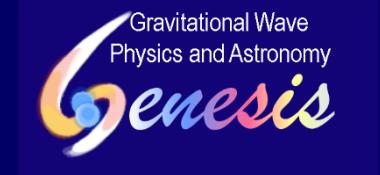


Nuclear Physics Uncertainties in Core–Collapse Supernovae

Shun Furusawa(RIKEN, iTHEMS)

We have to improve
nuclear excitations (level densities) and
electron captures (strength distributions)
for nuclei with $(N,Z) \approx (50,30)$
(SF PRC 98.065802('18), SF+ PRC 95.025809 ('17b)).

H. Togashi (RIKEN), J. Holt (TEXAS A&M), I. Mishustin (FIAS),
H. Nagakura (Princeton), K. Sumiyoshi (Numazu),
S. Yamada (Waseda), H. Suzuki, K. Saito (Tokyo U. of Sci.)

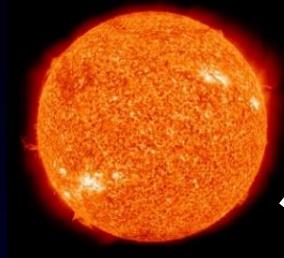


Evolutions of Stellar objects

Stellar formation



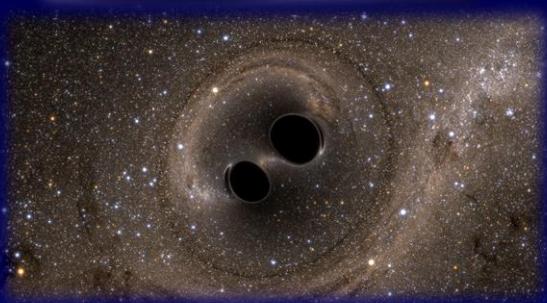
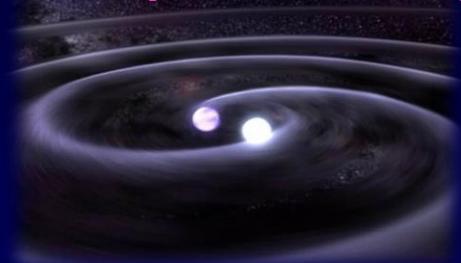
Stars



White Dwarf
→Thermonuclear
(Type Ia) Supernovae



Compact Star mergers



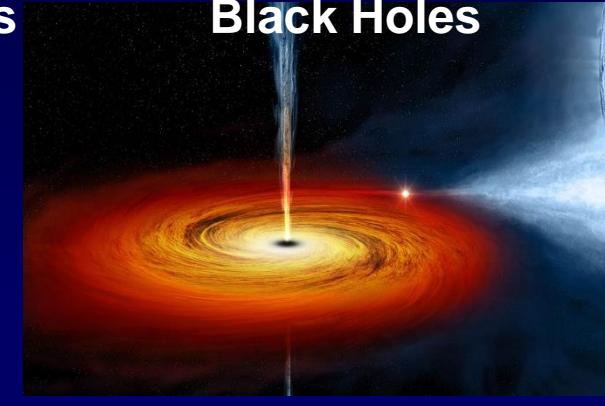
Core-Collapse
Supernovae
(CCSNe)



