

# Super asymmetric fission in super heavy nuclei

Michał Warda

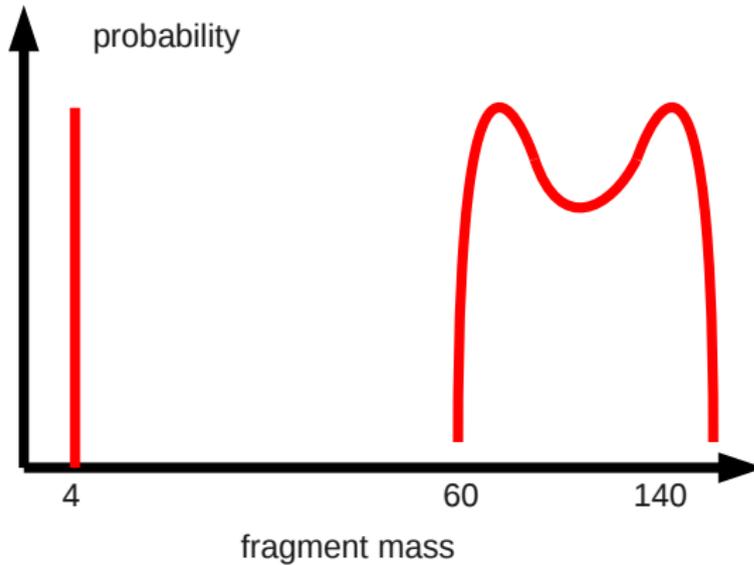
Uniwersytet Marii Curie-Skłodowskiej  
Lublin, Poland

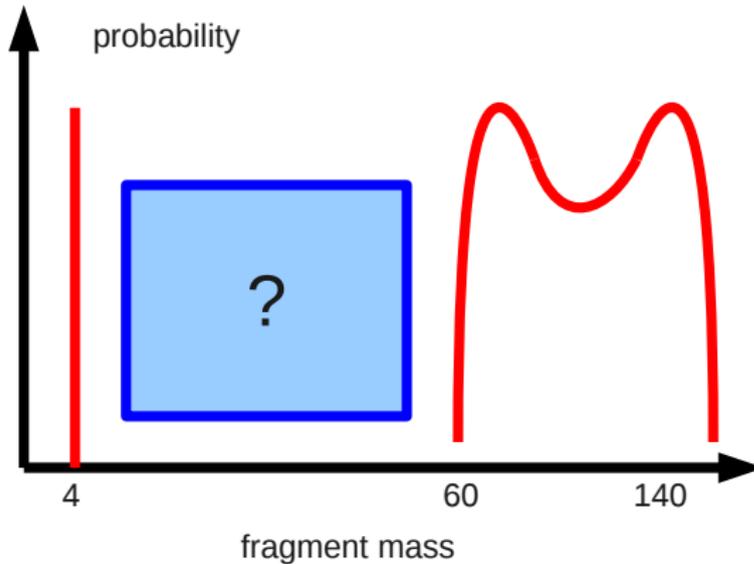
TSUKUBA, 10.12.2018



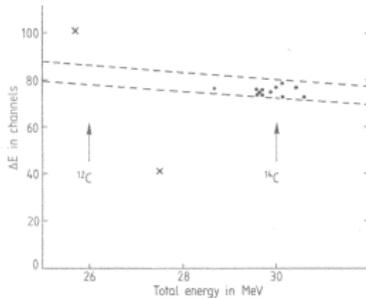
- L.M. Robledo, UAM, Madrid
- A. Zdeb, UMCS, Lublin / CEA, Bruyères-le-Châtel



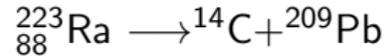




# Discovery of cluster radioactivity



**Fig. 1** Contents of the two-dimensional array  $\Delta E$  versus  $E_{\text{total}}$  after a run of 189 days. The dotted line indicates the allowed region for carbon ions and the arrows indicate the total energies expected for  $^{12}\text{C}$  and  $^{14}\text{C}$  emissions in the decay of  $^{223}\text{Ra}$ . The lower of the two crosses represents a quadruple pile-up. Below the total energy displayed, large numbers of triple and double  $\alpha$ -pile-ups were recorded. Single  $\alpha$ -events (and, in part, even double  $\alpha$ -pile-ups) were biased out on the analogue side to avoid deadtime problems on the digital side. The upper cross is an event which was recorded during a thunderstorm which affected the mains badly. A run of 194 days was made before this one, yielding 8 events and, in addition, a run of approximately half a year was performed to investigate possible cosmic ray-induced events. Channel 77 in  $\Delta E = 6.7$  MeV, which is exactly as expected for 30 MeV  $^{14}\text{C}$ . Detector characteristics: The dead layer of the  $\Delta E$  detector ( $200\text{ mm}^2$  active area,  $8.2\ \mu\text{m}$  sensitive thickness) was determined to lie between  $0.3$  and  $0.8\ \mu\text{m}$ . In addition a protective layer of gold of thickness  $20\ \mu\text{g cm}^{-2}$  was evaporated on the source and  $15\ \mu\text{g cm}^{-2}$  carbon film inserted between the source and the  $\Delta E$  detector. An extra  $30\text{--}40\ \mu\text{g cm}^{-2}$  of gold is present on the  $E$ -detector ( $300\text{ mm}^2$  active area). This gives a total of  $150\text{--}250\ \mu\text{g cm}^{-2}$  of effective dead layer (Si equivalent) and an energy loss of  $^{14}\text{C}$  ions of  $0.5\text{--}0.8$  MeV. The source of strength  $3.3\ \mu\text{Ci}$  gave a counting rate of  $\approx 4,000\ \text{s}^{-1}$ , corresponding to an effective solid angle of detection of  $\approx 1/3$  sr.



H.J. Rose and G.A. Jones, *Nature* **307**, 245 (1984)  
 Sandulescu, Poenaru and Greiner, *Sov. J. Part Nucl.* **11**, 528 (1980)



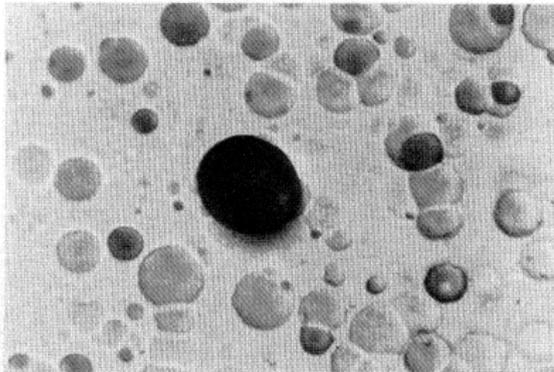


FIG. 1. Photomicrograph showing one etch pit due to a 56 MeV  $^{24}\text{Ne}$  ion striking a Cronar detector nearly head on. About  $3 \times 10^6$  alpha particles passed through this field of view.

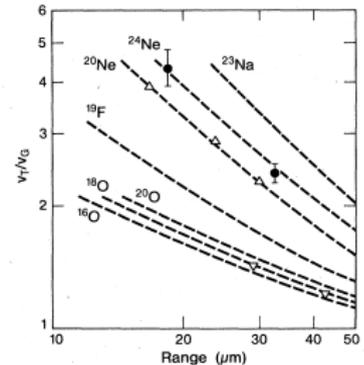


FIG. 2. Comparison of average signal of  $^{24}\text{Ne}$  nuclei ( $\bullet$ ) emitted from  $^{232}\text{U}$  with calibrations (dashed lines) obtained with  $^{18}\text{O}$  ( $\nabla$ ) and  $^{20}\text{Ne}$  ( $\Delta$ ) ions at Lawrence Berkeley Laboratory accelerators. Ratio of etching rate along track to general etching rate  $v_T/v_G$ , is plotted as a function of residual range.

Barwick et al., PRC 31, 1984 (1985)



# Cluster radioactivity: key facts

- Emitters:  ${}_{87}^{221}\text{Fr}$  —  ${}_{96}^{242}\text{Cm}$   
experimental evidence in 12 even-even, 9 odd nuclei
- Clusters:  ${}^{14}\text{C}$  —  ${}^{34}\text{Si}$
- Heavy mass residue: doubly magic  ${}^{208}\text{Pb} \pm 4$  nucleons  
"Lead radioactivity"
- Half lives:  $10^{11}$  s —  $10^{26}$  s
- $\alpha$  branching ratio:  $10^{-9}$  —  $10^{-16}$



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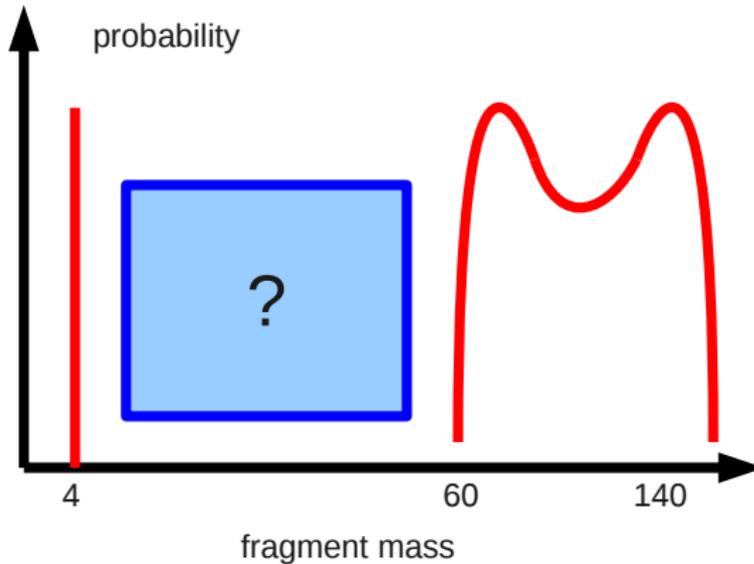
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# Theoretical description

- Extrapolation of Gamov model of alpha emission
- Modified Geiger-Nuttall formula for half-lives
- Very asymmetric fission
- Potential energy surfaces are determined in the self-consistent procedure in HFB theory with Gogny D1S force



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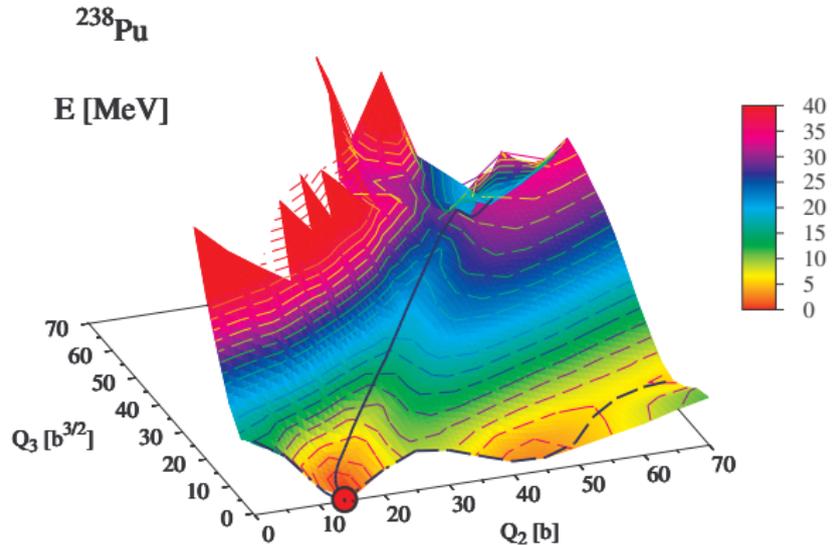
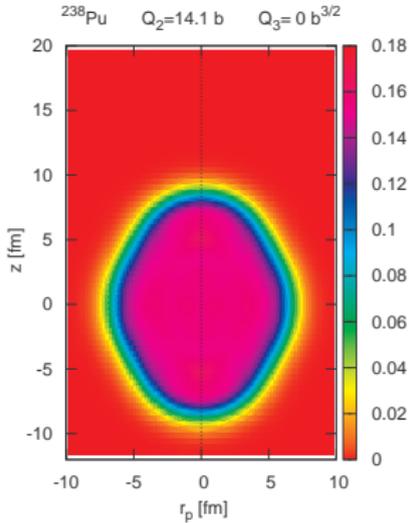


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# Shape evolution: $^{238}\text{Pu}$

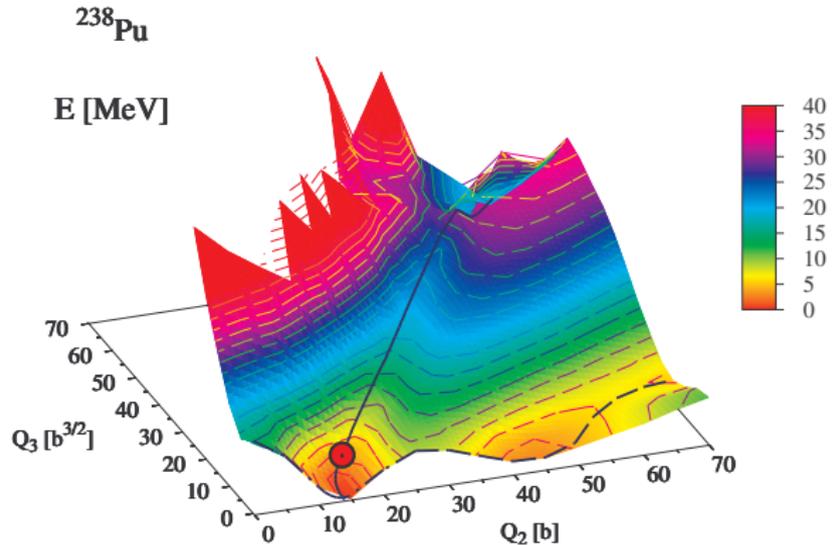
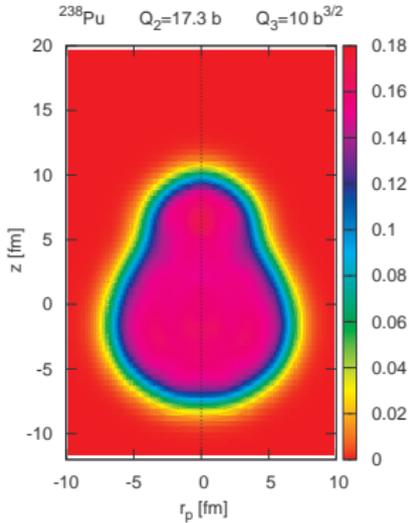


M. Warda and L. M. Robledo, Phys. Rev. C 84, 044608 (2011).

[www.umcs.lublin.pl](http://www.umcs.lublin.pl)



