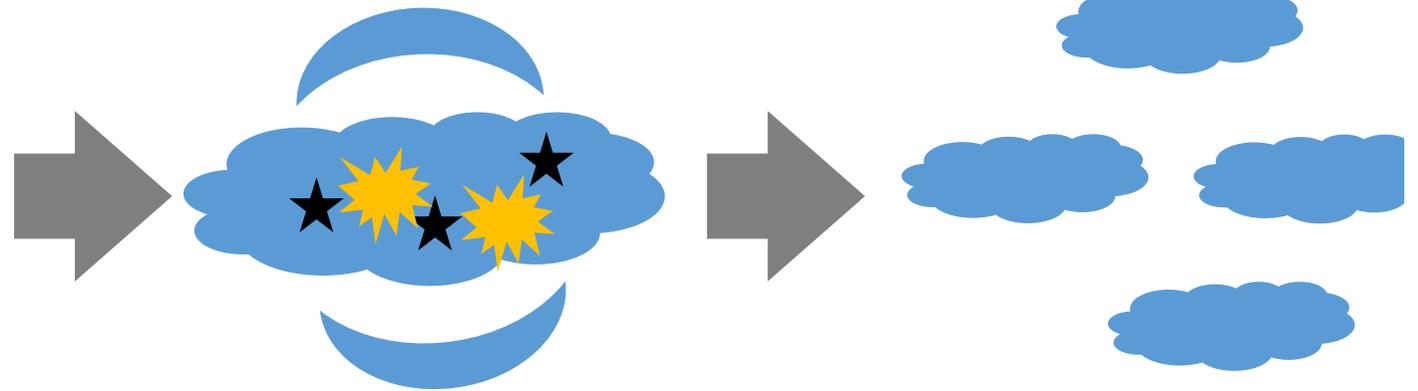
Massive galaxies
($M_{\text{halo}} \sim 10^{11-12} M_{\text{sun}}$)

Clustering
($M_{\text{halo}} \sim 10^{13} M_{\text{sun}}$)