Neutron Stars



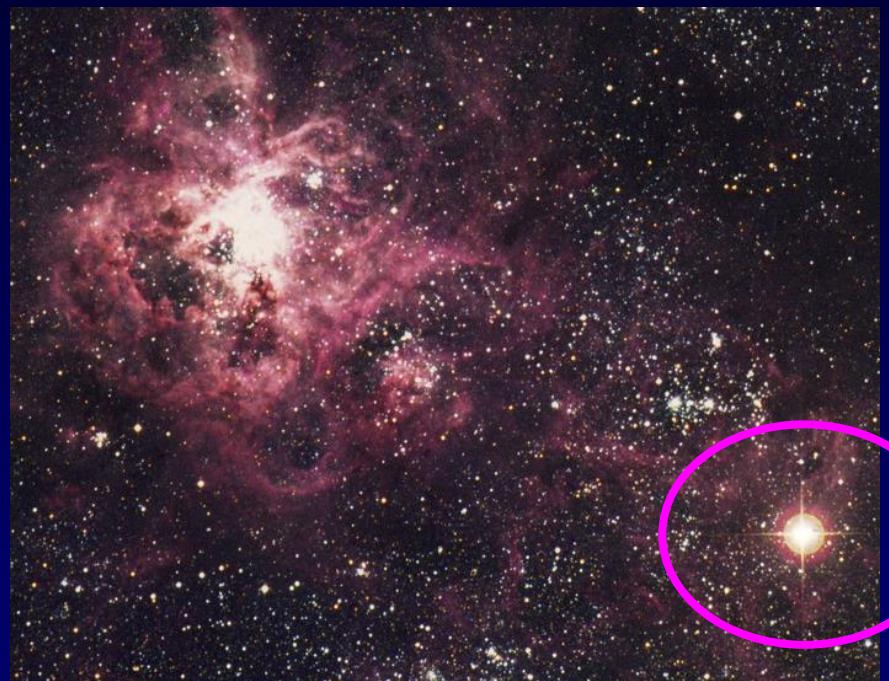
Black Holes



Core-Collapse Supernovae

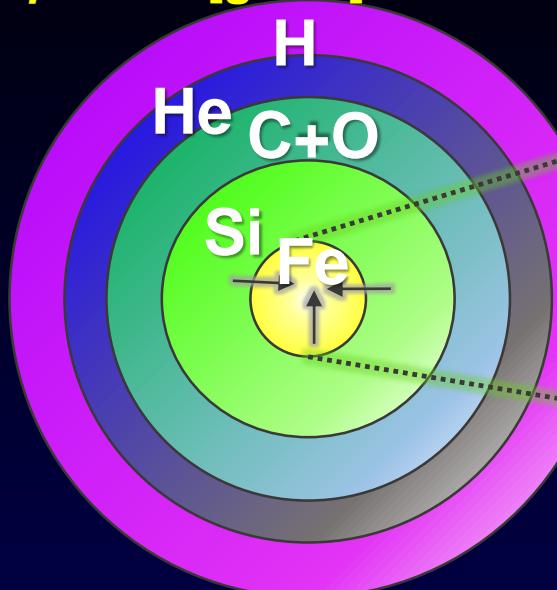
- Energetic events 10^{51} erg (ejecta), 10^{53} erg (neutrino)
- Emissions of **neutrinos** and **gravitational Waves**
- Formations of a **neutron star** or a **black hole**
- Nucleosynthesis site of **heavy elements**
- Extreme test for nuclear physics

SN 1987A

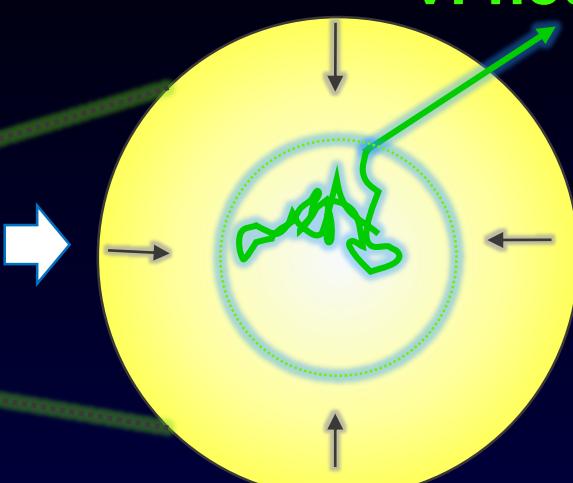


Core-Collapse Supernovae

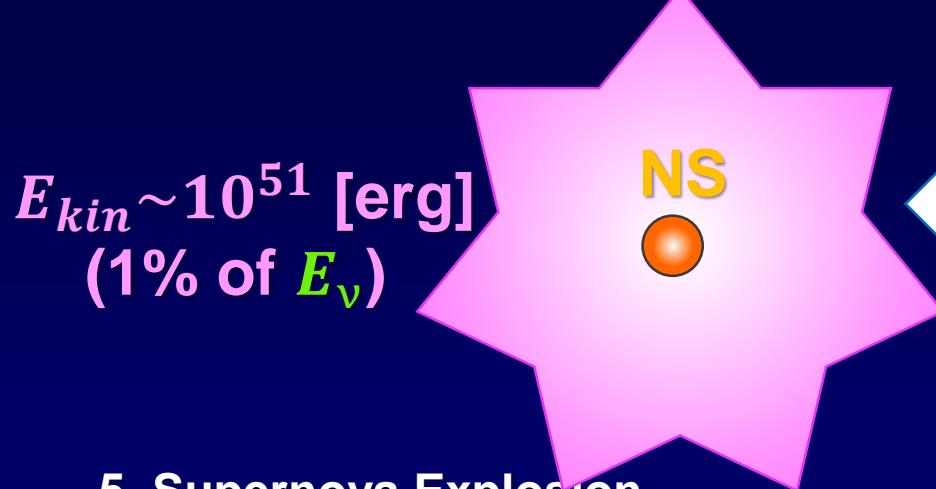
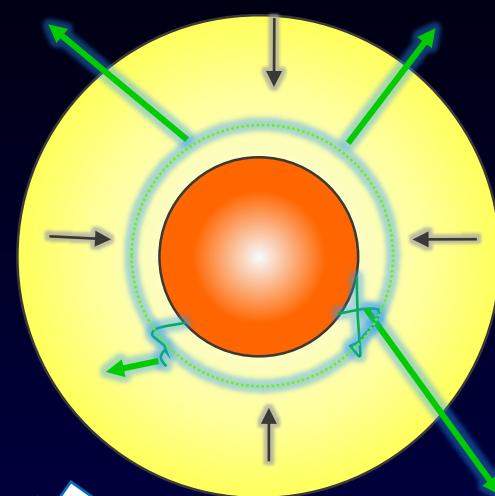
1, Core collapse
 $\rho \sim 10^{10} \text{ [g/cm}^3\text{]}$



2, Neutrino trapping
 $\rho \sim 10^{12} \text{ [g/cm}^3\text{]}$



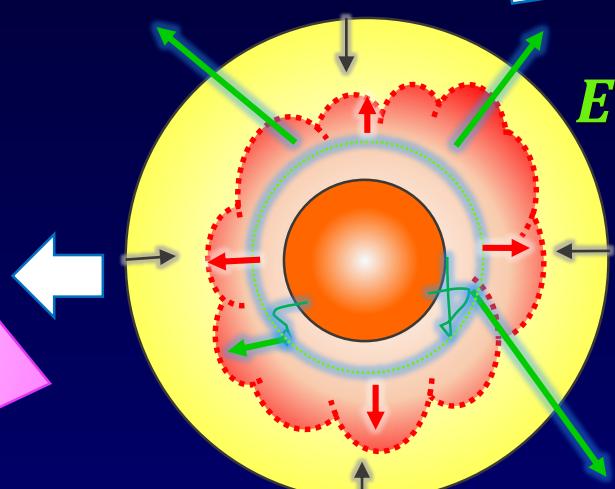
3, Core bounce
 $\rho \sim 10^{14} \text{ [g/cm}^3\text{]}$