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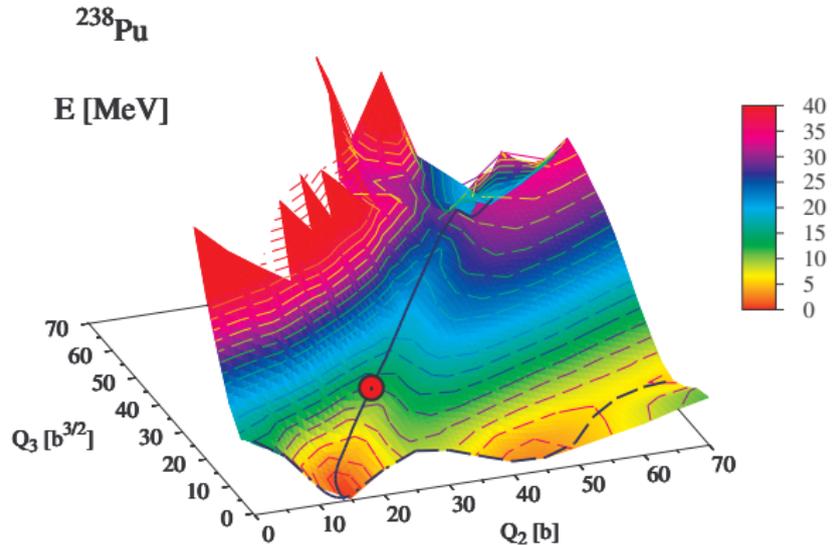
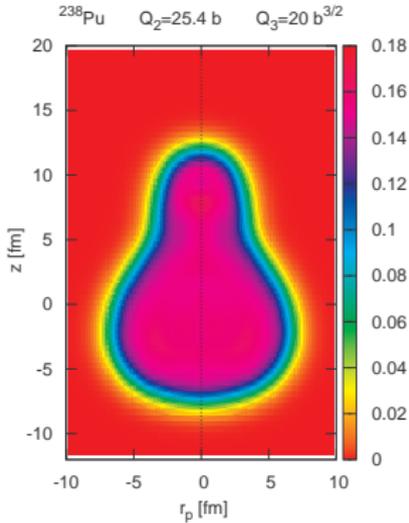


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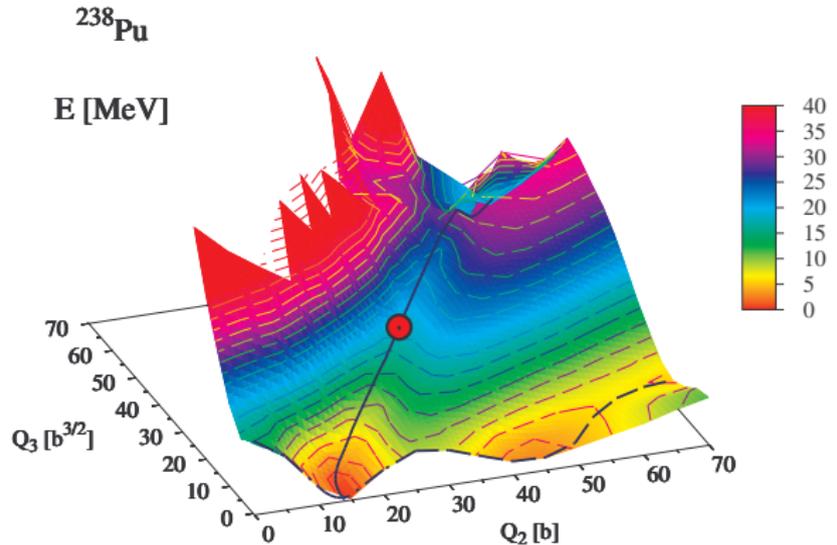
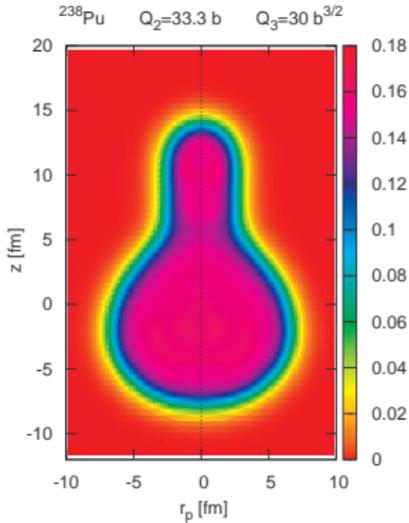


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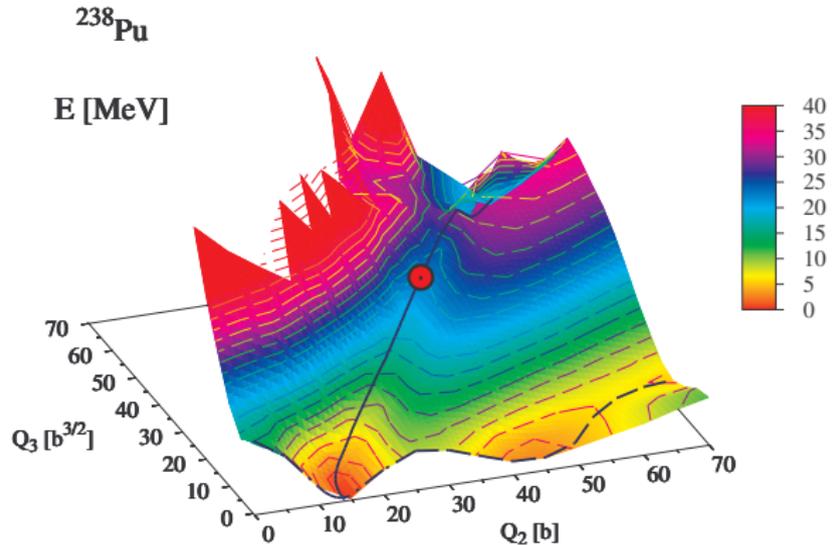
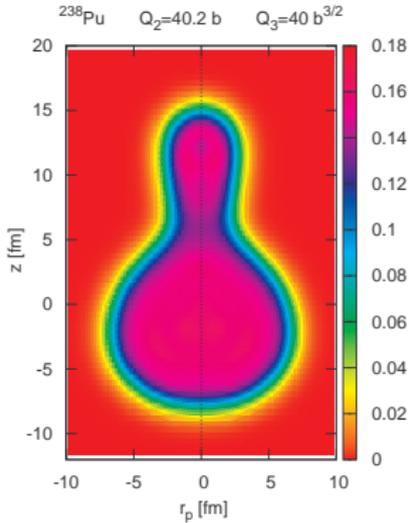


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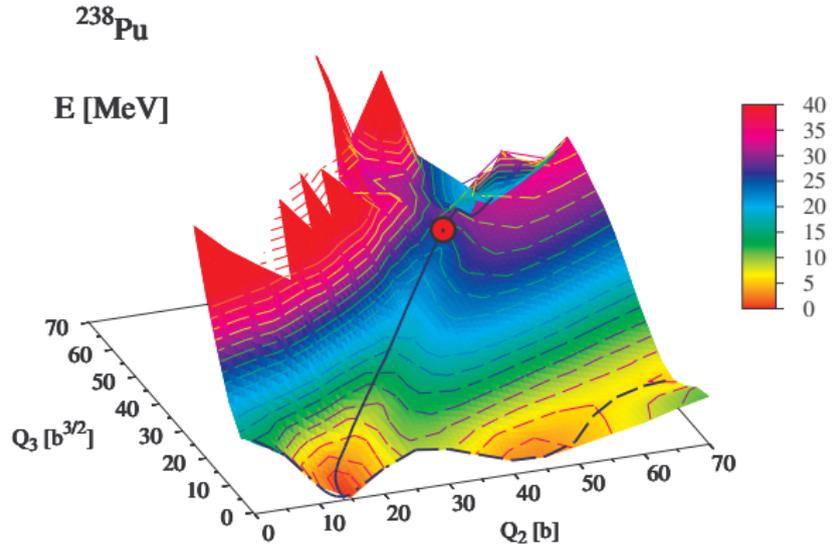
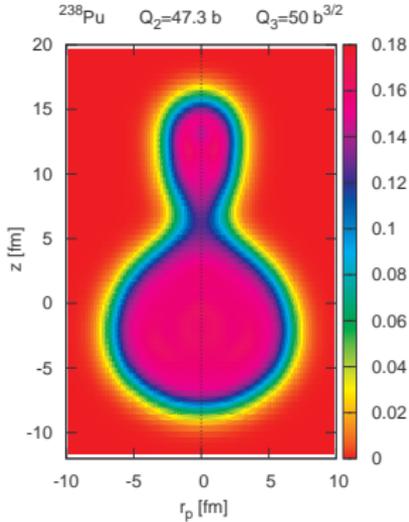


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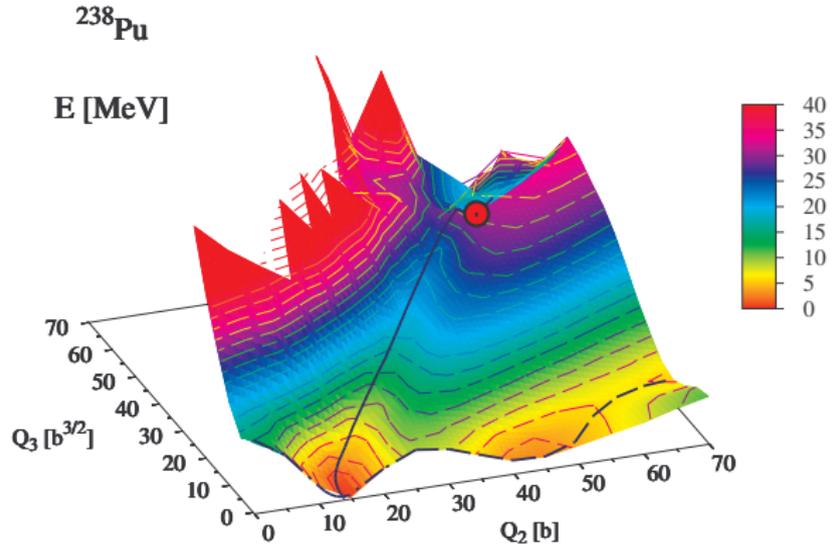
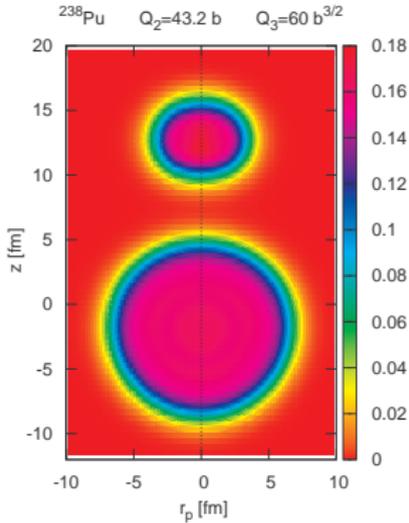


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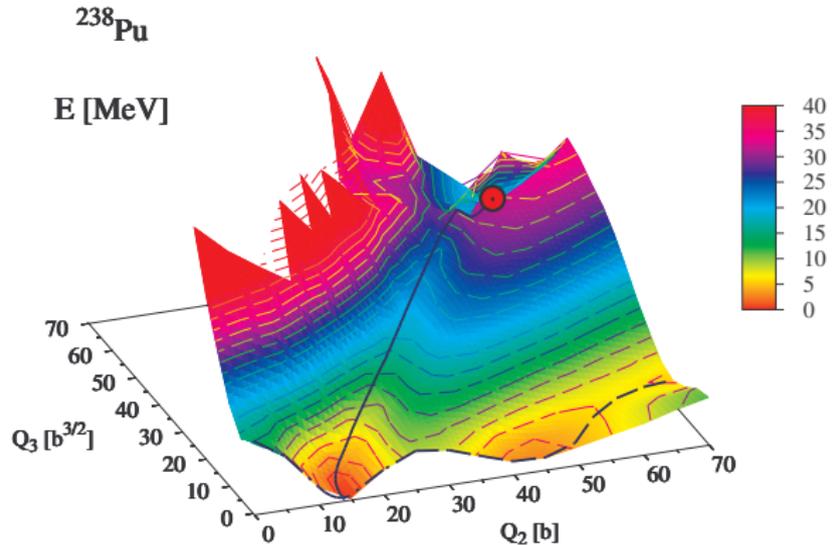
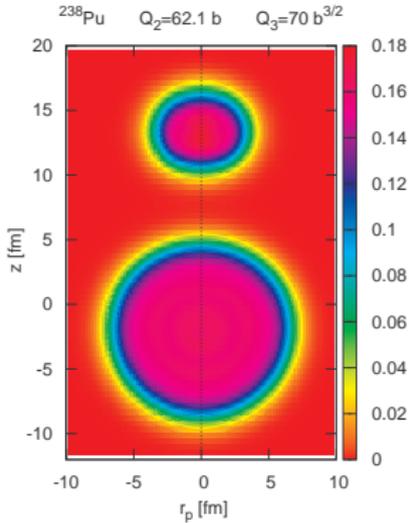


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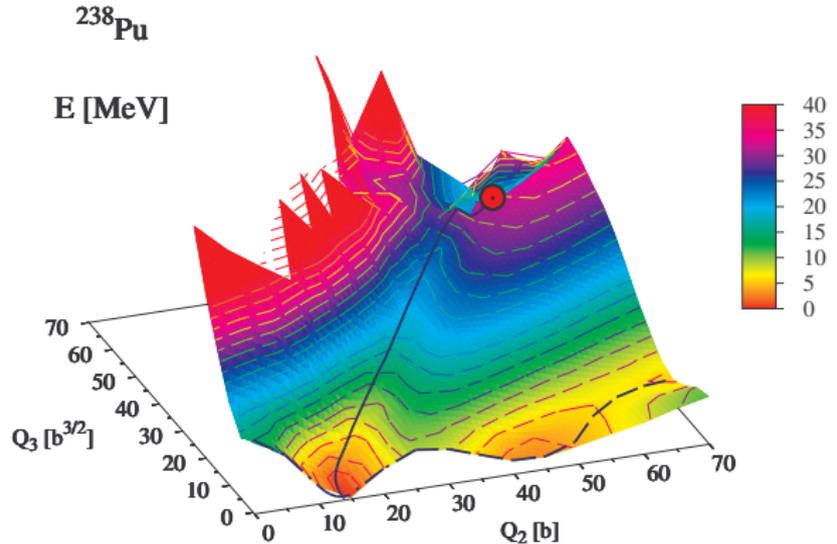
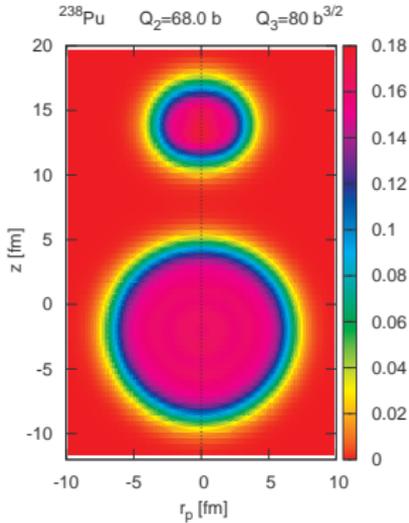