Infrared bright



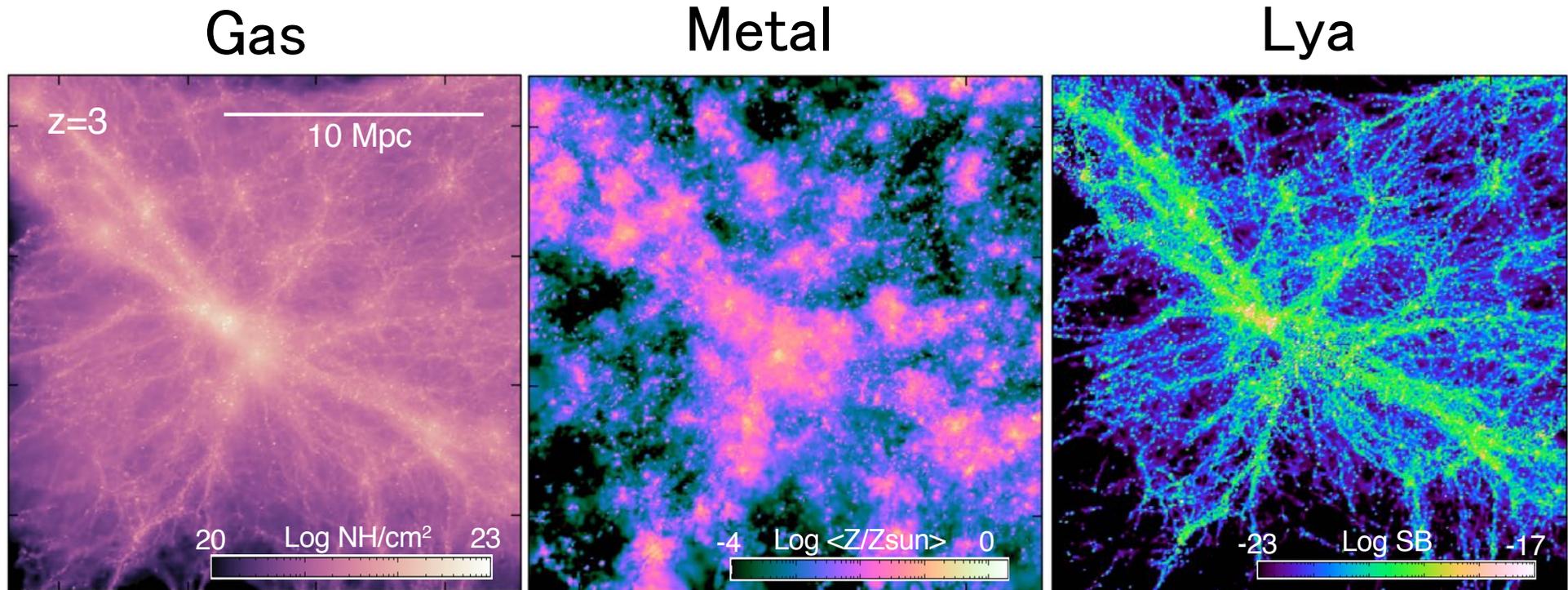
Infrared bright



UV bright

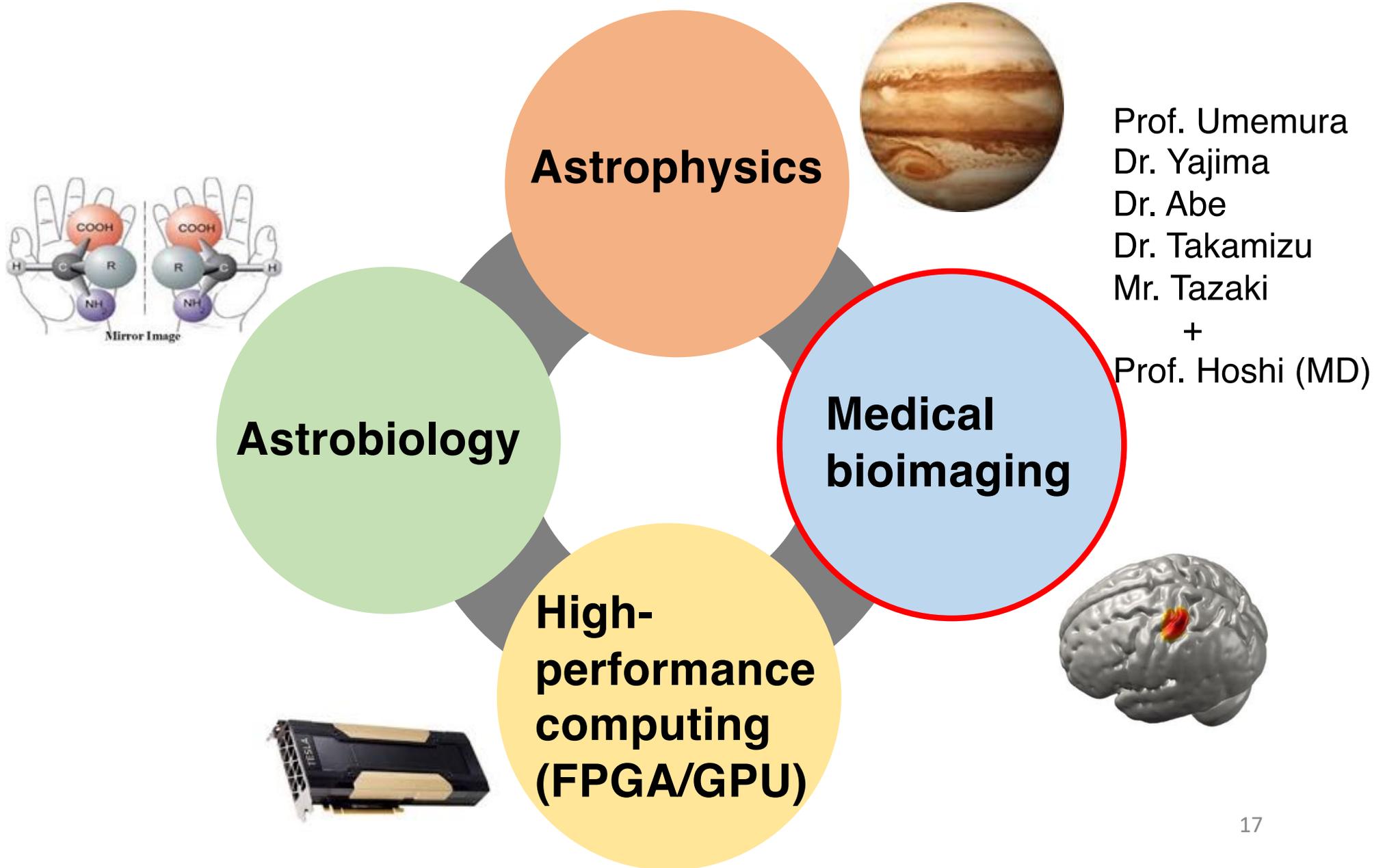
Lya intensity map

We consider Lya cooling radiation under UVB
(Stellar and AGN radiation are not included)



Metal enriched along filaments
Filaments are bright at Lya line

Interdisciplinary science

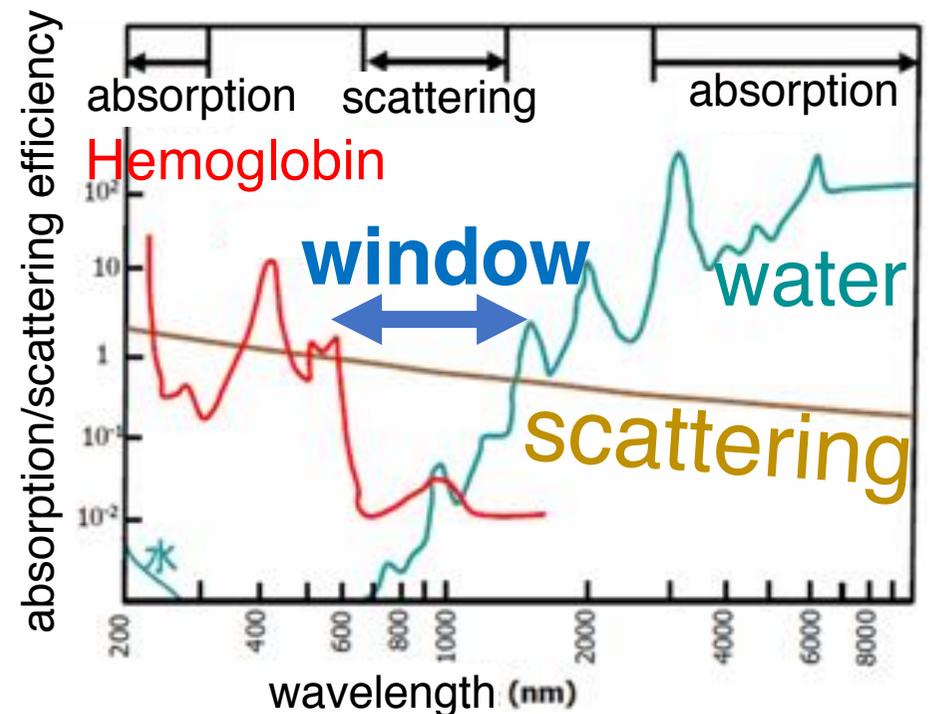
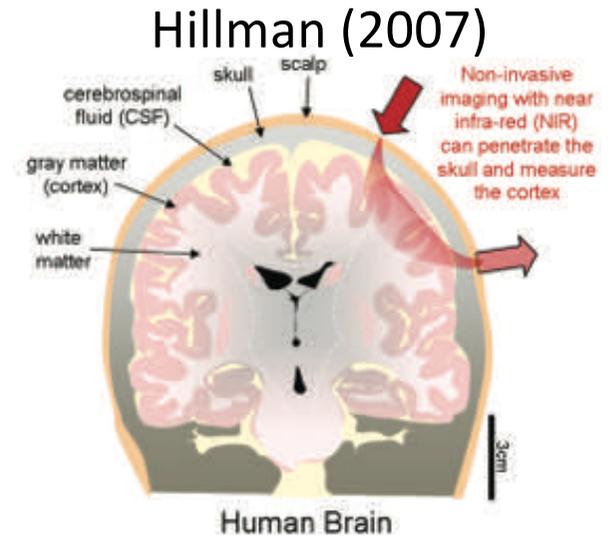