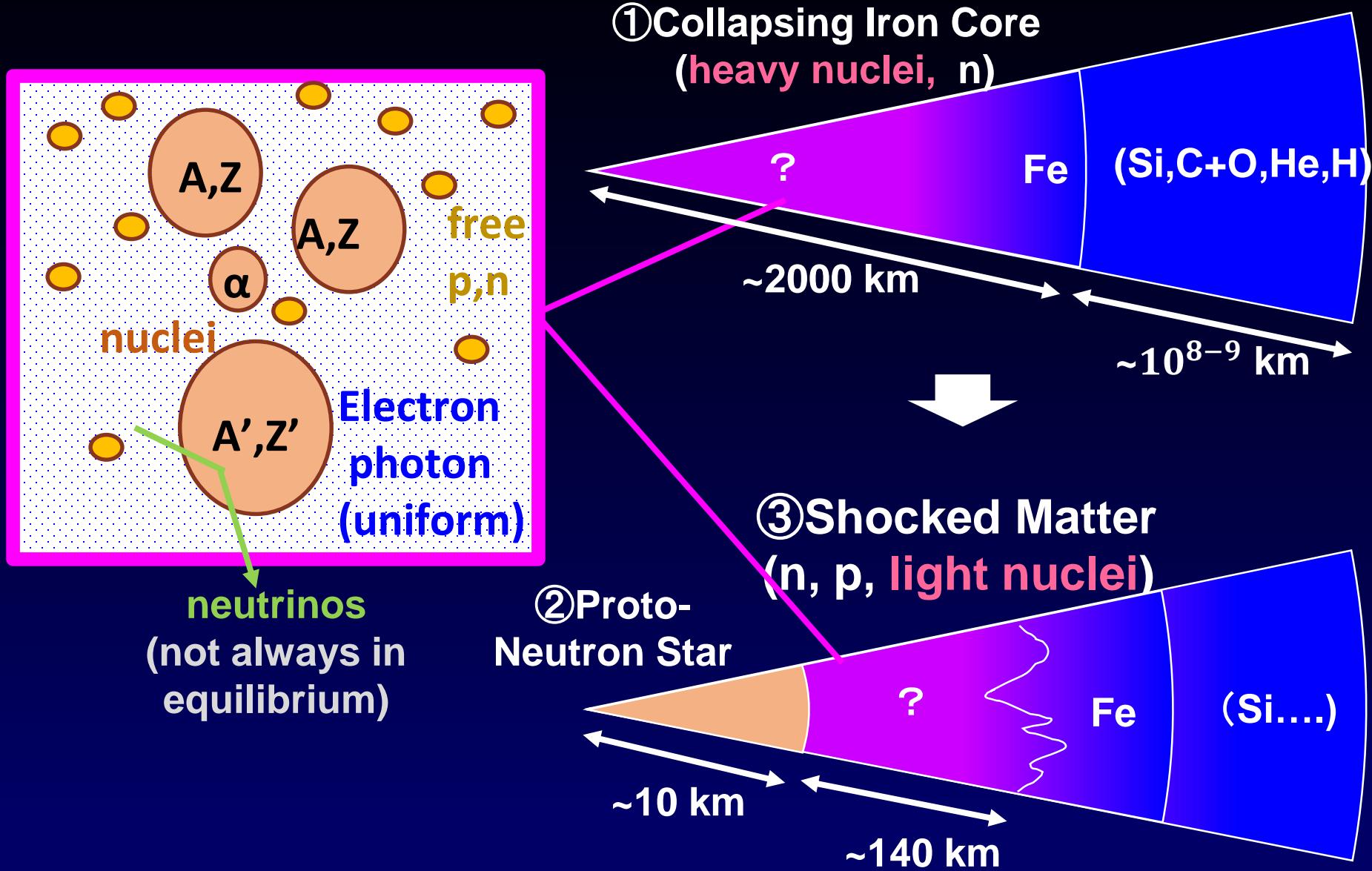
5, Supernova Explosion

4, Shock Propagation in Core

$E_\nu \sim 10^{53} \text{ [erg]}$

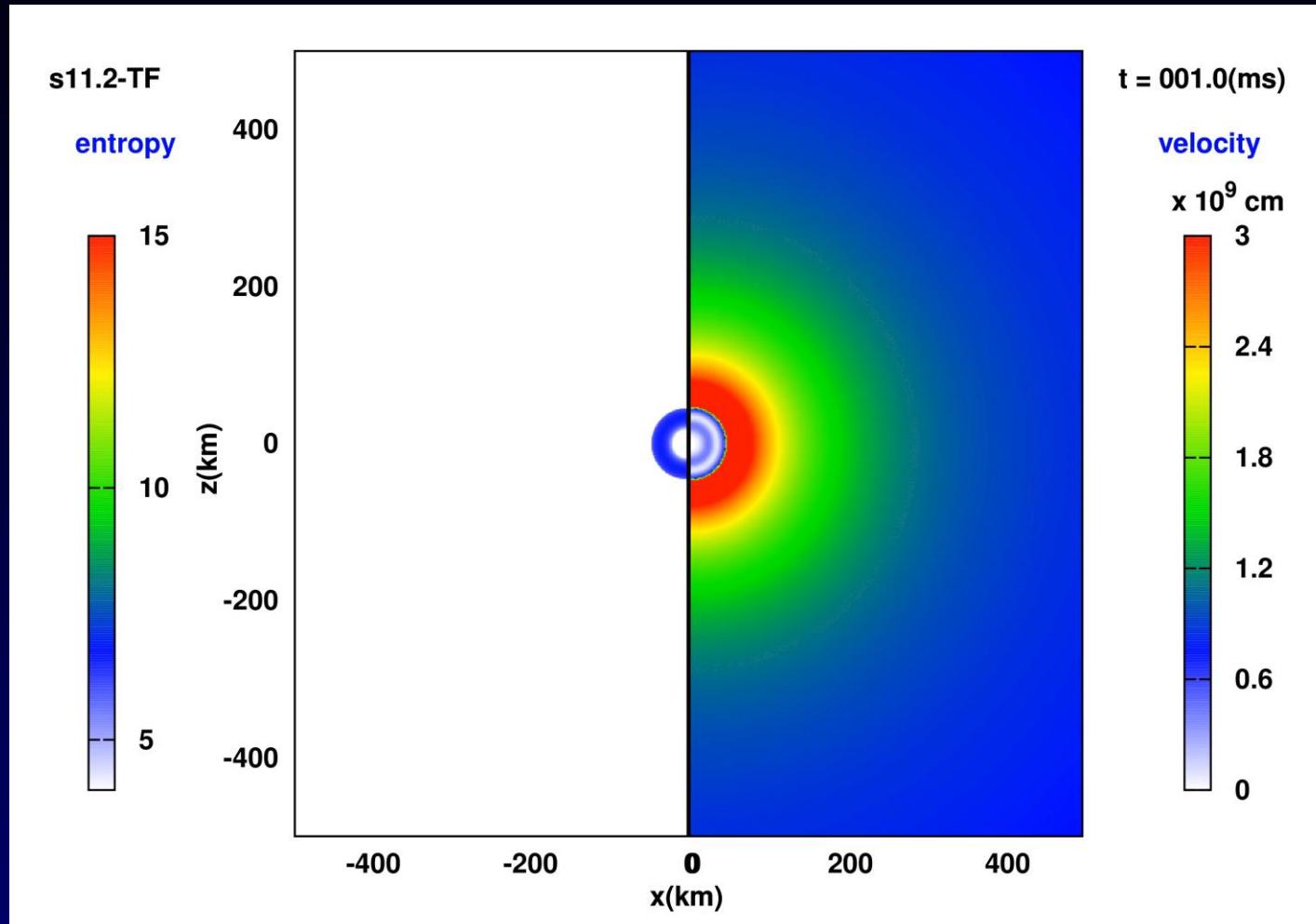