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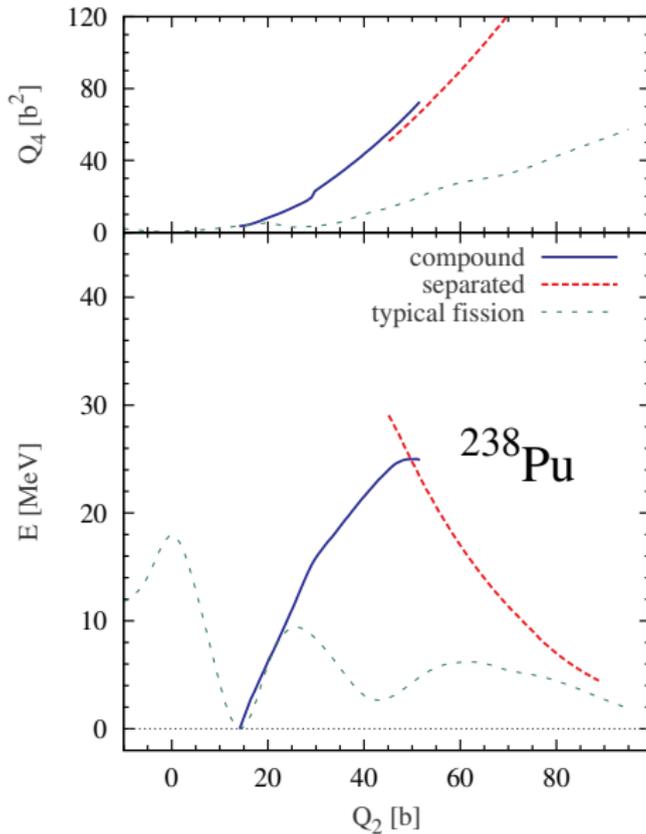
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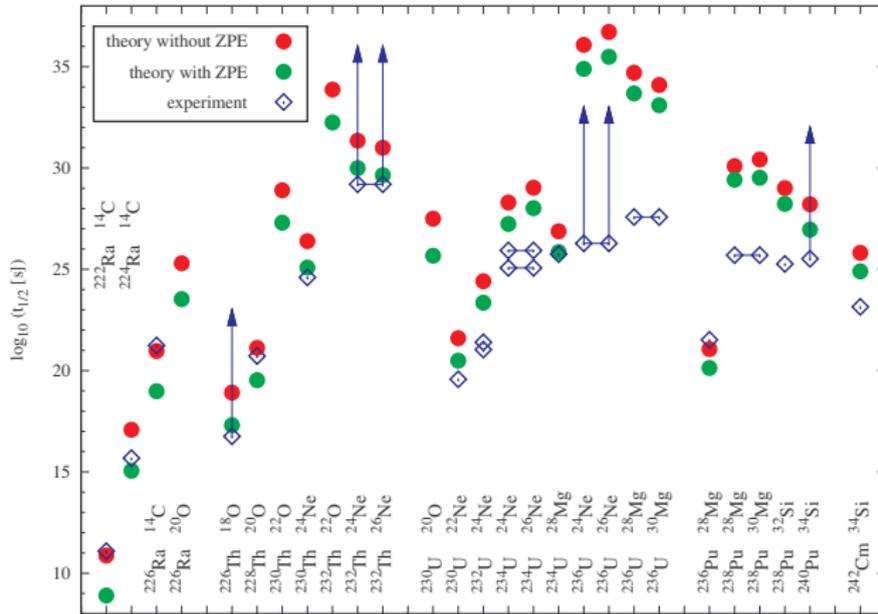


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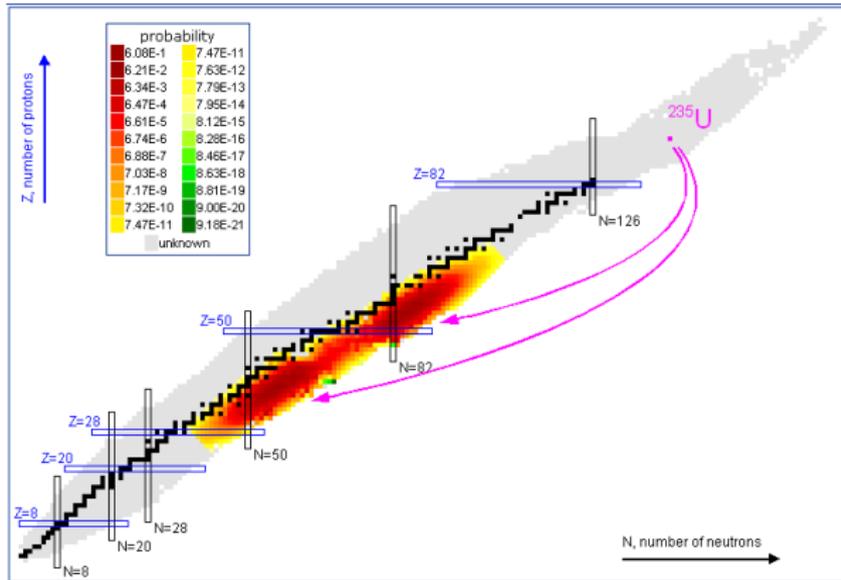
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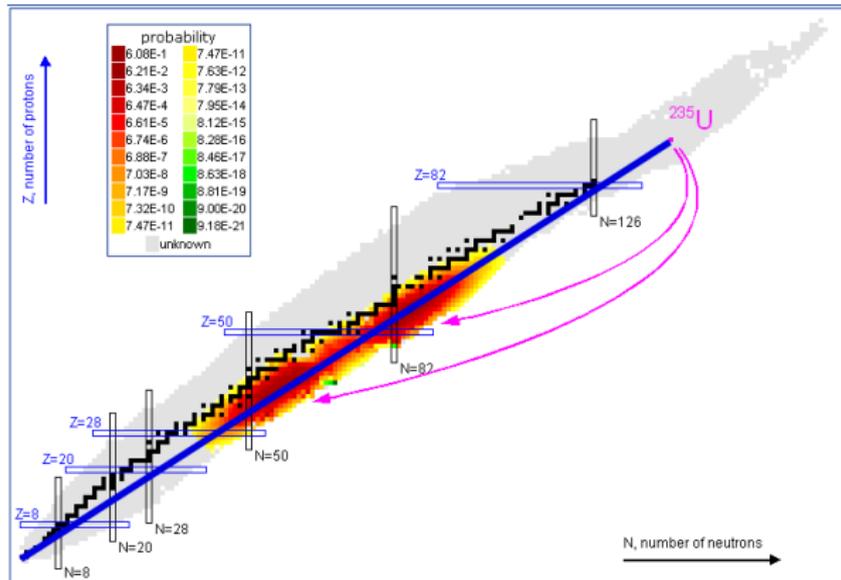


# Fission fragments - N/Z ratio



<http://lablementlounge.blogspot.com/2011/03/why-fuel-rods-are-radioactive.html>

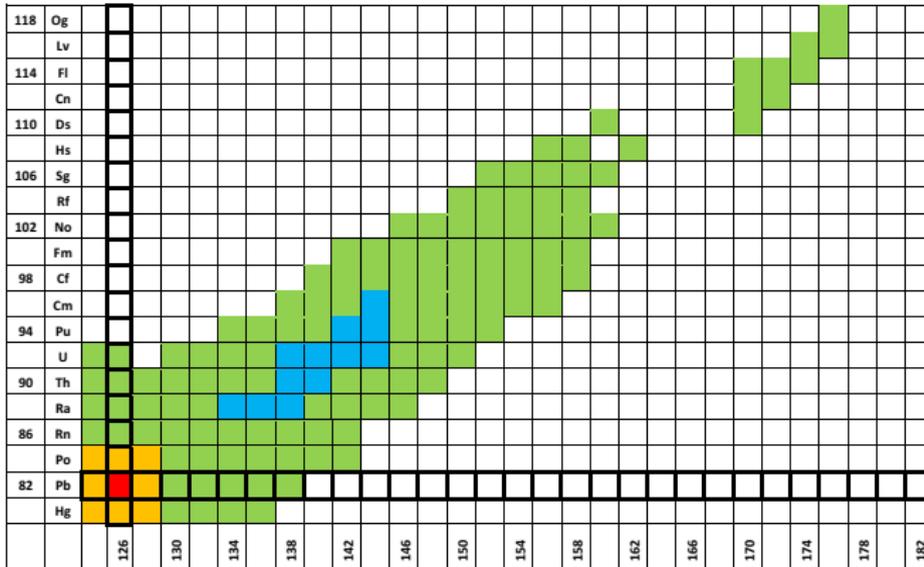
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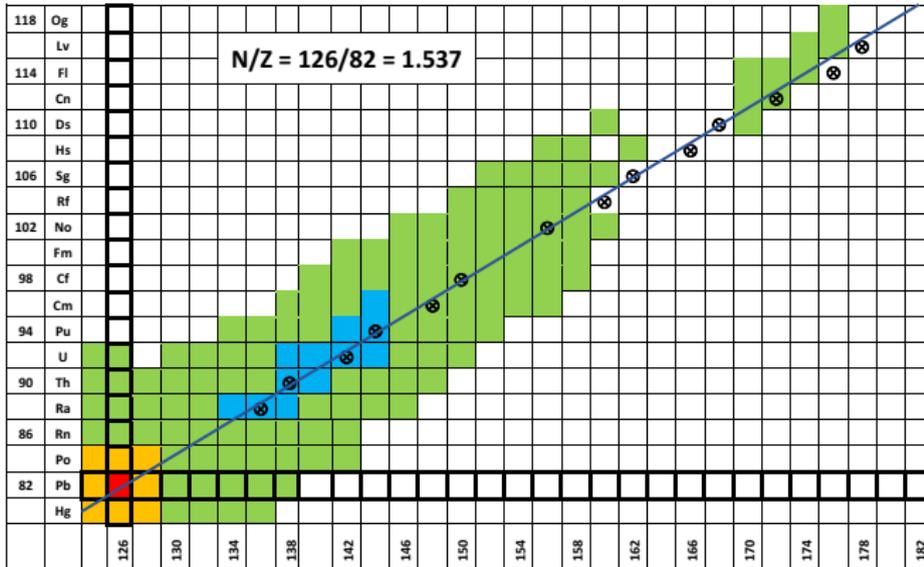


# Cluster radioactivity - chart of nuclides

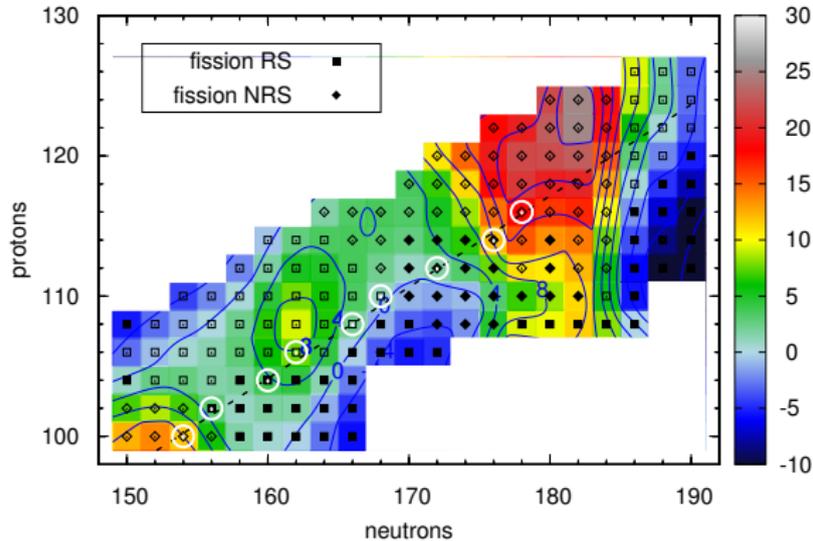




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# Chart of SH nuclides

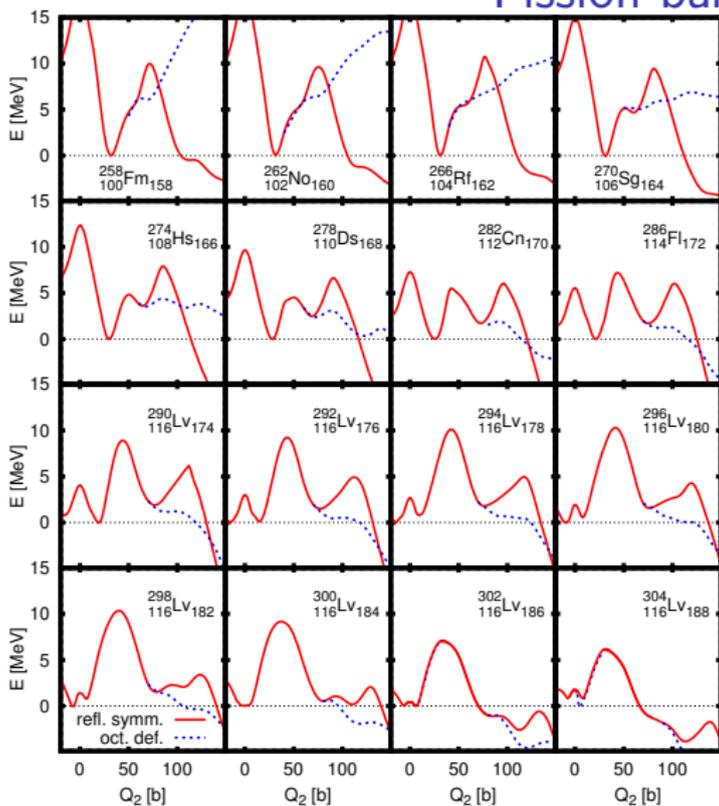


M. Warda, J.L. Egido, Phys. Rev. C 86 (2012) 014322

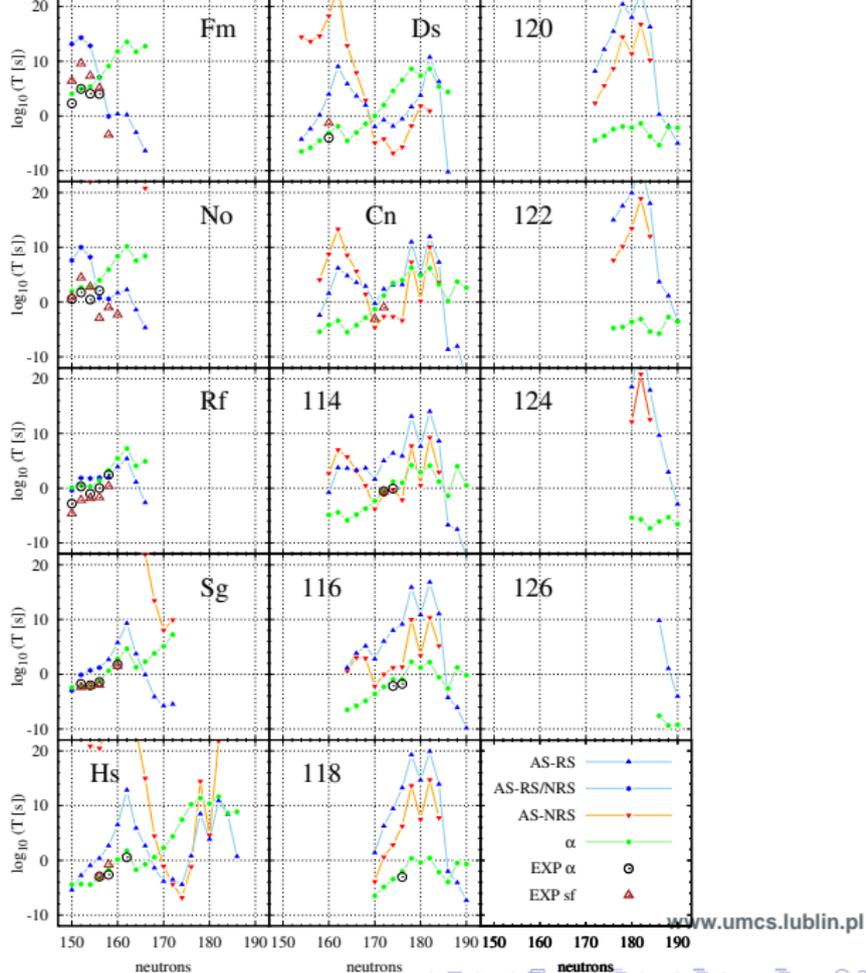
A. Baran, M. Kowal, P.G. Reinhard, L.M. Robledo, A. Staszczak, M. Warda, Nucl. Phys. A 944 (2015) 442