Optical/NIR bio-imaging

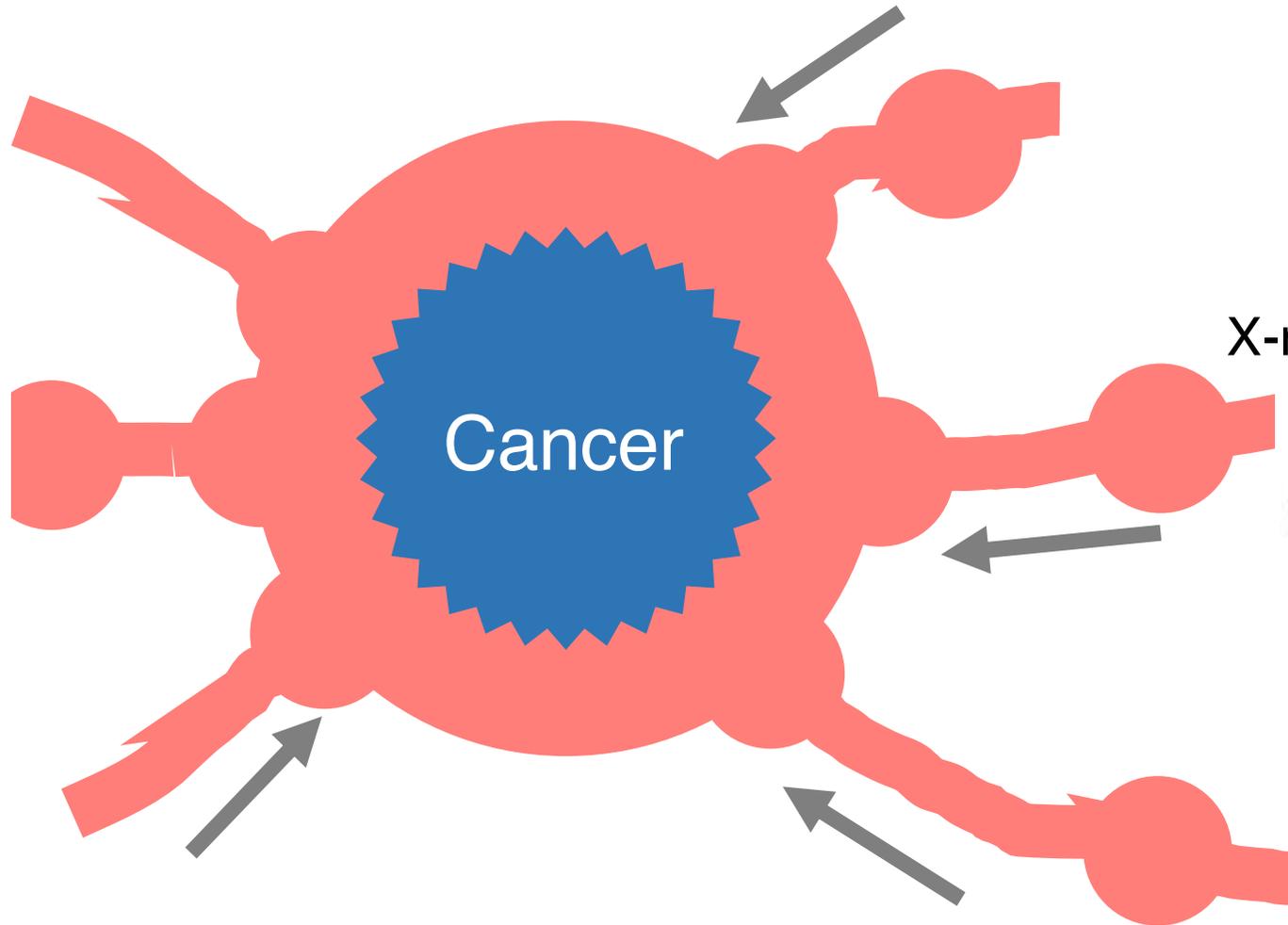
Medical diagnosis using near-infrared light which is returned from a human body via scattering processes

This diagnostic method requires radiative transfer simulations

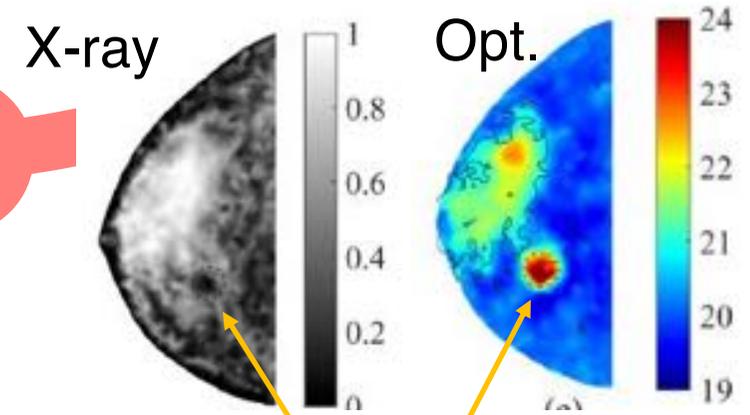
No radiative exposure, 
Non-invasive,
No contrast medium required,
No side effect,
Low-cost, high-time resolution
So, OK for new-born babies and infants