Supernova matter in Core-Collapse Supernovae



Supernova Simulations

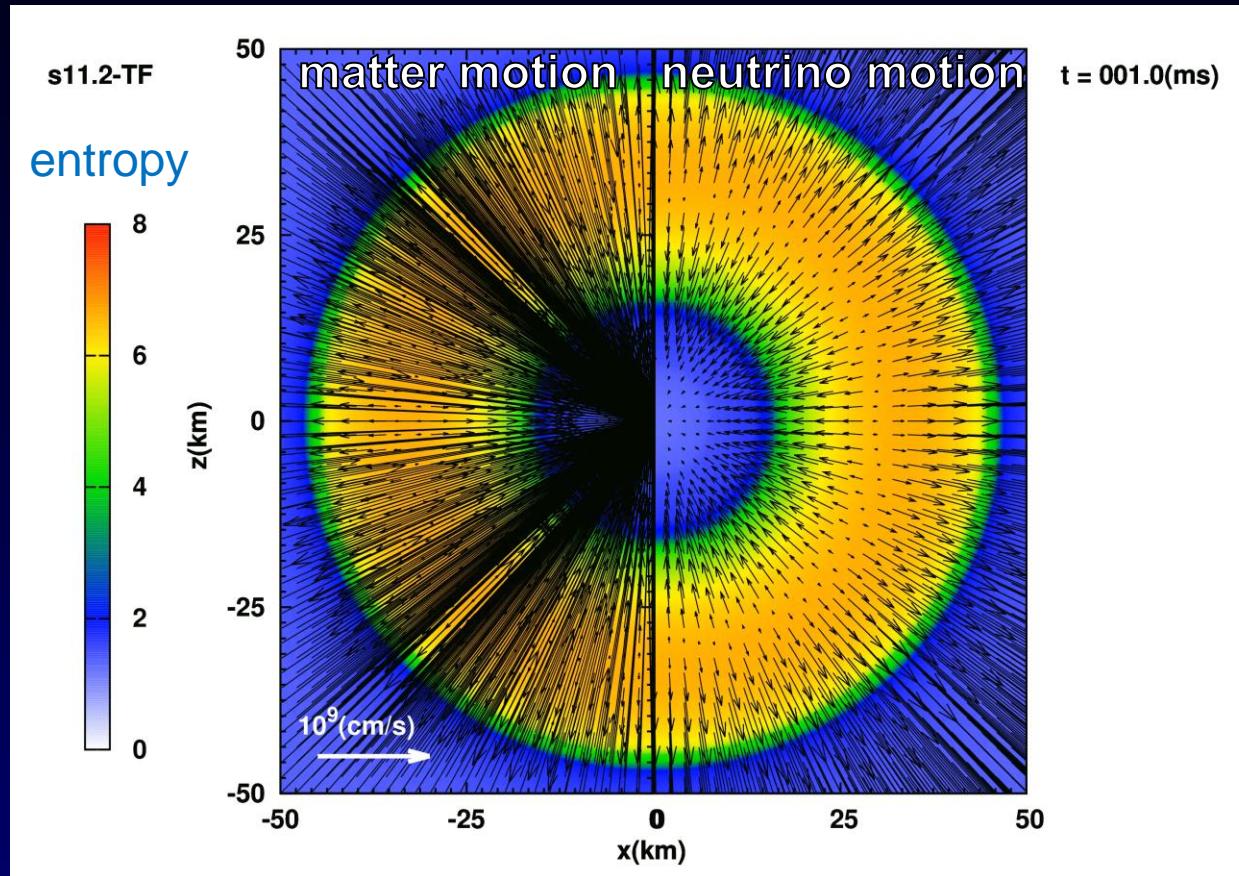
- ① Hydrodynamics of matter in 3D space
- ② Neutrino transport in 3D space \times 3D momentum space