# Fission barriers



# Fission and $\alpha$ -decay half-lives



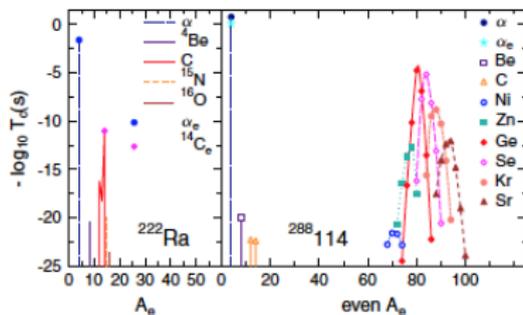
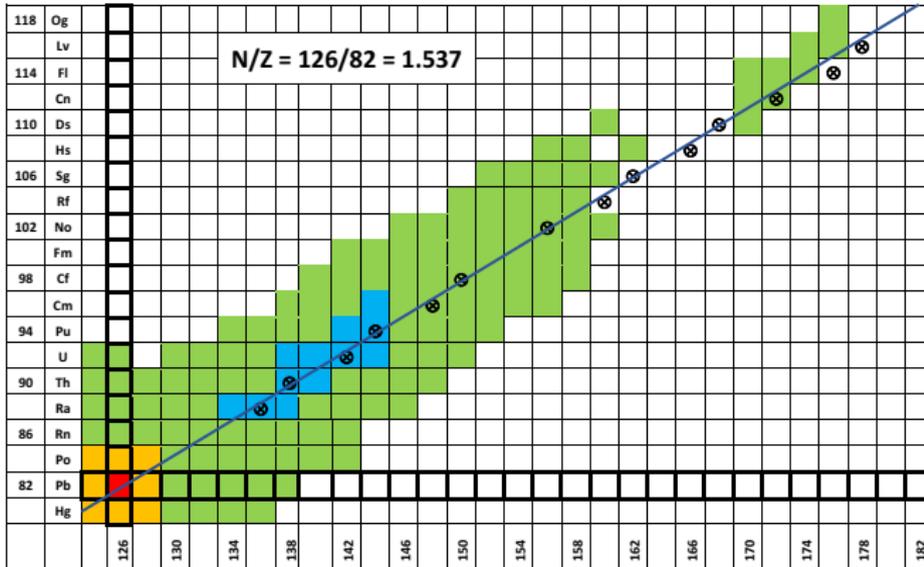


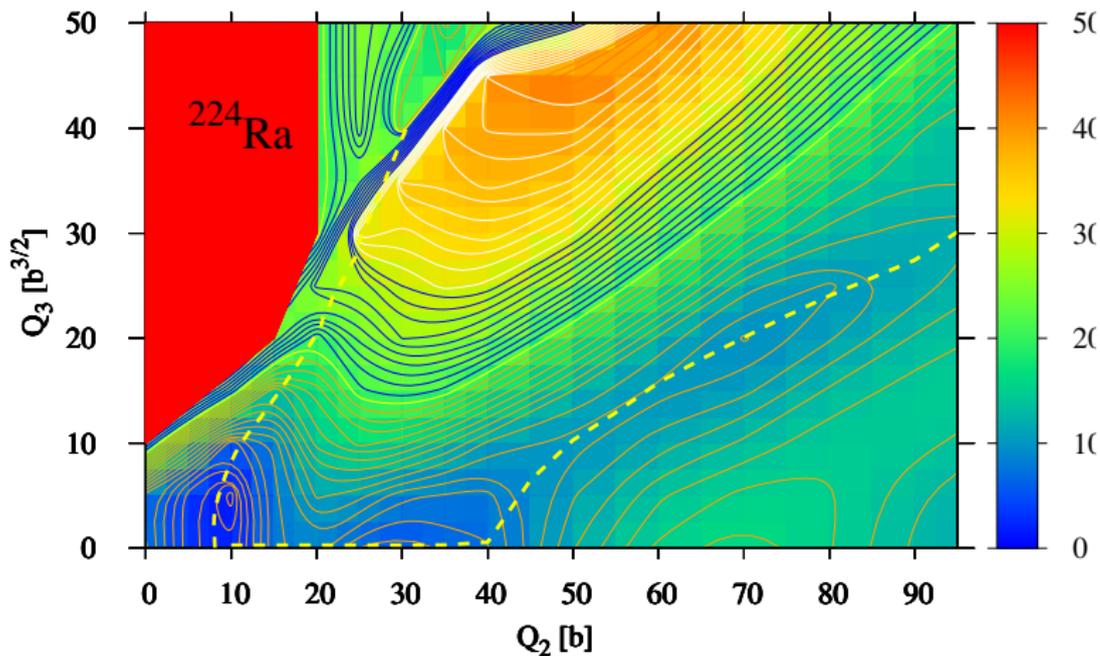
FIG. 1 (color online). Time spectra of different cluster emissions from  $^{222}\text{Ra}$  (left panel) and from the superheavy nucleus  $^{288}114$  (right panel). The most probable emitted clusters from  $^{222}\text{Ra}$  and  $^{288}114$  are  $^{14}\text{C}$  and  $^{80}\text{Ge}$ , respectively, both leading to  $^{208}\text{Pb}$  daughter nucleus.

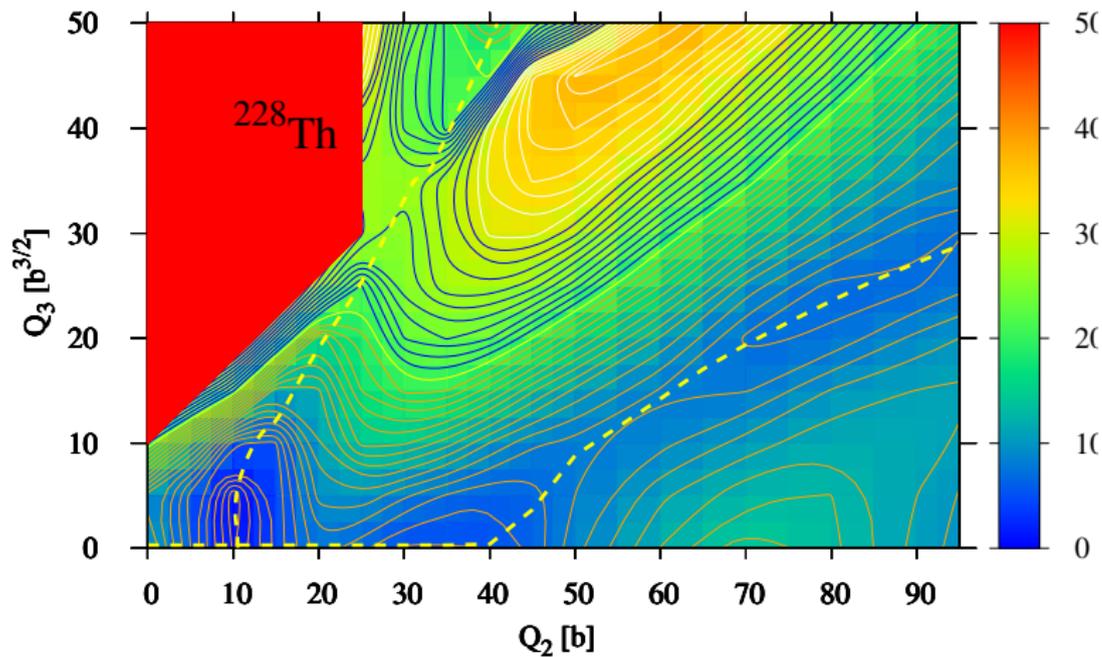
D. N. Poenaru, R. A. Gherghescu, and W. Greiner  
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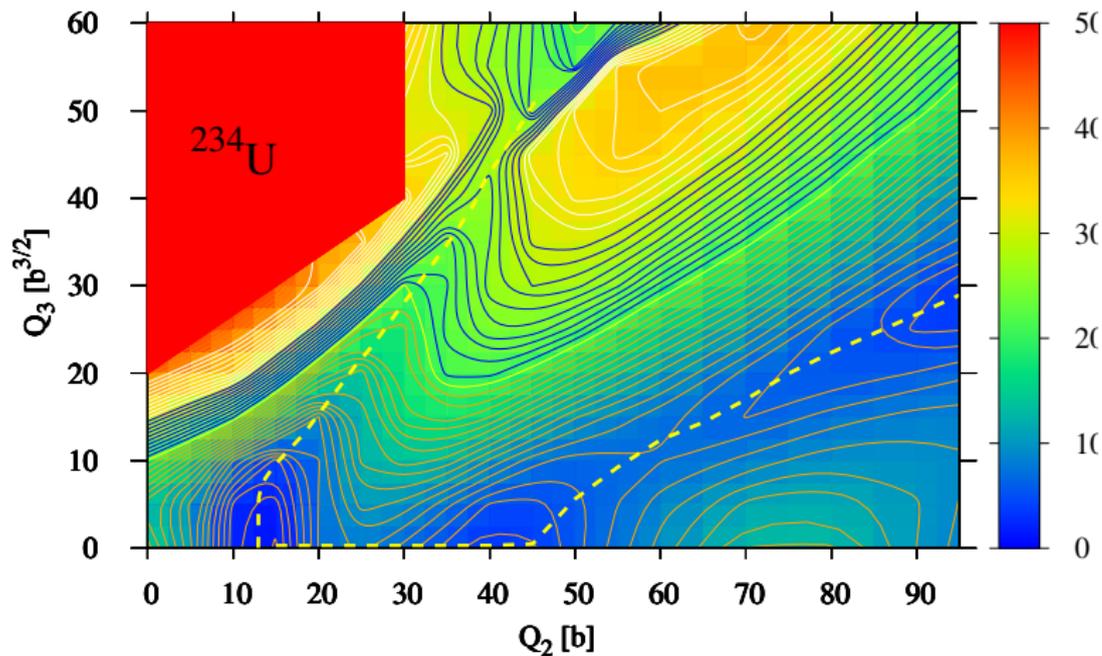


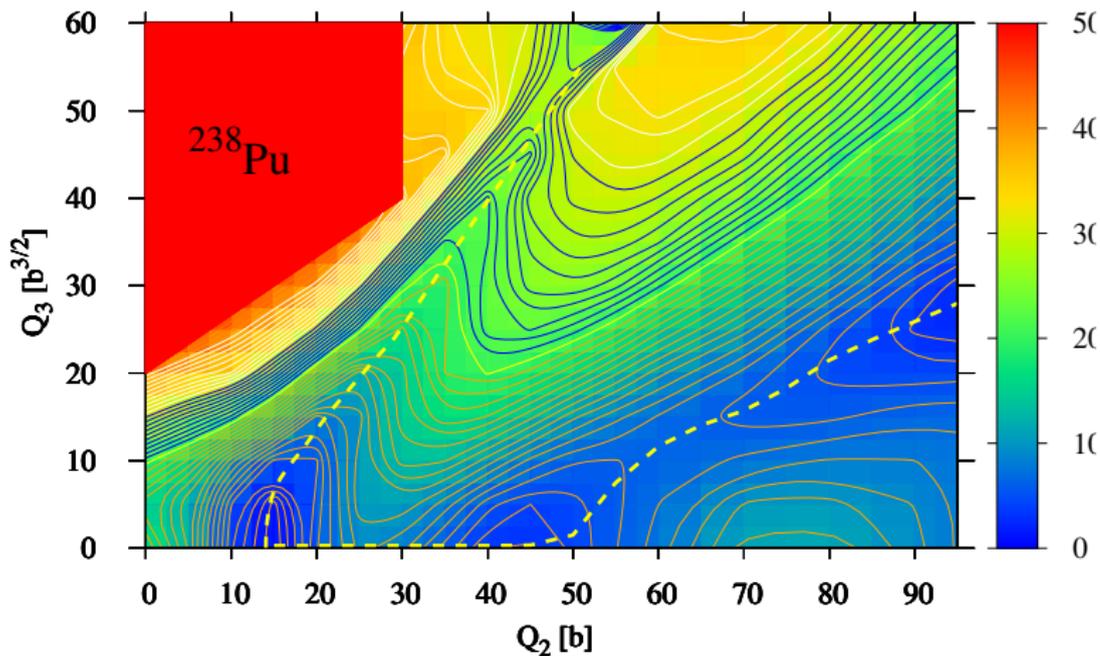
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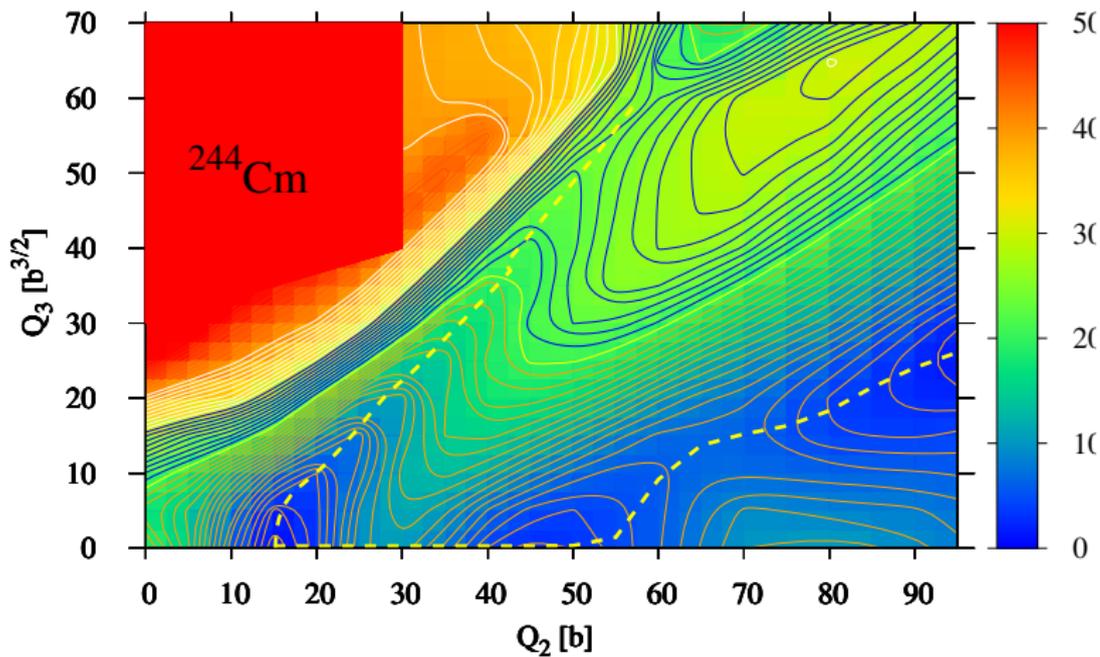