Cancer gathers blood



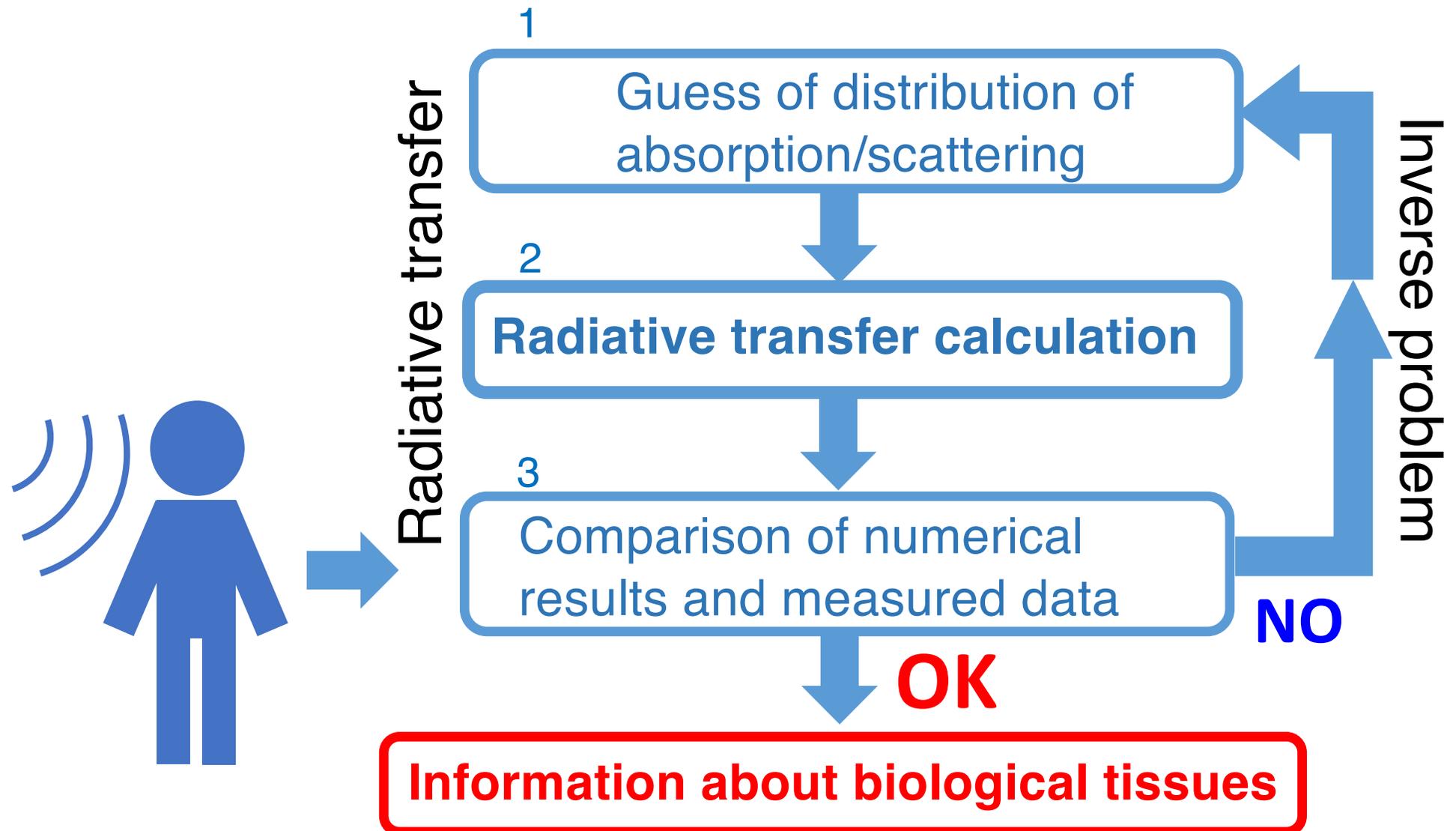
Breast cancer



Cancer

Increase of absorption efficiency

Diffuse Optical Tomography (DOT)

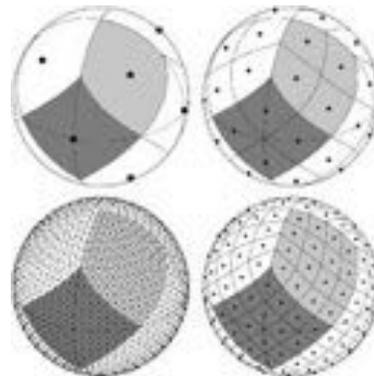
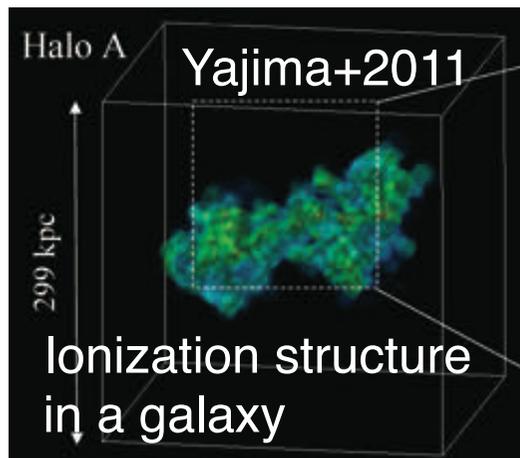


Numerical simulations of radiative transfer in a human body

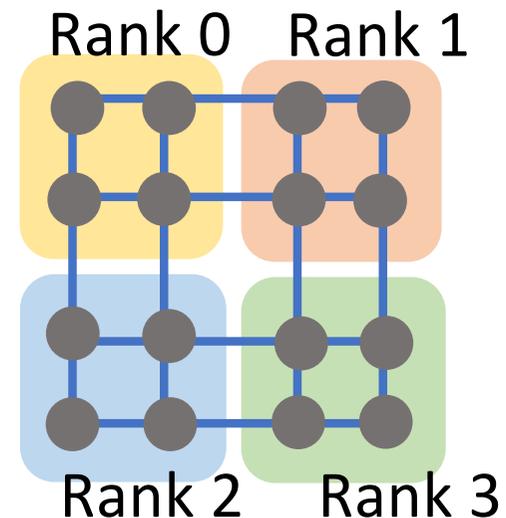
Basic equation

$$\frac{\partial I}{c\partial t} + n \cdot \nabla I = -\alpha I + \oint \phi(\Omega', \Omega) I d\Omega'$$

- * Scheme: ART method (Yajima+2009)
- * Angle grids made by HEALPix
- * Parallelization: domain decomposition



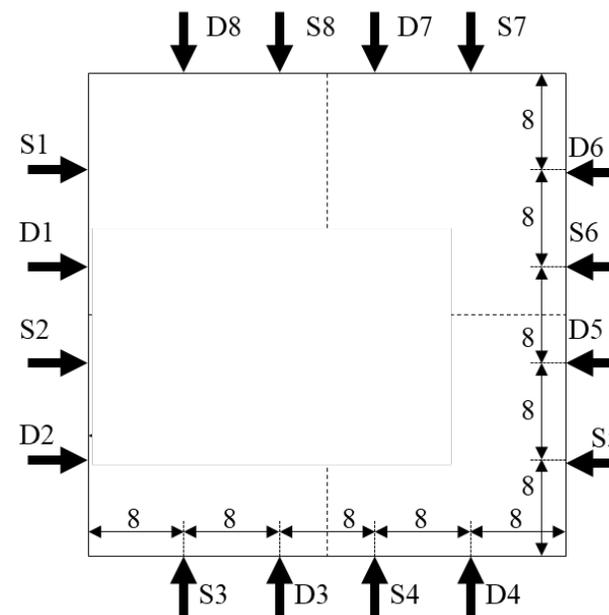
HEALPix (Gorski et al. 2005)