2D (axisymmetric) simulation(Nagakura+) at Supercomputer K
based on Togashi-Furusawa EOS (SF+17d)

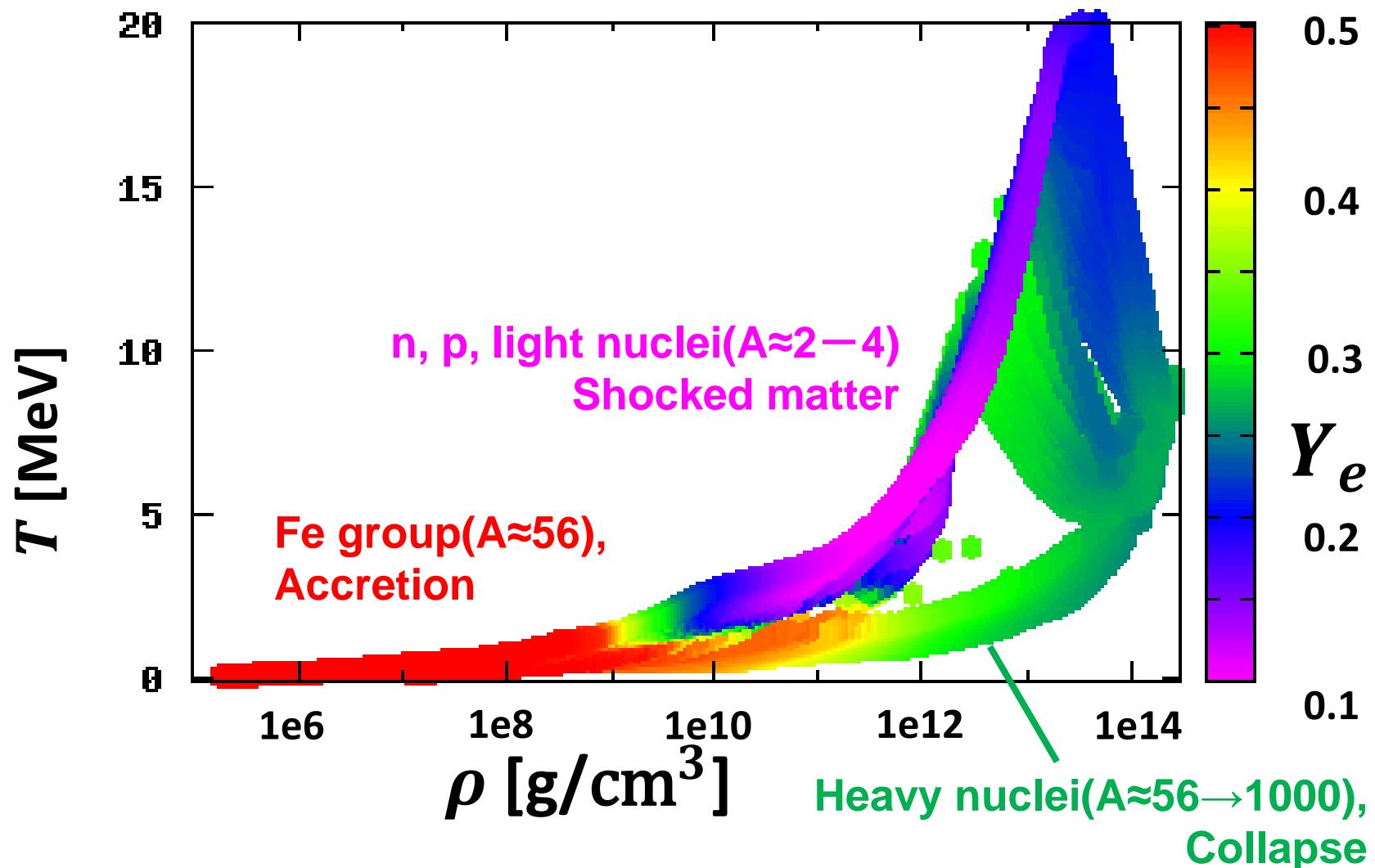
Inputs of Supernova Simulations

- ①Equation of State \Rightarrow Stiffness, Nuclear compositions (Which nuclei appear)
- ②Weak interaction rates \Rightarrow Neutrino emissions, absorptions, and scattering
Ex. $(N, Z) + e^- \leftrightarrow (N + 1, Z - 1) + \nu_e$



Motions of neutrinos and matter around Proto-Neutron Star
(Nagakura+) Togashi-Furusawa EOS (SF+17d)