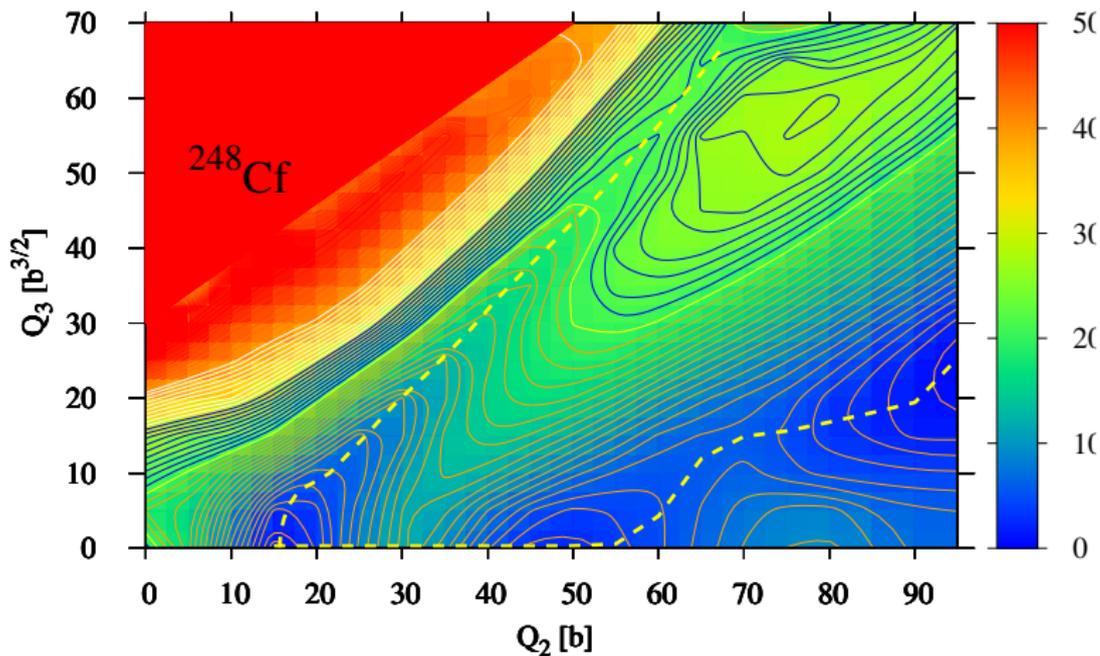


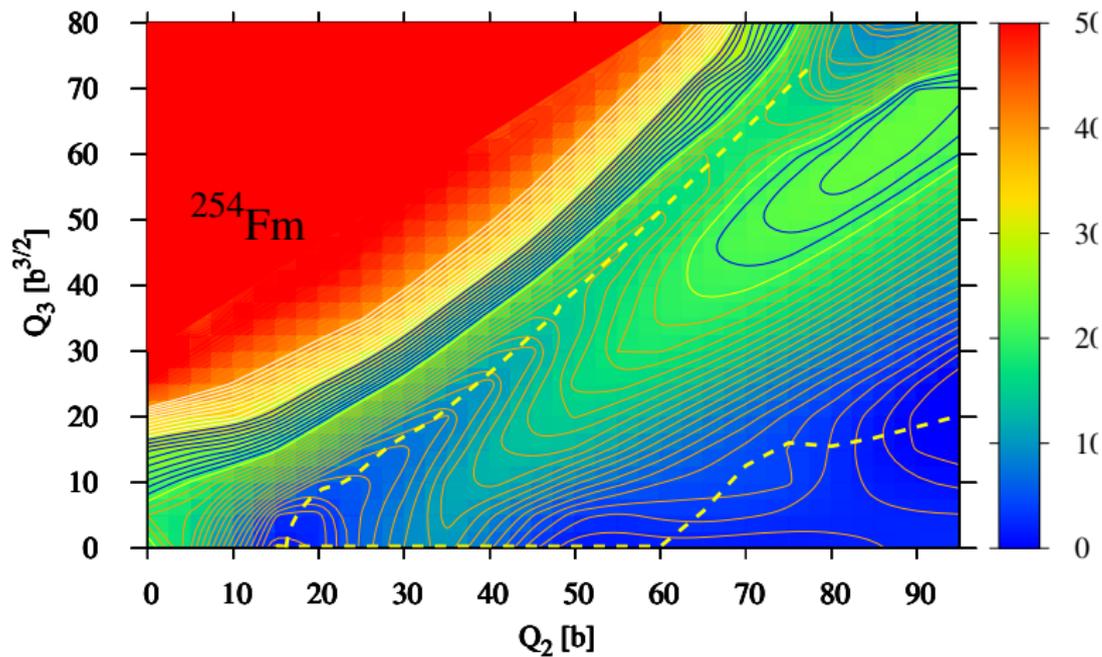


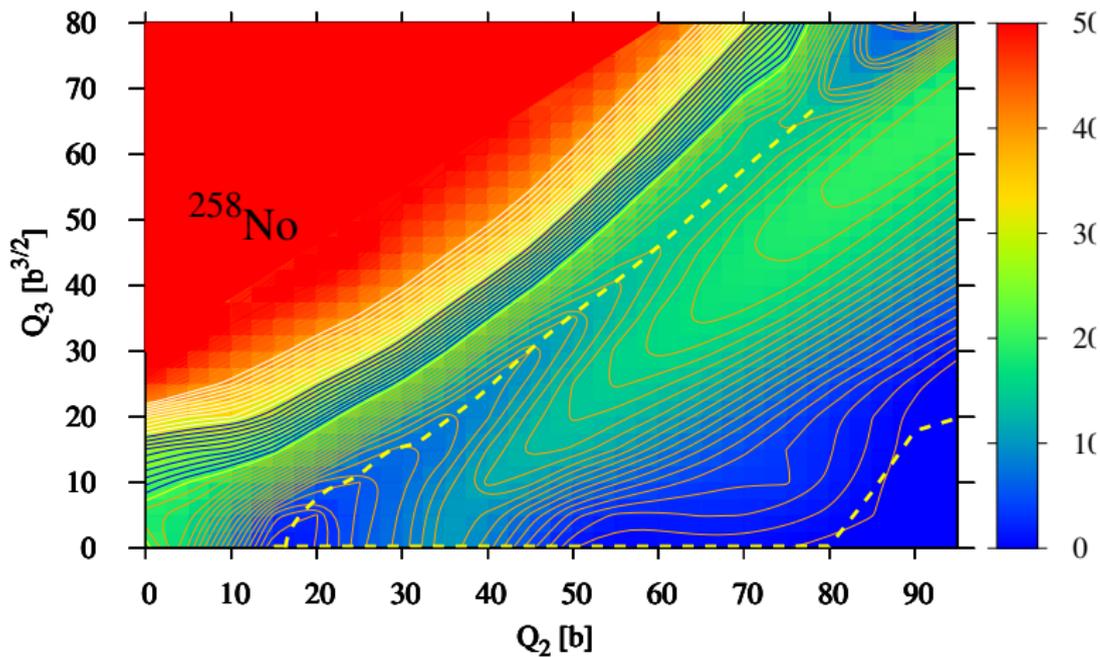


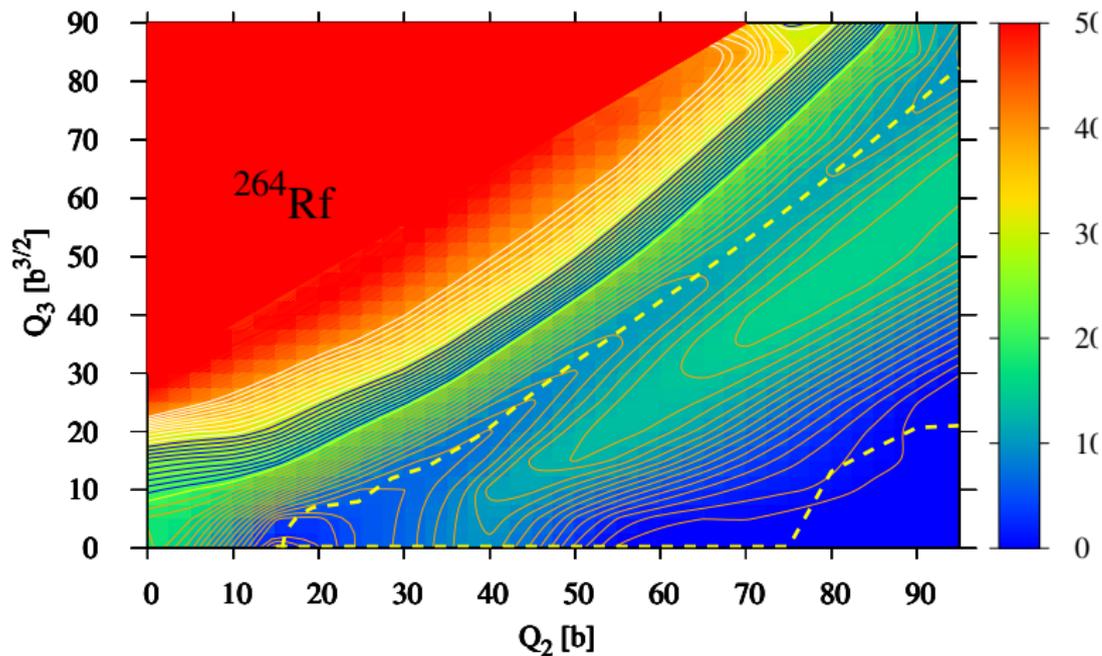


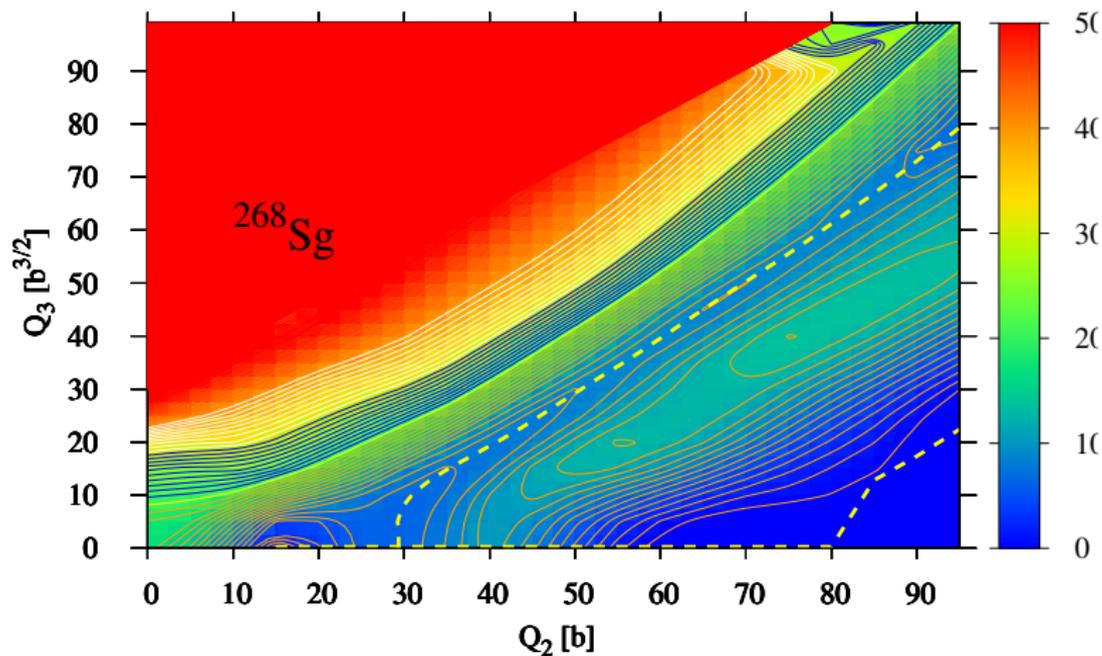


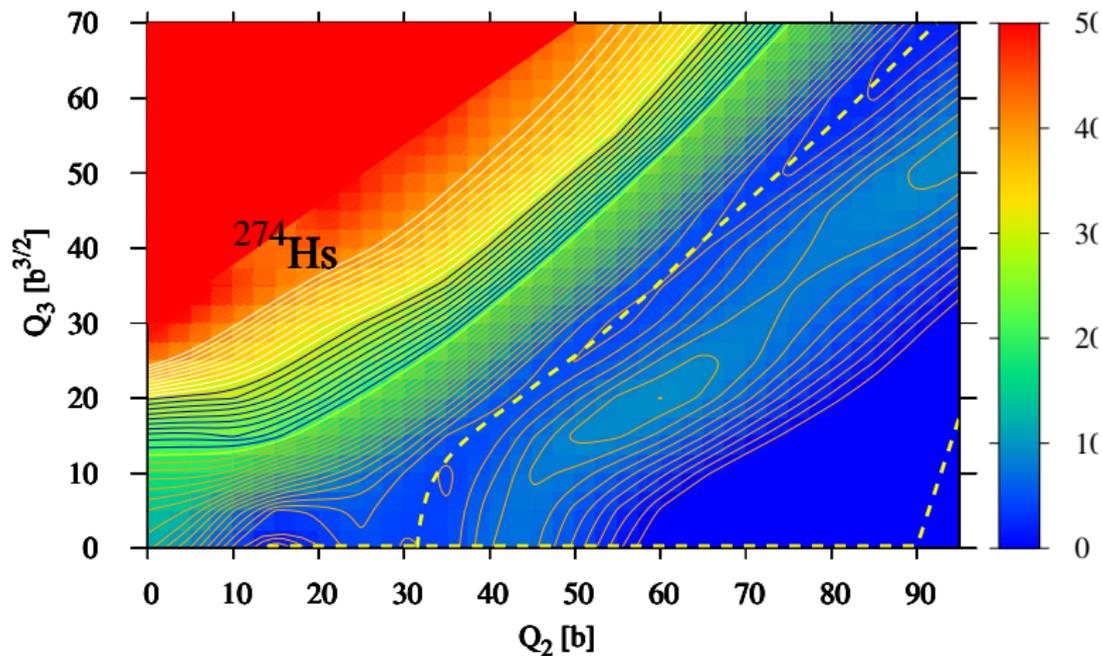


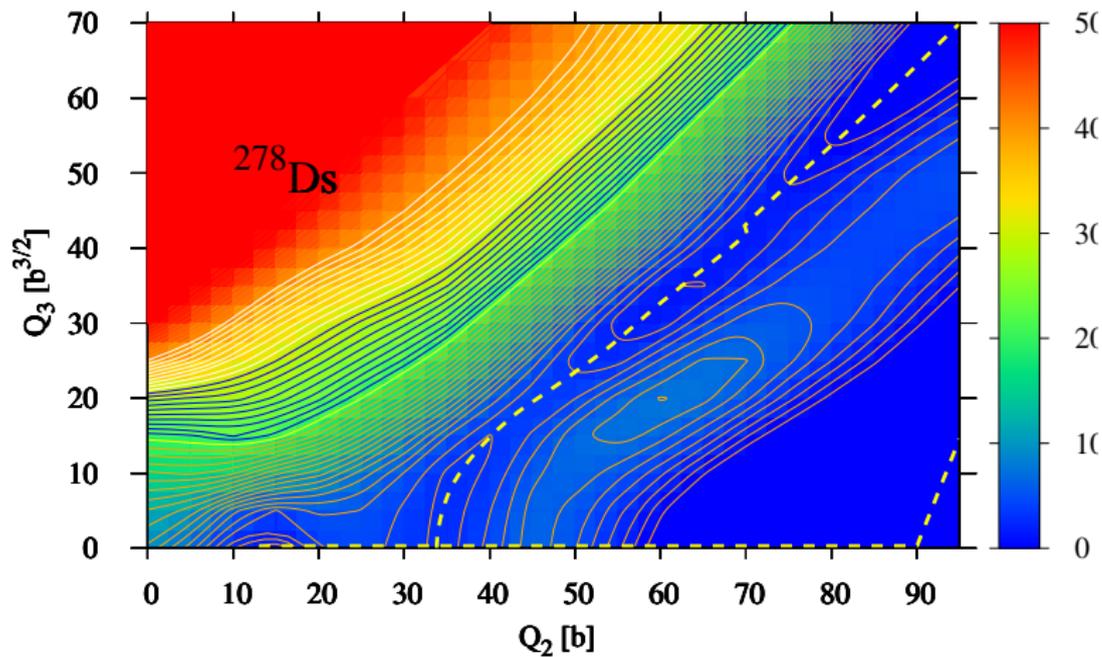


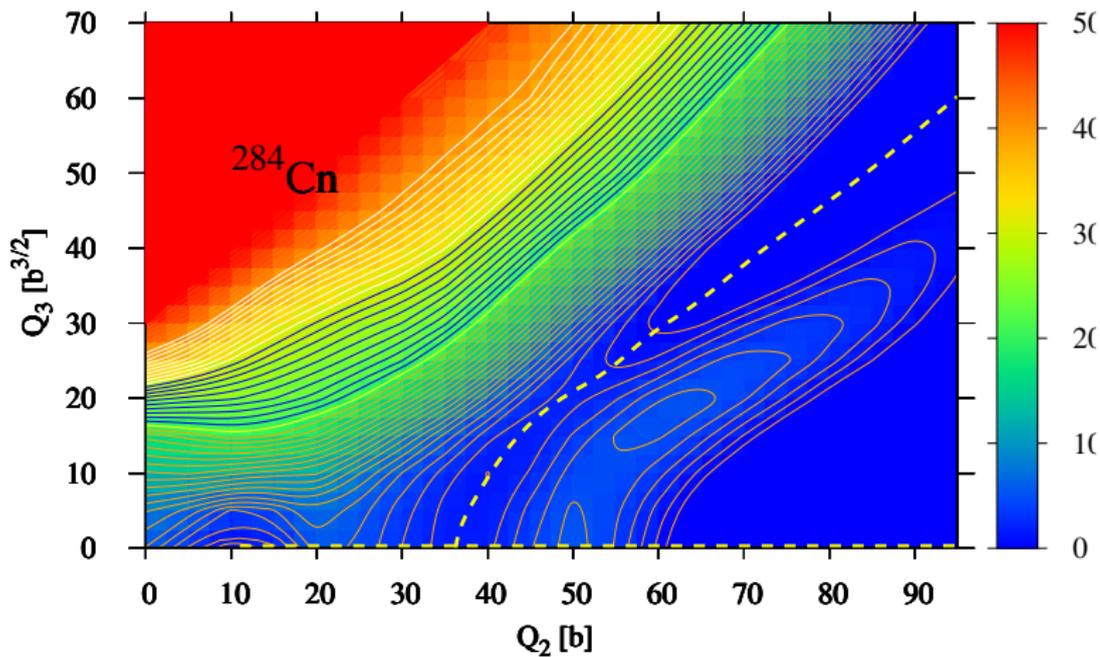