Test calculation

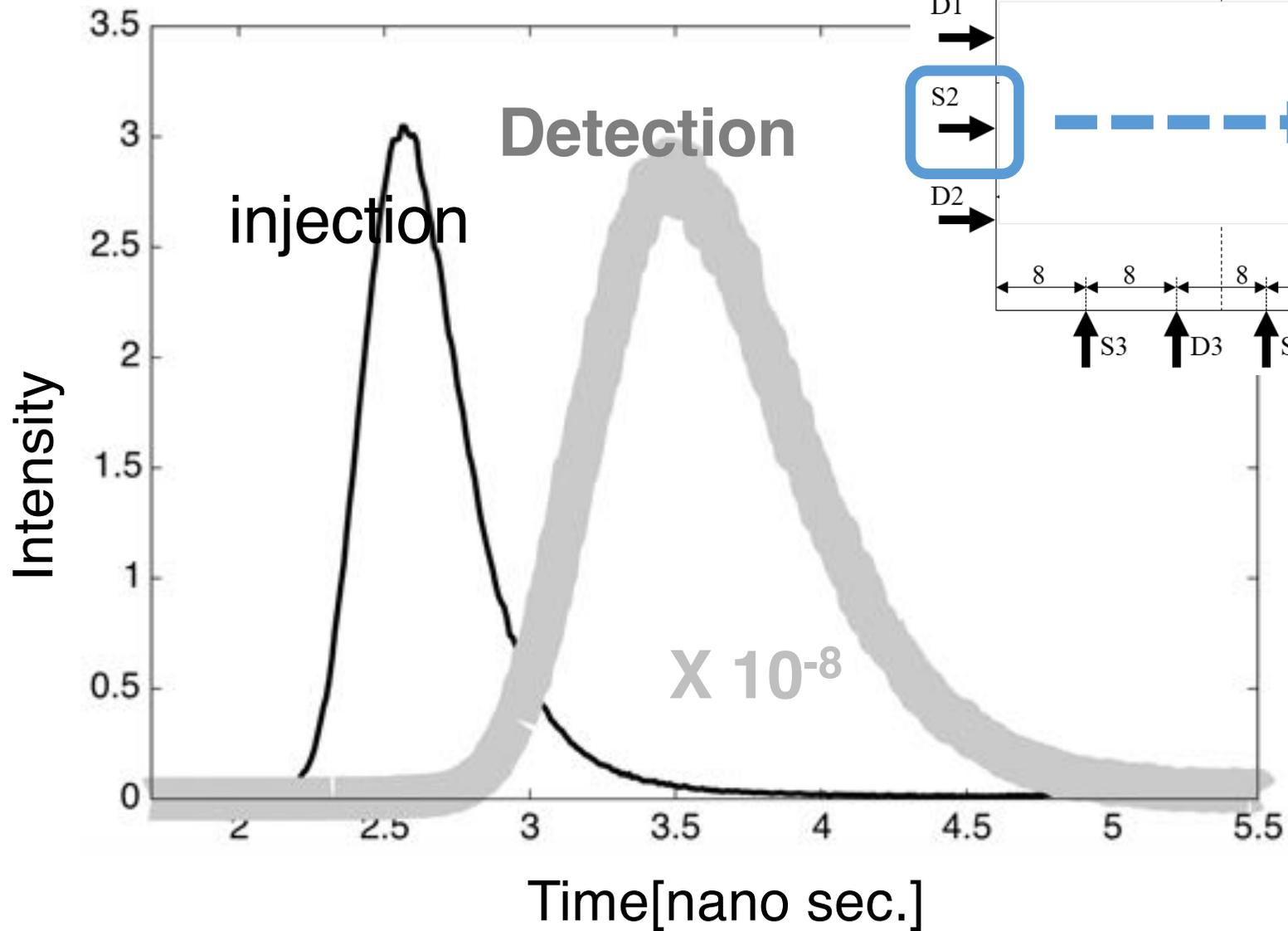
Pulse injection test for polyurethane modeling biological tissues