(ρ, T, Y_e) in Core-Collapse Supernova Simulations

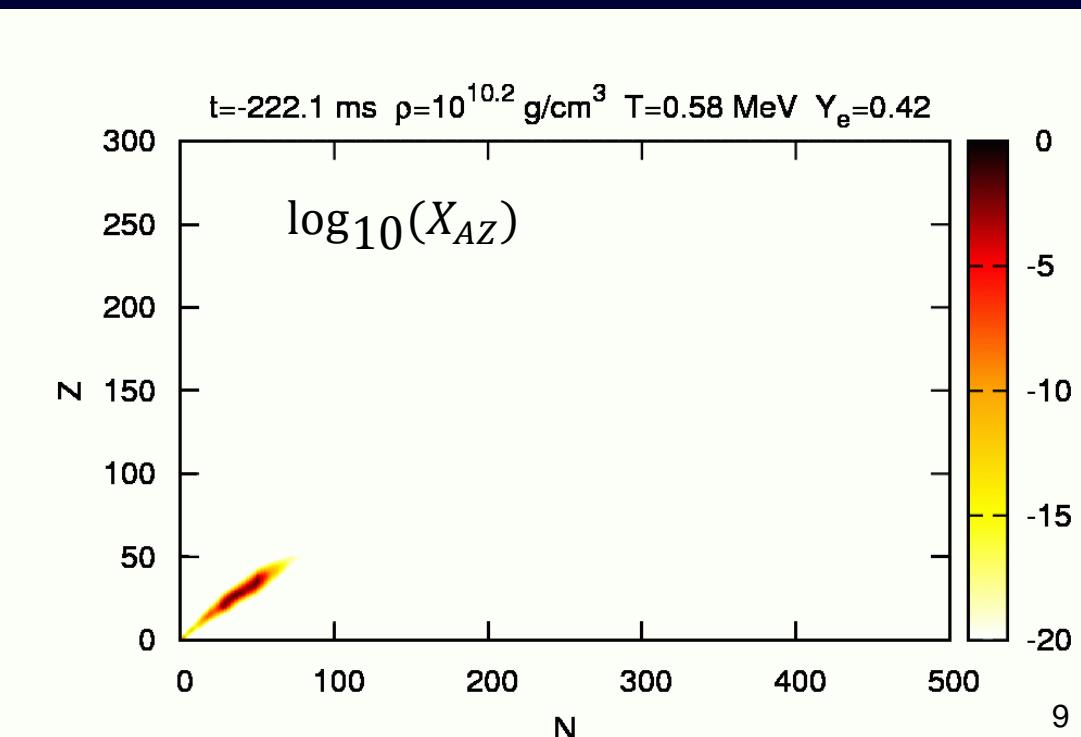


Nuclear Statistical Equilibrium (NSE, 核統計平衡)

- $\tau_{\text{nuclear reaction}}$ (strong and ele.mag.) $\ll \tau_{\text{dynamics}}$
- All nuclear components in chemical equilibrium @ $T \sim 0.4$ MeV
 - $(A, Z) \leftrightarrow (A - 1, Z) + n$ $X(Z, N)$
 - $(A, Z) \leftrightarrow (A - 1, Z - 1) + p$
- Free energy minimization $\Rightarrow \mu_{AZ} = Z \mu_p + (A - Z) \mu_n$

Ex1) Central mass fraction of stellar core collapse

- Dense electrons reduce nuclear Coulomb energy.
→ **large mass nuclei**
- $\mu_n > \mu_p$
→ **neutron-rich nuclei**
- Nuclei are excited.

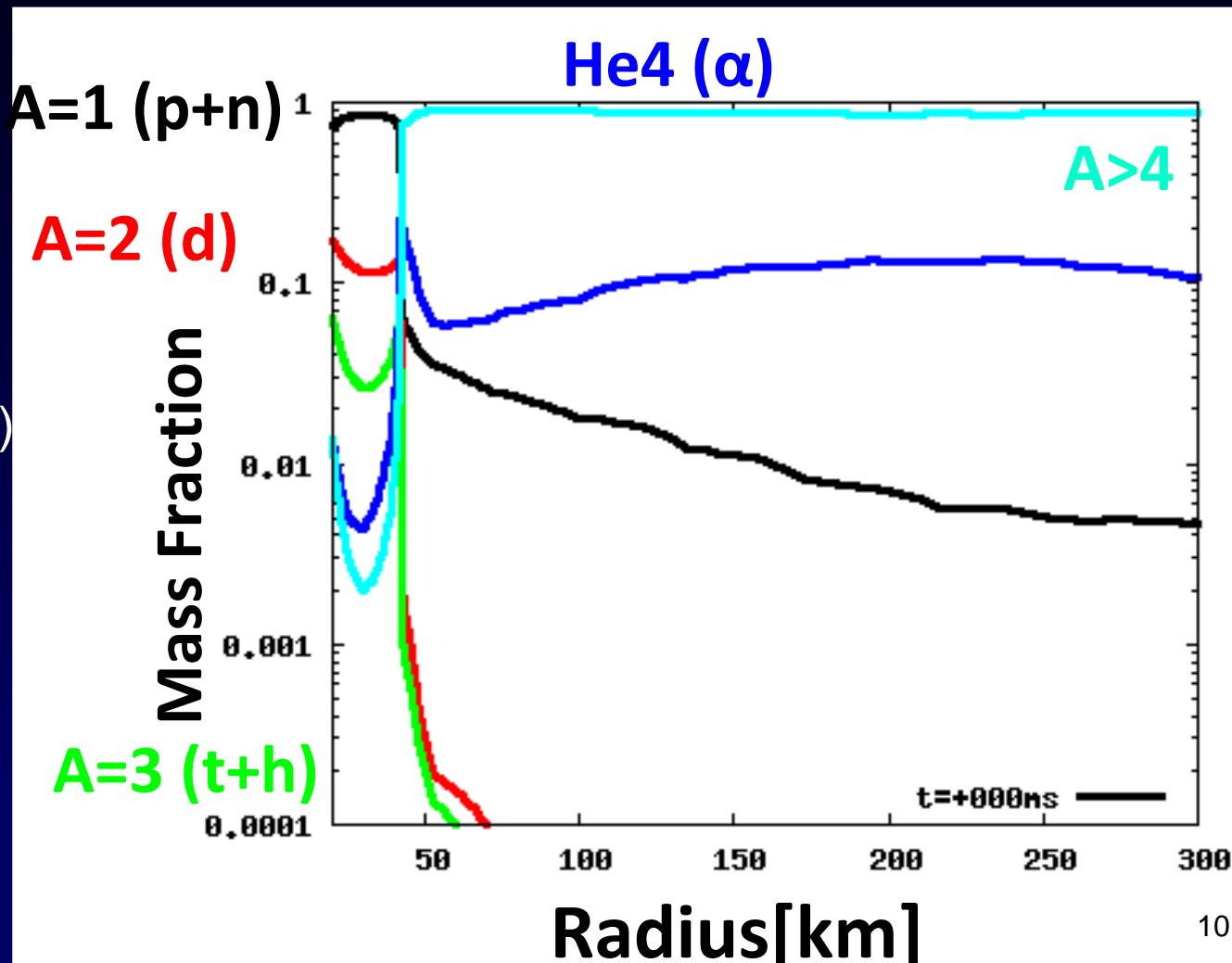


Nuclear Statistical Equilibrium (NSE, 核統計平衡)