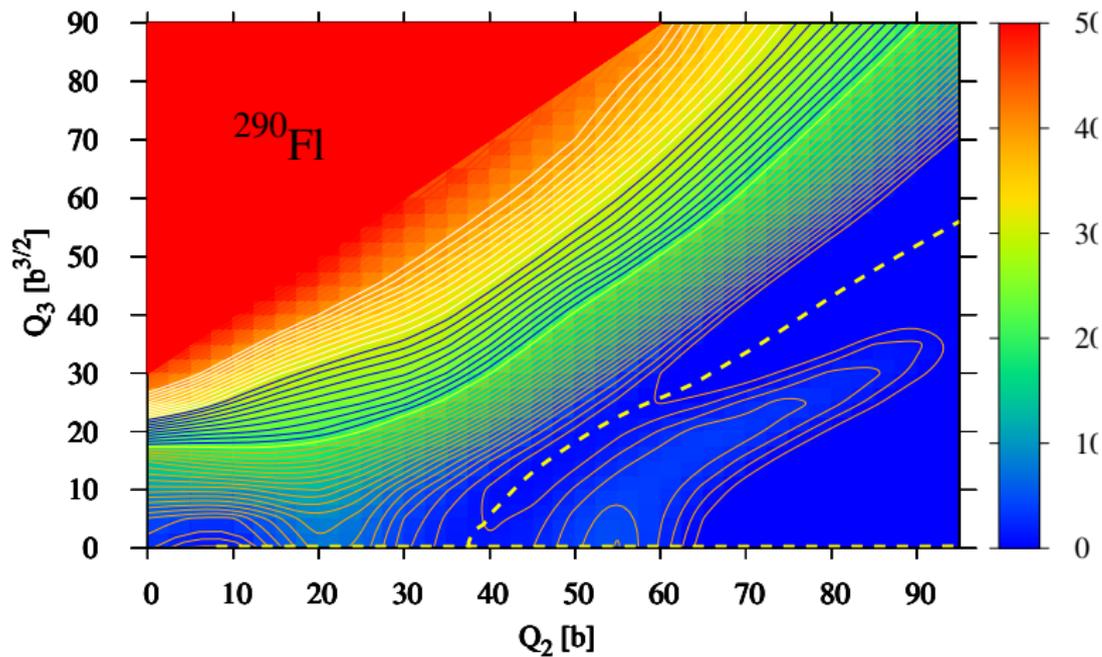


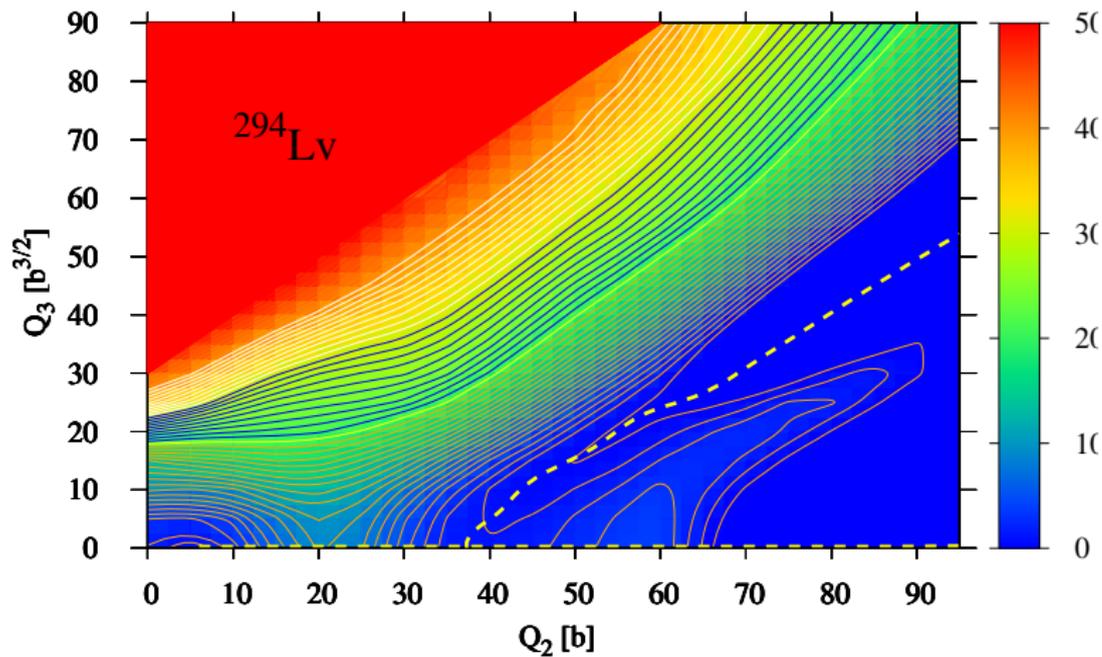


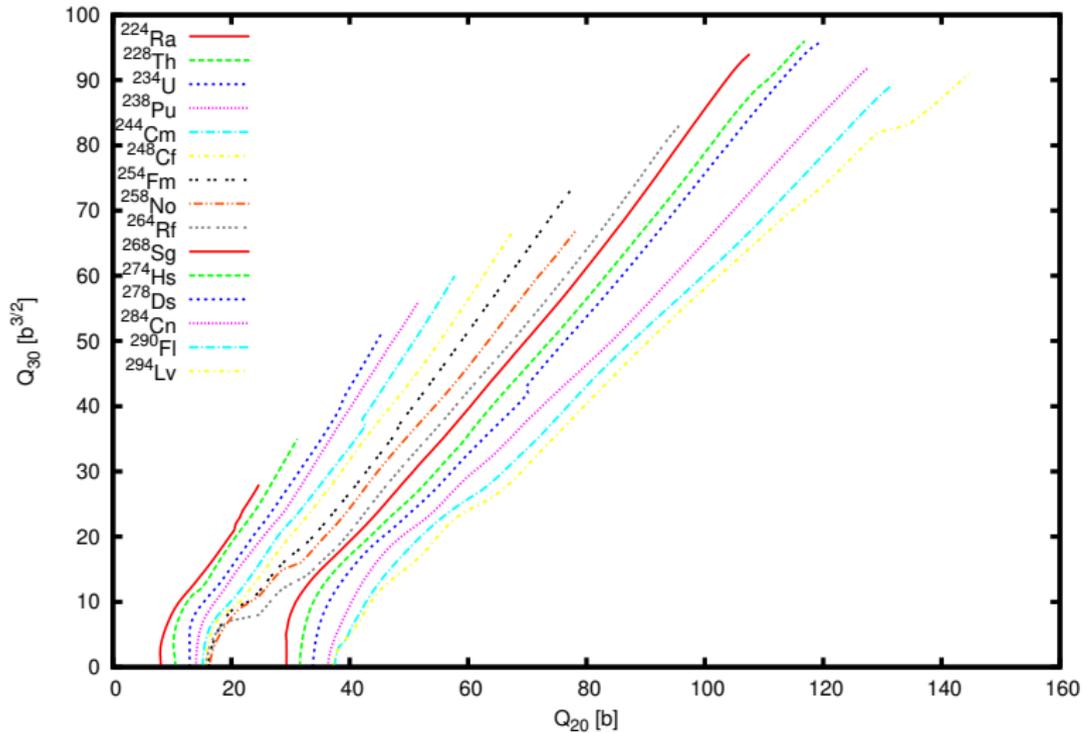


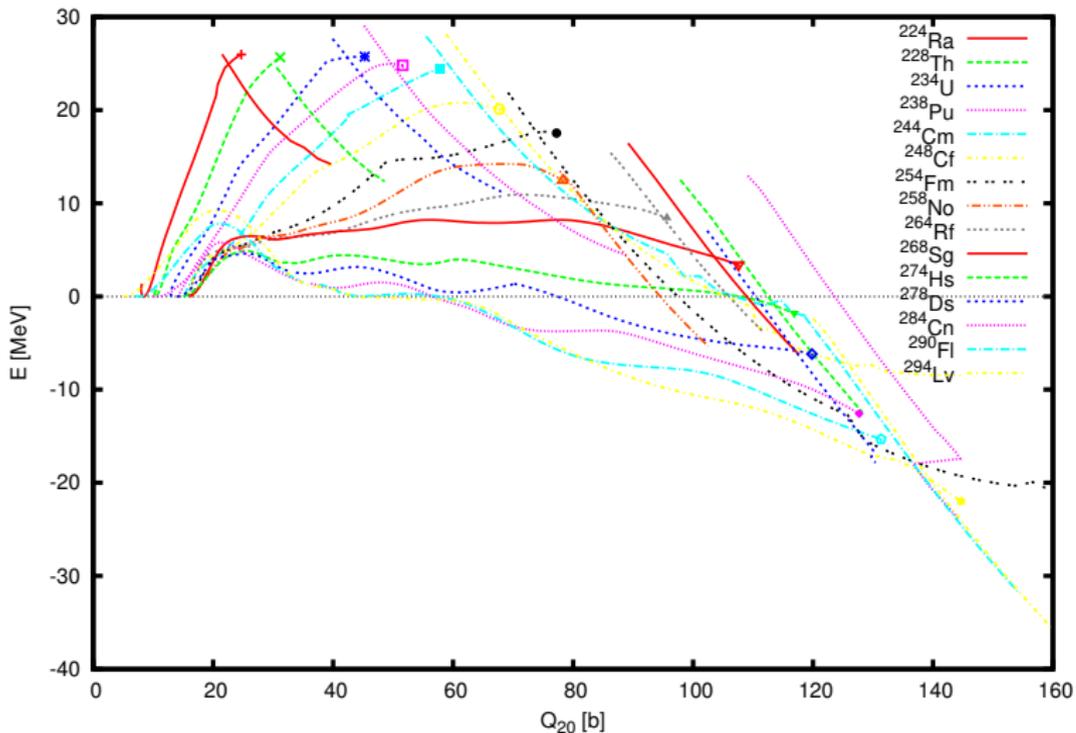


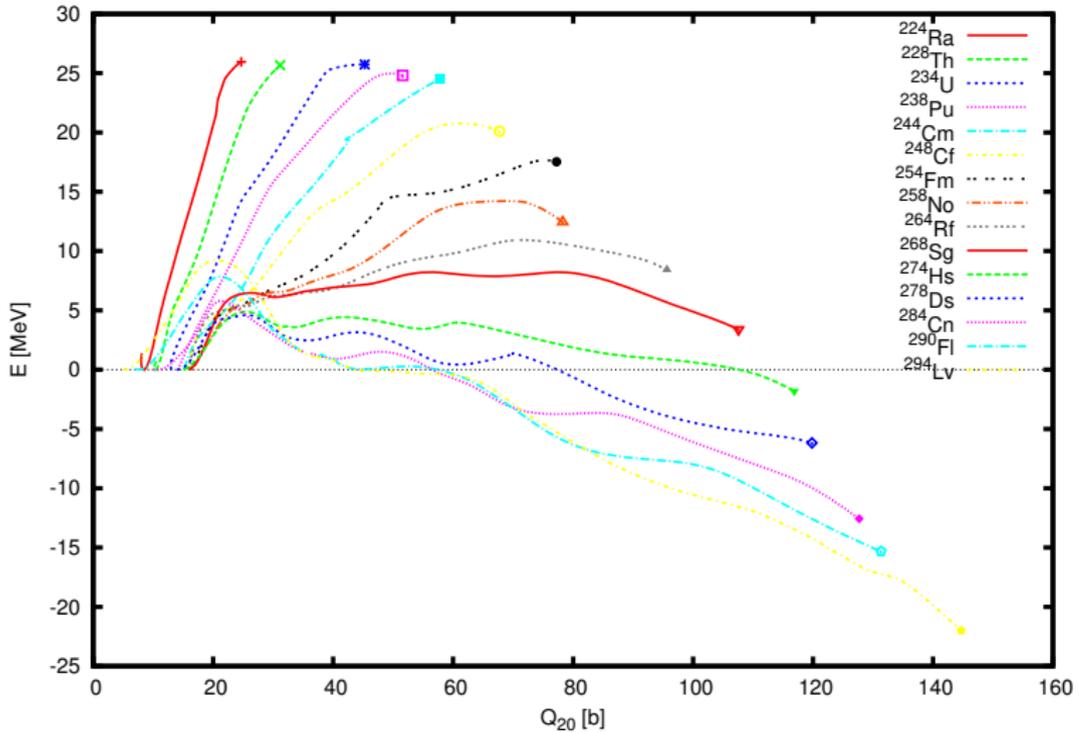




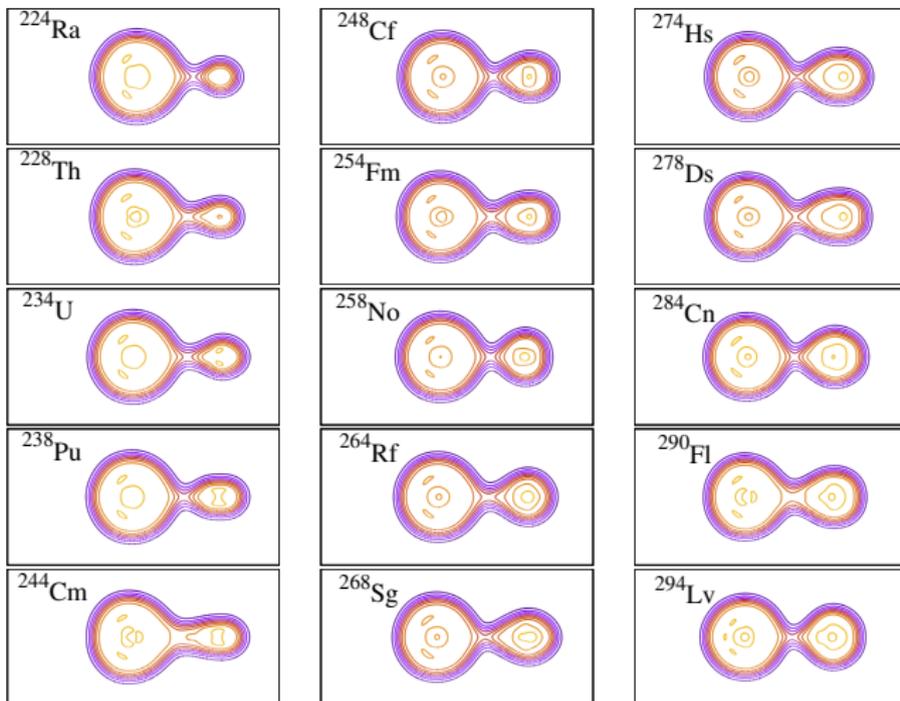




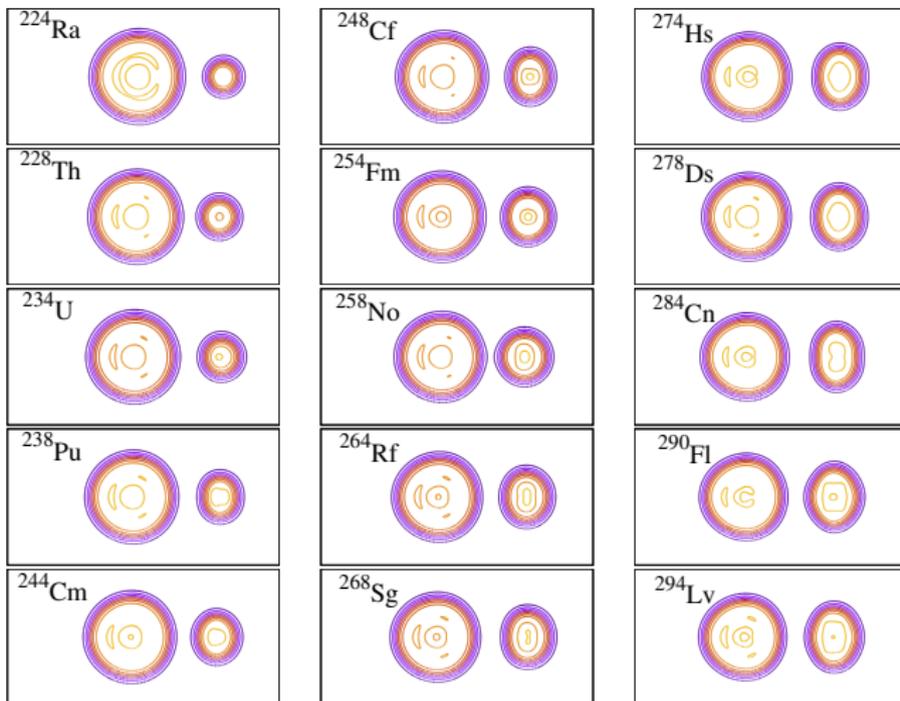


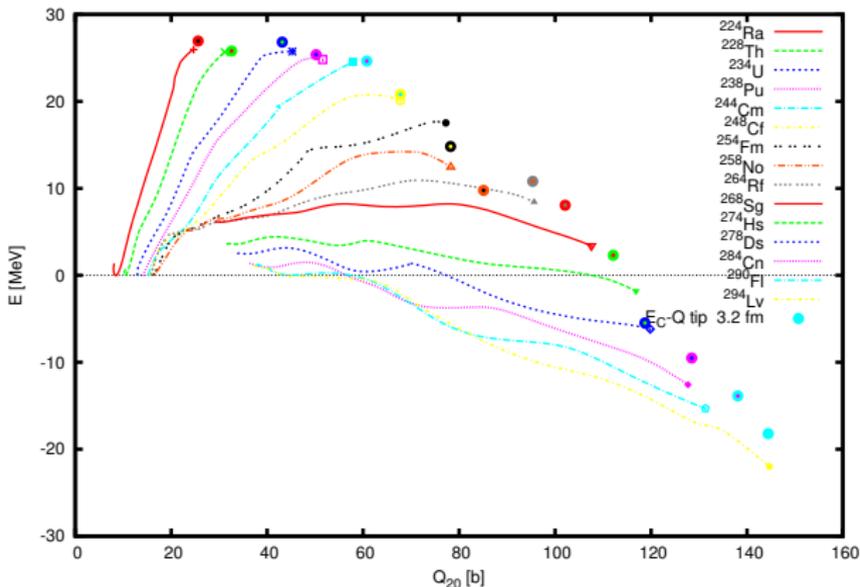