From Prof. Hoshi

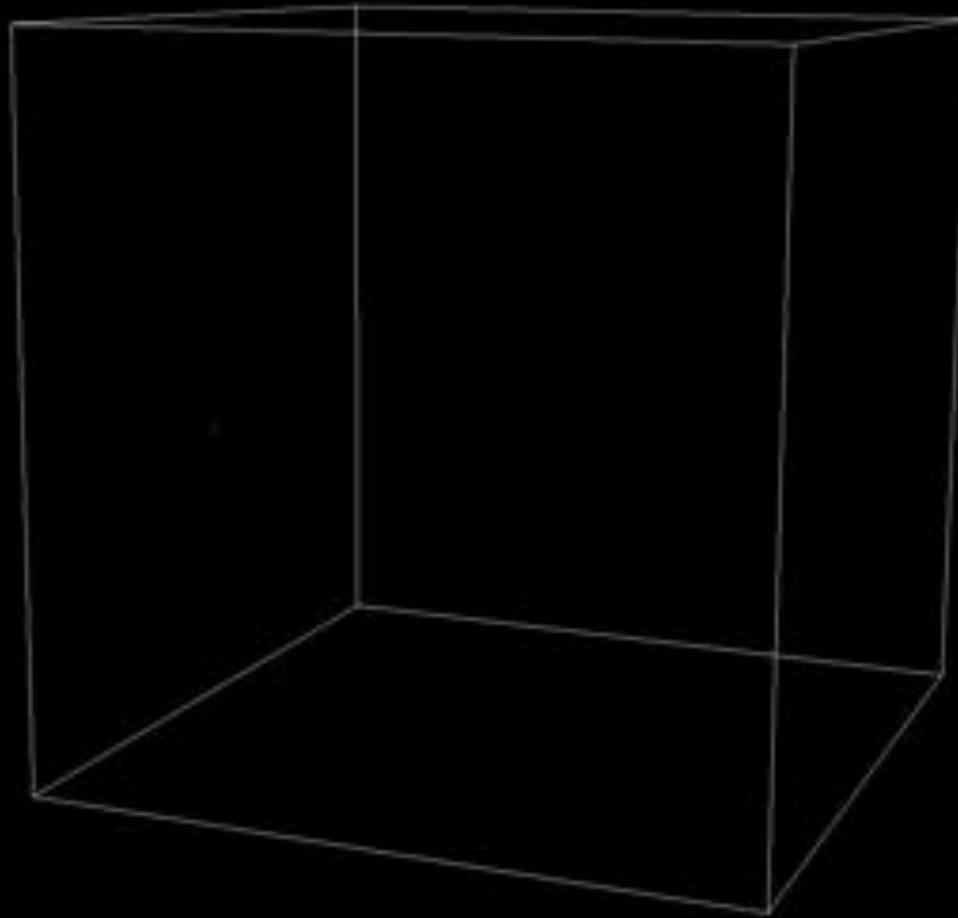


S, 照射 ; D, 受光、最短SD間隔, 8 mm
計測平面 : ファントム底面から、35 mm, 45 mm, 55 mm

Experimental data

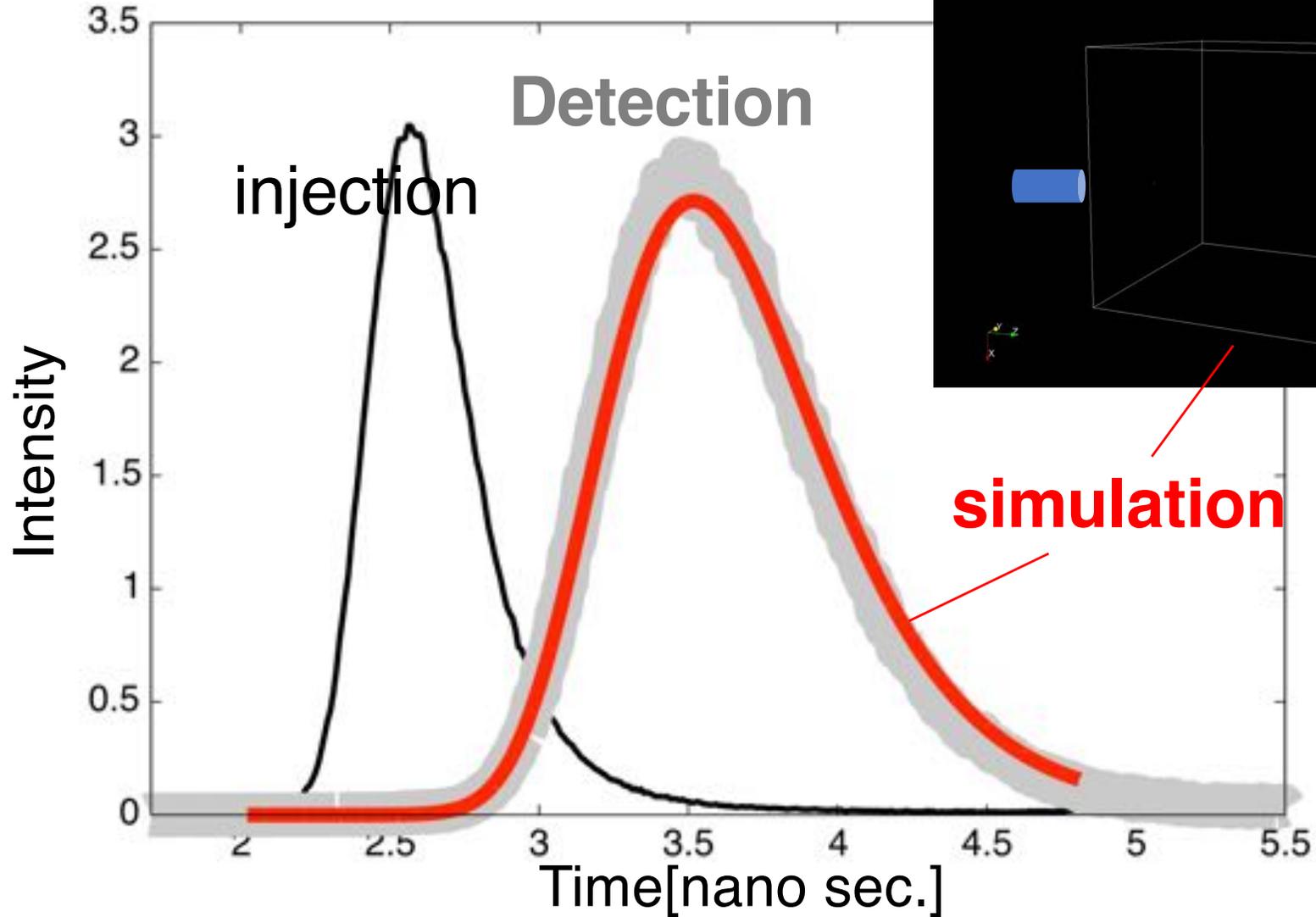


Simulation results



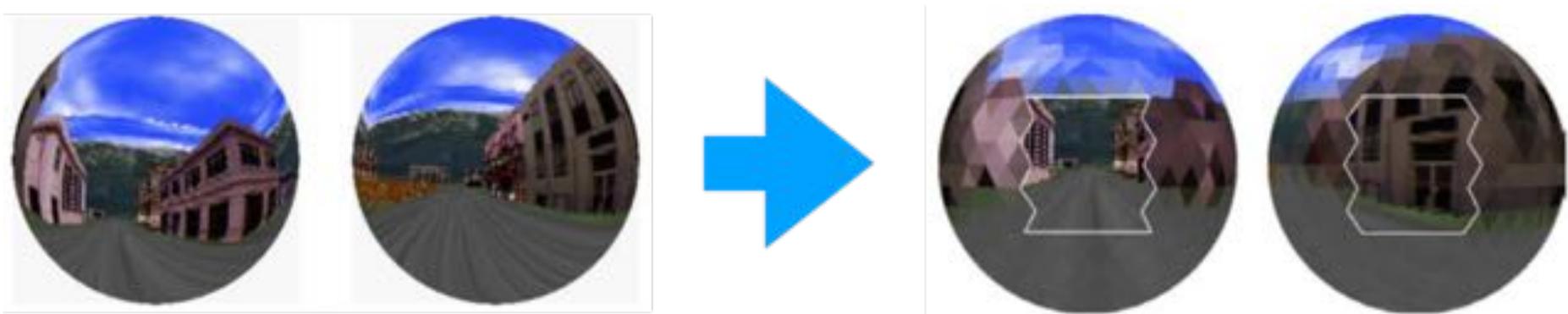
Simulation results

(Yajima, Abe, Umemura in prep.)