- $\tau_{\text{nuclear reaction}} \ll \tau_{\text{dynamics}}$
- All nuclear components in chemical equilibrium @ $T \sim 0.4$ MeV
- Free energy minimization \Rightarrow NSE $\mu_{AZ} = Z \mu_p + (A - Z) \mu_n$

Ex2) Mass fraction of shocked matter

Light cluster physics
(deuteron weak rates,
pairing at high T & p...)
should be improved.
(SF+13b)



Current EOS tables as functions of (ρ , T , Y_e)

Soft $R_{1.4} < 12.5$ km, $R_{1.4} = 12.5\text{-}13.5$ km, $R_{1.4} > 13.5$ km stiff

- Single Nucleus Approximation EOS : n, p, α , $\langle A \rangle$

- Compressible LDM (LS)- Skyrme **180, 220, 375** (Latimer+'91)
- Thomas-Fermi (STOS) –RMF **TM1e** (in prep.) , **TM1**(H. Shen+'98),
 - **Variational method with AV18 & UIX** (Togashi+'17)

- Nuclear Statistical Equilibrium EOS : n, p & all nuclei

- HS - **SFHo**, **DD2**, **TM1**, ... (Hempel+'11, Steiner+'13)
- FYSS – **AV18 & UIX** (SF, Togashi+'17) , **TM1** (SF+'13,'17) ,
 - **χ EFT** , **DBHF** with Bonn A, **TM1e** (SF+ in prep.)
- RG – **SLy4** (Raduta & Gulminelli'18)

- Hybrid EOS : NSE @low ρ & SNA @high ρ

- SHO - **FSU**, **FSU2.1**, **NL3** (G.Shen et al. '11)
- SRO - **SLy4**, **KDE0v1**, **NRAPR**, **LS220** (Schneider et al. '17)

**Different Inputs
for NSE EOS**
①bulk matter,
②masses, and
③excitations

Systematical study of nuclear physics inputs for NSE EOS (SF, PRC '18b)

free energy density

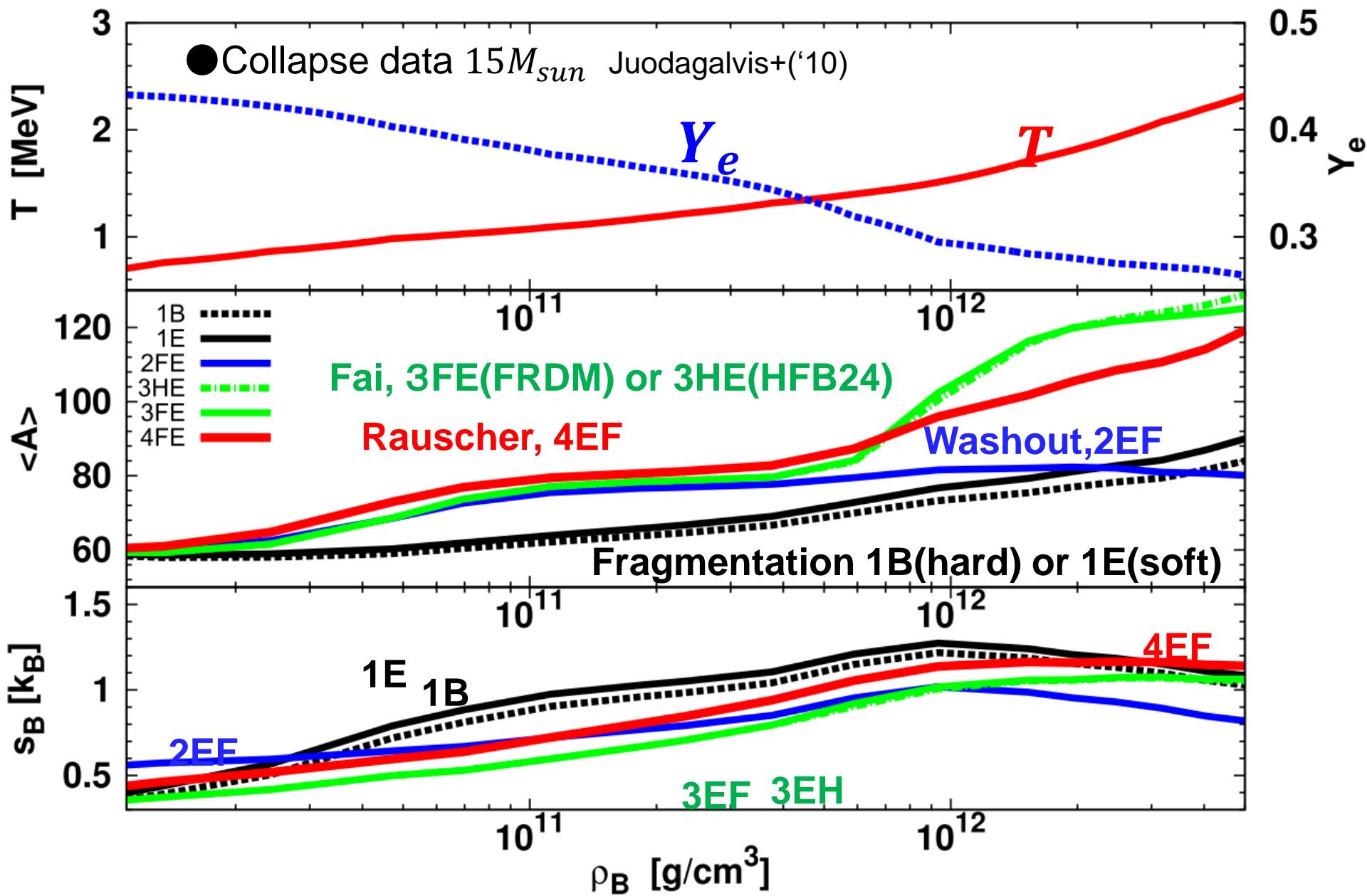
$$f = f_{n,p} + \sum_{AZ} n_{AZ} (E_{AZ}^{kin} + M_{AZ})$$