# Pre-scission shapes

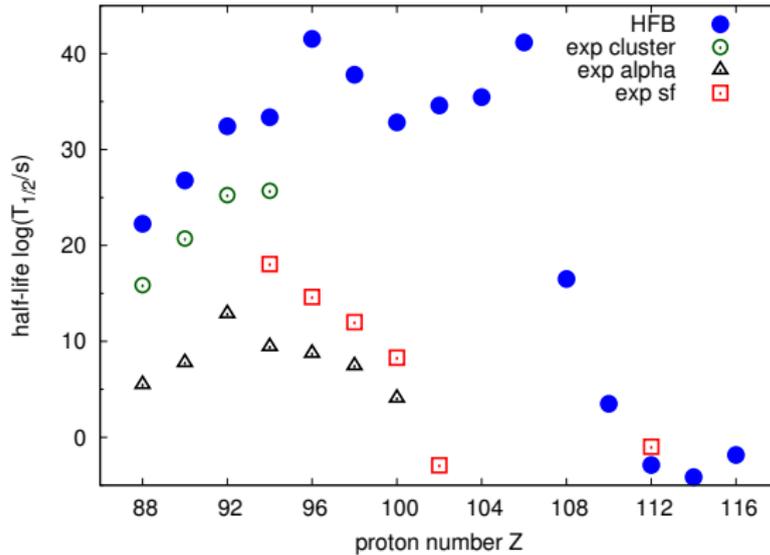


# Post-scission shapes





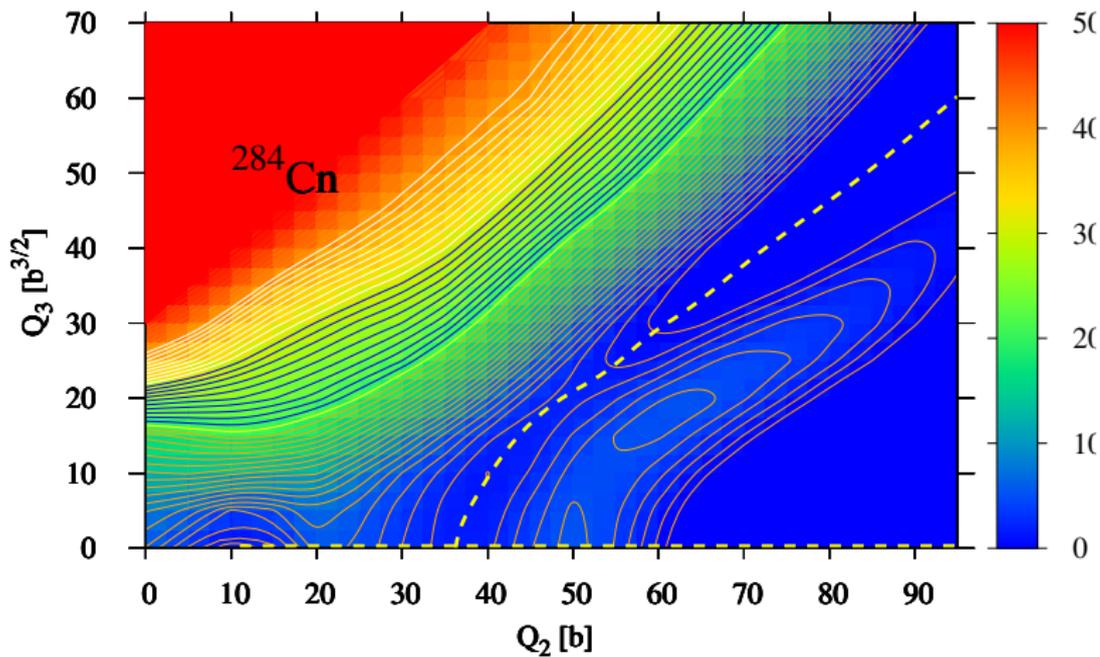
$$E = k \frac{82(Z - 82)e^2}{r_{208} + r_{A-208} + d} - Q$$

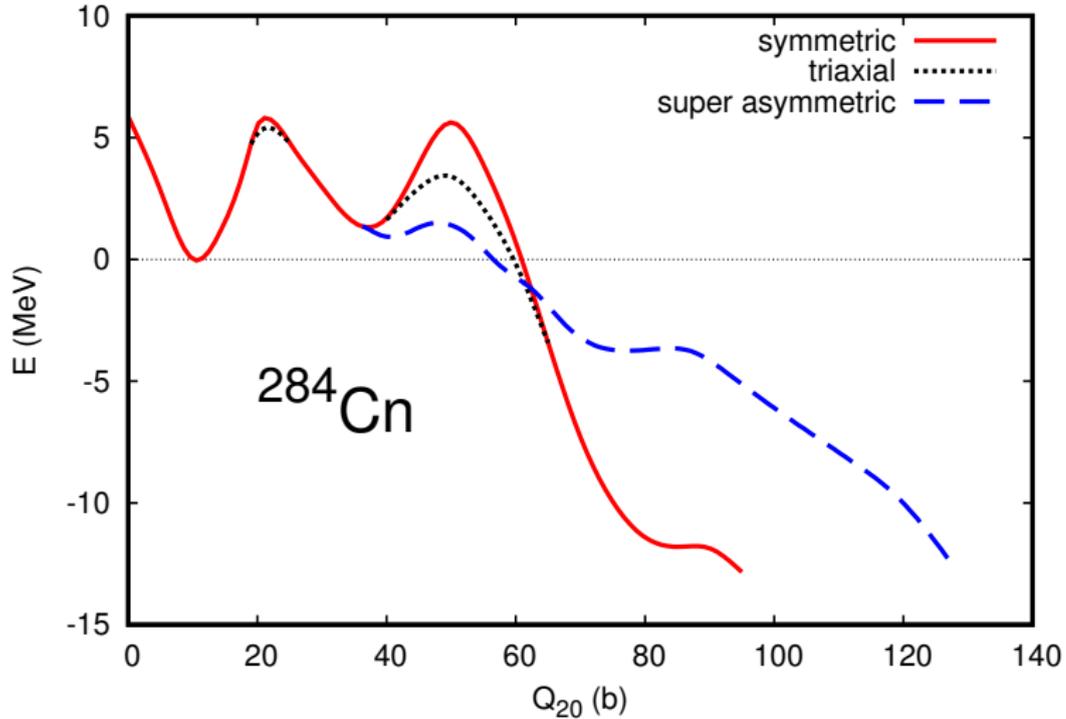


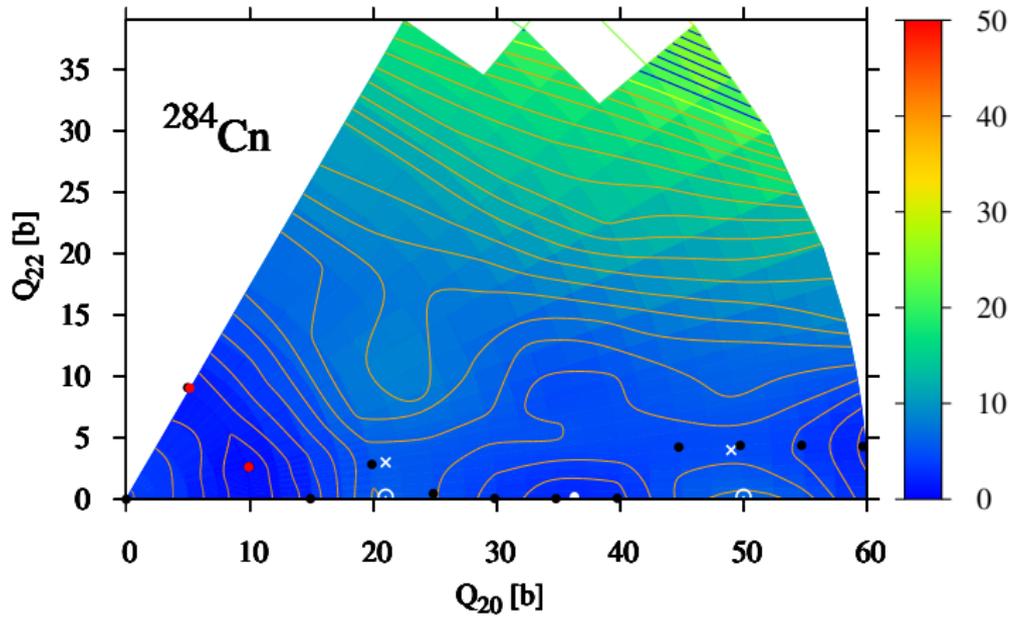
## Experimental evidence in $^{284}\text{Cn}$ :

