Study of ⁴⁰S by Gogny-TDHFB method

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1. Motivation

2. Basic equations

3. (1) Pairing energy with respect to separation Rz in CHFB/TDHFB

(2) Single-particle energy and occupation weights

4. Summary

²⁰O + ²⁰O head-on collision by Gogny-TDHFB



Cf. Y. H and Guillaume Scamps, Phys. Rev. C 94, 014610 (2016)





transferred neutron number vs relative gauge angle

45

135

20

22

0,90





probability $P_L(N_I)$ of finding N_L neutrons in the left nucleus after the closest approach

16

Relative distance R (fm)

14

18

 $^{20}O + ^{20}O$

10

 10^{-1}

 10^{-2}

 10^{-4}

12

 $^{20}O + ^{20}O$ head-on collision





1. smooth decrease of the pairing energy

2. damped oscillation



2. Basic equation

cf. Ring & Schuck, The Nuclear Many-Body Problems

Bogoliubov trans. :
$$\begin{cases} \beta_k^{\dagger} = \sum_{\alpha} (U_{\alpha k} C_{\alpha}^{\dagger} + V_{\alpha k} C_{\alpha}), \\ \beta_k = \sum_{\alpha} (U_{\alpha k}^* C_{\alpha} + V_{\alpha k}^* C_{\alpha}^{\dagger}). \end{cases}$$
$$i\hbar \frac{\partial}{\partial t} \begin{pmatrix} U(t) \\ V(t) \end{pmatrix} = \mathcal{H} \begin{pmatrix} U(t) \\ V(t) \end{pmatrix} \qquad \mathcal{H} = \begin{pmatrix} h & \Delta \\ -\Delta^* & -h^* \end{pmatrix}.$$
$$h_{\alpha \beta} = T_{\alpha \beta} + \Gamma_{\alpha \beta}, \\ \Gamma_{\alpha \beta} = \sum_{\nu^{\delta}} \mathcal{V}_{\alpha \gamma \beta \delta} \rho_{\delta \gamma}, \quad \Delta_{\alpha \beta} = \frac{1}{2} \sum_{\nu} \mathcal{V}_{\alpha \beta \gamma \delta} \kappa_{\gamma \delta}, \\ \rho_{\alpha \beta} = (V^* V^T)_{\alpha \beta}, \quad \kappa_{\alpha \beta} = (V^* U^T)_{\alpha \beta}. \end{cases}$$

predictor-corrector method

$$\begin{pmatrix} U(t) \\ V(t) \end{pmatrix}^{(n+1)} = \exp\left(-i\frac{c\Delta t}{c\hbar}\mathcal{H}^{(n+\frac{1}{2})}\right) \begin{pmatrix} U(t) \\ V(t) \end{pmatrix}^{(n)}$$

harmonic oscillator	Lagrange mesh
х, у	Z

$$X$$

 Y
 Y

$$\{ \phi_{n_x}(x), \phi_{n_y}(y), \phi_{n_z}(z) \} \longrightarrow \{ \phi_{n_x}(x), \phi_{n_y}(y), \underline{f_{n_z}(z)} \}$$
 harmonic oscillator Lagrange mes

$$\begin{split} f_l(z) &= \frac{1}{N} \frac{\sin\left(\pi\left(z-z_l\right)/h\right)}{\sin\left(\pi\left(z-z_l\right)/L\right)} & f_k(z_{k'}) = \delta_{kk'} \\ L &= Nh & \int_{-L/2}^{L/2} f_l(z) f_{l'}(z) dz = h \, \delta_{ll'} \\ \\ \text{D. Baye and P. Heenen,} & \int_{-L/2}^{L/2} f_l(z) W(z) f_{l'}(z) dz = h \, W(z_l) \, \delta_{ll'} \end{split}$$

HFB calculations with constraint term $\propto |z|$



3-1. Pairing energy vs Rz

 $^{20}O + ^{20}O$ head-on collision

smooth change of pairing energy with respect to separation Rz



3-2. TDHFB trajectories, total energy and pairing energies



3-2. TDHFB trajectories, total energy and pairing energies



\bigstar TDHFB trajectory (initial Rz = 9.3 fm)



\Rightarrow TDHFB trajectory (initial Rz = 5.7 fm)

pairing energy (TDHFB from Rz = 5.7 fm)



3-3. TDHFB trajectories and single-particle energies



magnifications



typical trajectories



2.4 Comparison of canonical weights between CHFB and TDHFB







4. Summary

1. smooth change of pairing energy

<==> change of distribution of the neutron single-particle energies and smooth change of occupation weights

2. damped oscillations

<==> (comparatively) large change of distributions of neutron occupation weights near chemical potential energy

3. More quantitative method of analysis?

Thanks for listening!