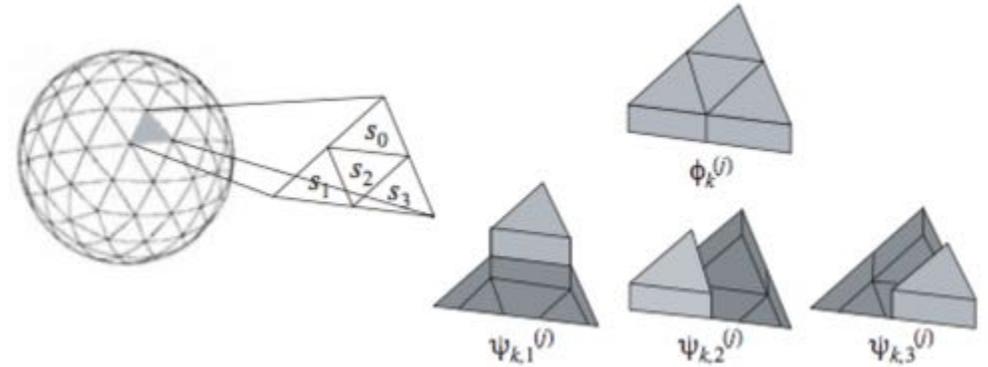
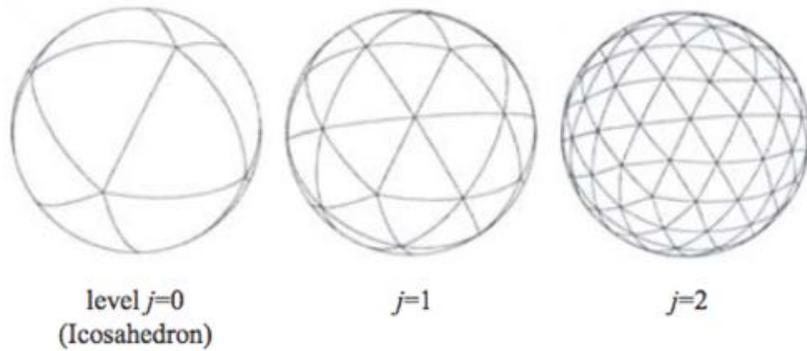
Spherical wavelet

Usual radiative transfer simulations take huge memory
place (x,y,z) , direction (θ, ϕ) , time(~ 10) $\Rightarrow \sim 1\text{TB}$



By using spherical wavelet method, we reduce memory and accelerate the simulations

Formulation

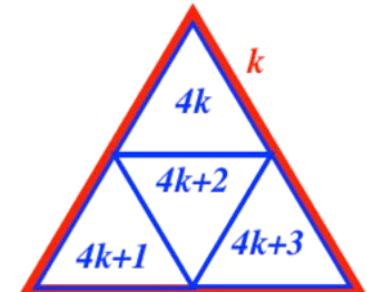


$$S_k^{(j)}(\vec{n}) = \lambda_k^{(0)} \varphi_k^{(0)}(\vec{n}) + \sum_{j=0}^{J-1} \sum_{m=1}^3 \gamma_{k,m}^{(j)} \psi_{k,m}^{(j)}(\vec{n})$$

where

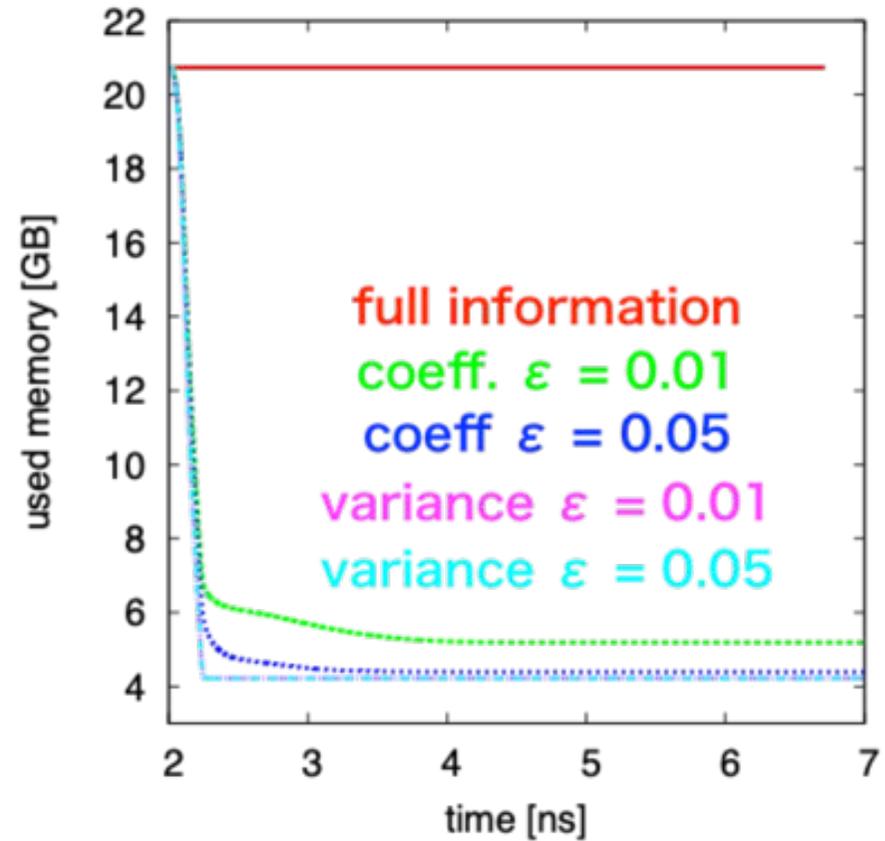
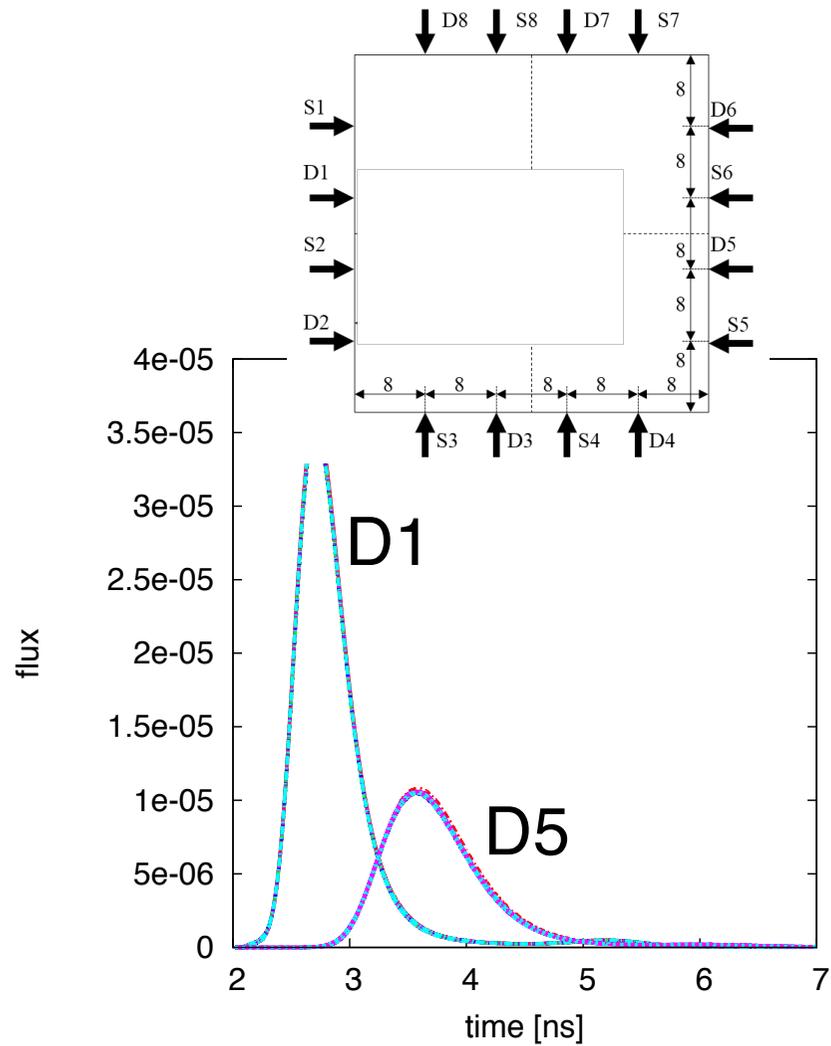
$$\lambda_k^{(j)}(\vec{n}) = \int d\Omega' I^{(j+1)}(\vec{n}') \int d\Omega \phi^{(j+1)}(\vec{n}, \vec{n}') \varphi_k^{(j+1)}(\vec{n}) \equiv \int d\Omega' I^{(j+1)}(\vec{n}') w_{\lambda,k}^{(j)}(\vec{n}', \vec{n})$$