- GSI: 9 events  
Ch. Düllmann, et al., Phys.Rev.Lett. 104, 252701 (2010)
- Dubna: 19 events  
Yu. Oganessian, Radiochim.Acta 99, 429 (2011)
- lifetimes: 30 ms - 400 ms

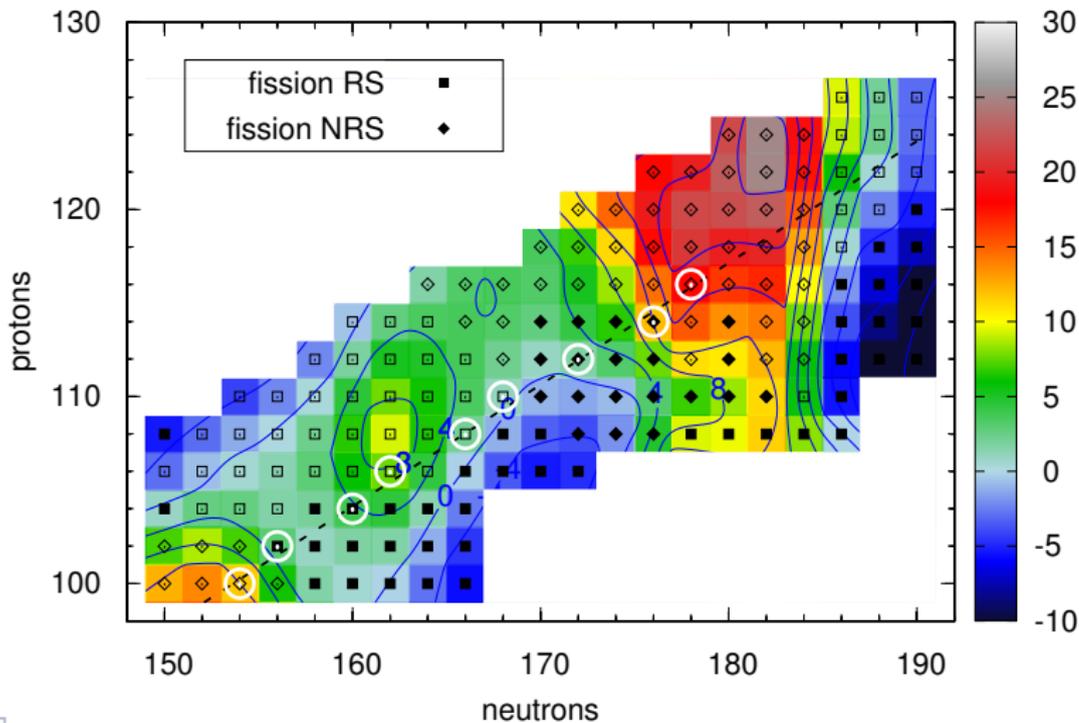


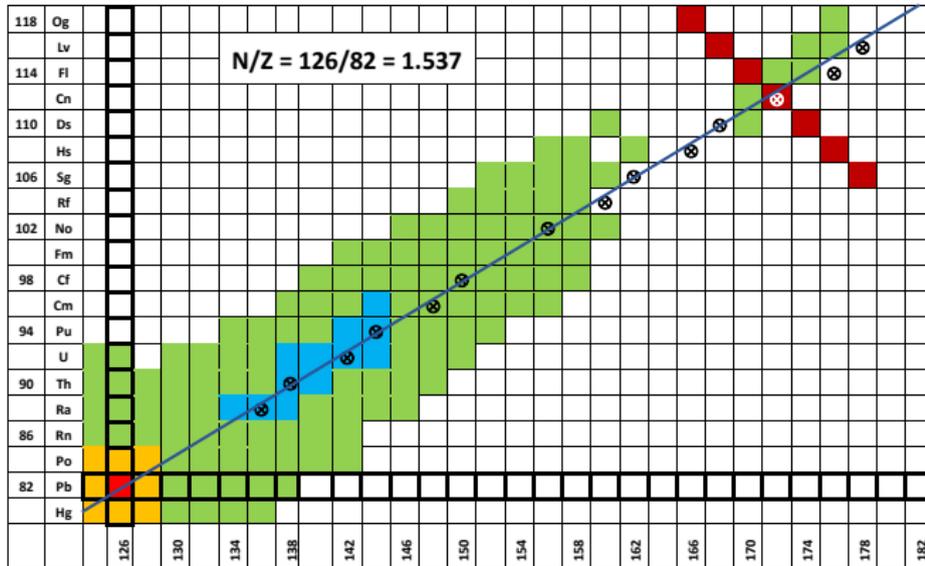


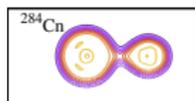
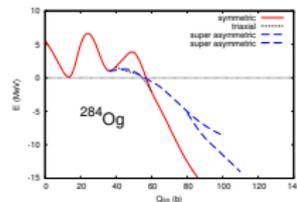
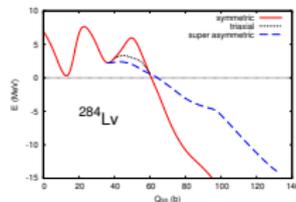
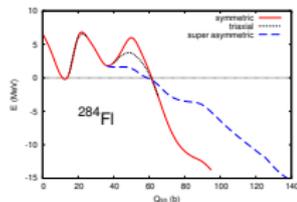
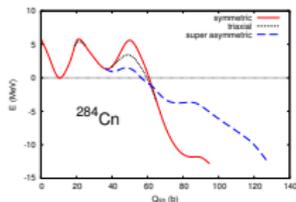
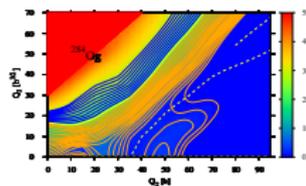
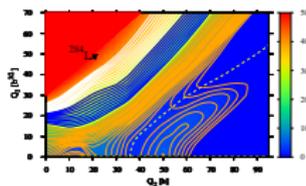
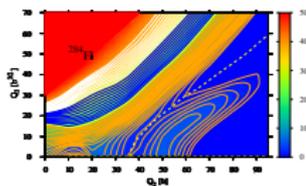
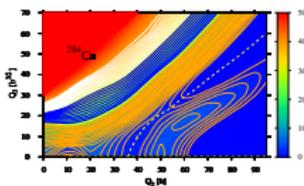




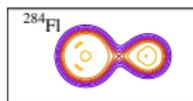
# Chart of SH nuclides



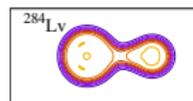




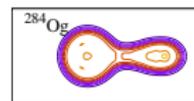
$Z_H = 82$   
 $N_H = 126$   
 $N/Z = 1.535$   
 $N_H/Z_H = 1.537$



$Z_H = 82$   
 $N_H = 124$   
 $N/Z = 1.491,$   
 $N_H/Z_H = 1.512$

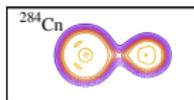
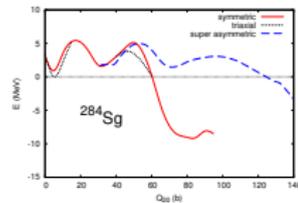
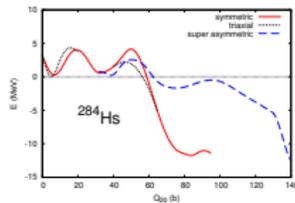
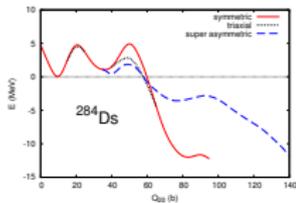
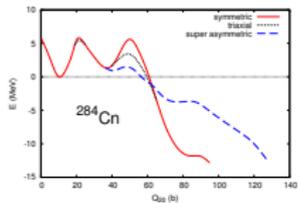
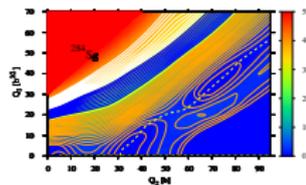
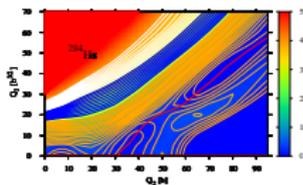
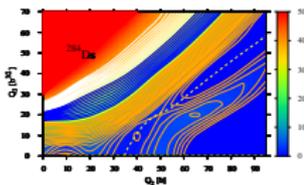
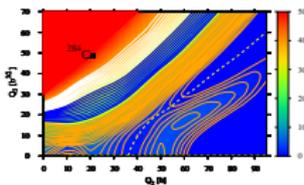


$Z_H = 83$   
 $N_H = 122$   
 $N/Z = 1.448$   
 $N_H/Z_H = 1.470$

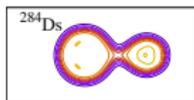


$Z_H = 86$   
 $N_H = 123$   
 $N/Z = 1.407$   
 $N_H/Z_H = 1.430$

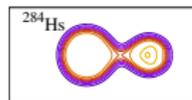




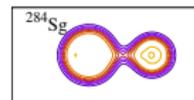
$Z_H = 82$   
 $N_H = 126$   
 $N/Z = 1.535$   
 $N_H/Z_H = 1.537$



$Z_H = 80$   
 $N_H = 126$   
 $N/Z = 1.581$   
 $N_H/Z_H = 1.575$



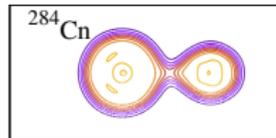
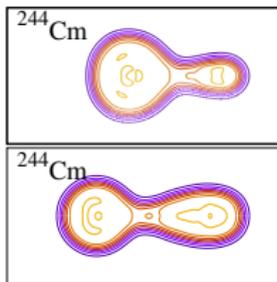
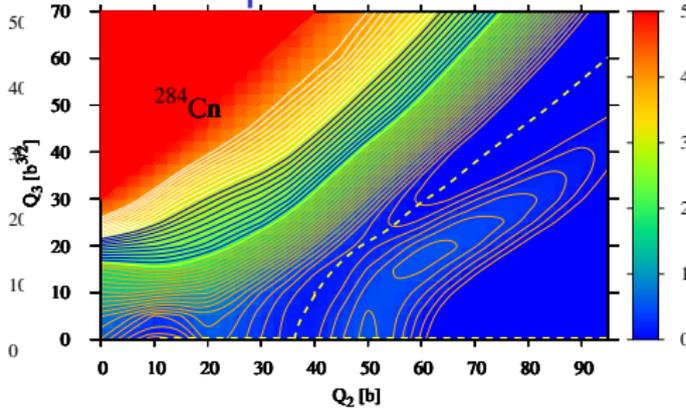
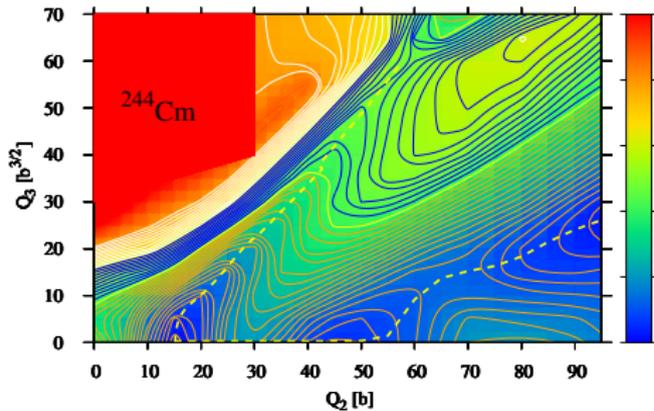
$Z_H = 78$   
 $N_H = 127$   
 $N/Z = 1.630$   
 $N_H/Z_H = 1.628$

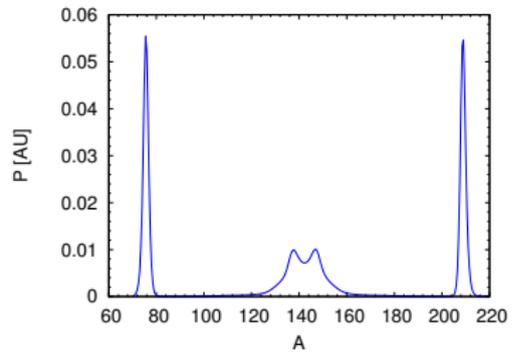
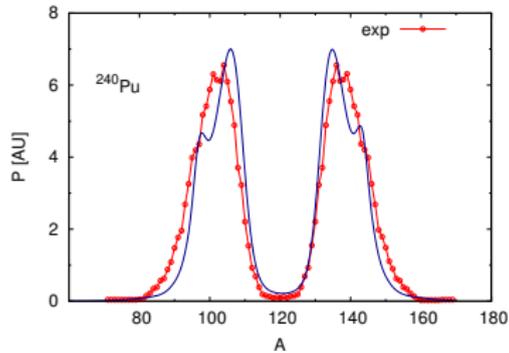


$Z_H = 75$   
 $N_H = 127$   
 $N/Z = 1.679$   
 $N_H/Z_H = 1.693$



# Actinides and superheavies





- Asymmetric fission in super heavy nuclei region has the same nature as cluster radioactivity in actinides
- This decay may be dominant in some super heavy nuclei
- Sharp fragment mass distribution with  $^{208}\text{Pb}$  fragment is predicted

M. Warda, A. Zdeb, L.M. Robledo  
*Cluster Radioactivity in Super Heavy Nuclei*  
Phys. Rev. **C 98** 041602(R) (2018)