$$\gamma_{k,m}^{(j)}(\vec{n}) = \int d\Omega' I^{(j+1)}(\vec{n}') \int d\Omega \phi^{(j+1)}(\vec{n}, \vec{n}') \gamma_{k,m}^{(j+1)}(\vec{n}) \equiv \int d\Omega' I^{(j+1)}(\vec{n}') w_{\gamma,k,m}^{(j)}(\vec{n}', \vec{n})$$



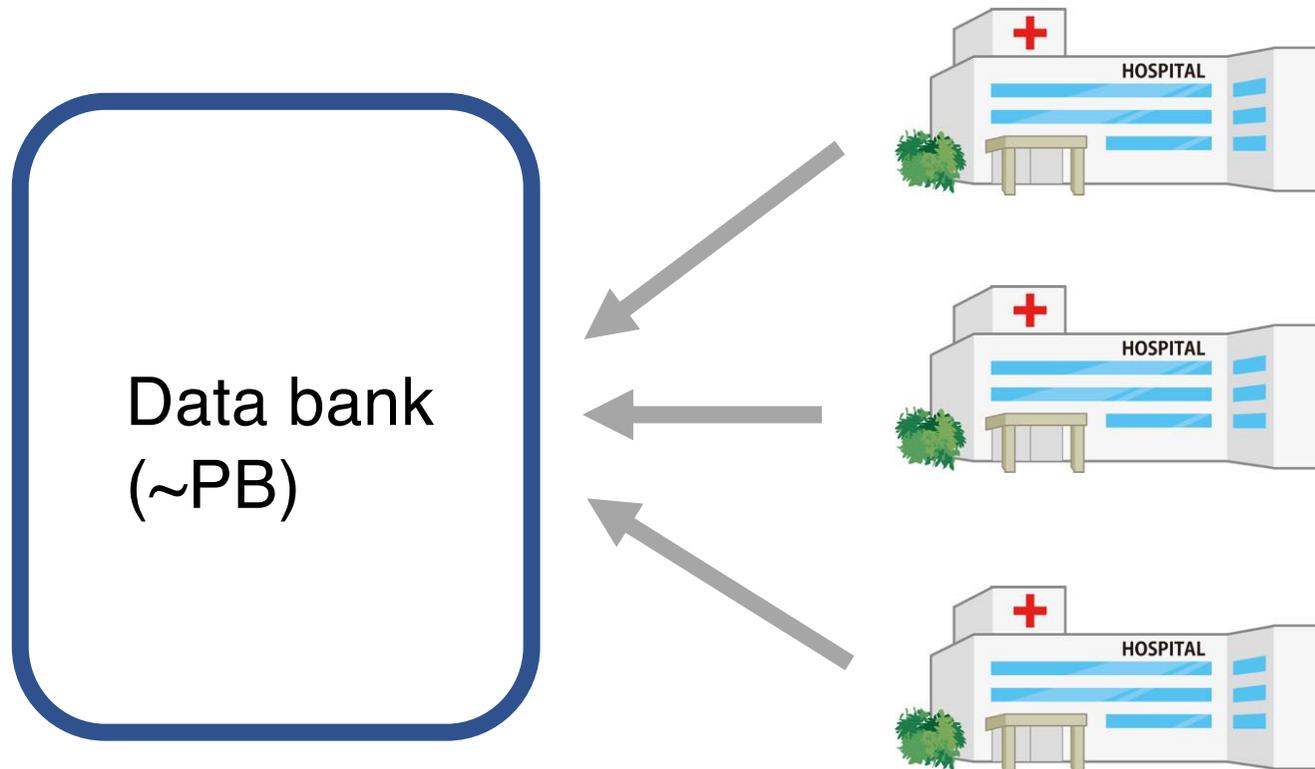
Reduced memory

(Abe, Yajima, Umemura in prep.)



Future plan

Acceleration of radiative transfer simulations
with FPGA/GPU on Cygnus
Simulations of huge parameter space



Summary

- We study galaxy formation and radiative properties by combining cosmological hydrodynamics simulations and radiative transfer calculations
- We find the galaxy evolve with supernova feedback and the radiative properties rapidly change that reproduce the observed diversity of distant galaxies
- We develop a new radiative transfer code to model near-infrared bio-imaging, and show the simulation matches the experimental data nicely