Individual number density

$$n_{AZ} = \kappa g_{AZ} \left(\frac{M_{AZ} T}{2\pi\hbar^2} \right)^{3/2} \exp \left(\frac{\mu_{AZ} - M_{AZ}}{T} \right).$$

Name	g_{AZ} Nuclear Excitations	$f_{n,p}$ (+ M_{AZ}) Bulk matter	M_{data} Mass data
1B	Fragmentation model (~SMSM)	B(Stiff)	No
1E			
2EF	Liquid drop model + shell washout (~FYSS)	E(Soft)	FRDM
3EF	Fai & Randrup (1982)	Oyamatsu & Iida ('07)	
3EK	(~HS)		HFB24
4EF	Rauscher (2003) (~SRO)		FRDM

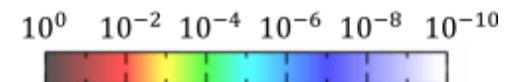
Average nuclear size and entropy are sensitive to excitation models



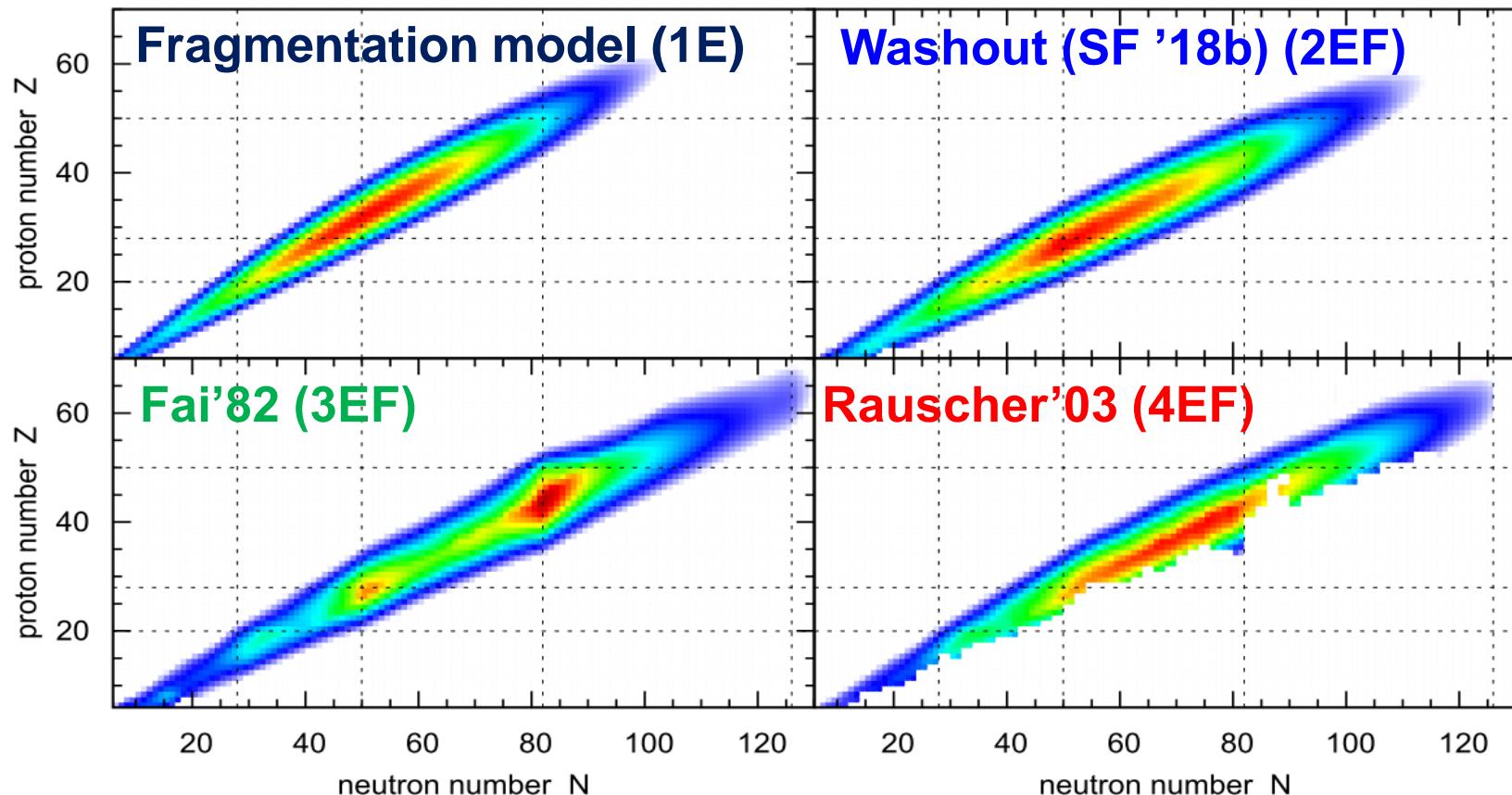
Nuclei at $\rho \sim 10^{11-12} \text{ g/cc}$

● Mass Fraction

$$X_{AZ} = An_{AZ}/(n_n + n_p + \sum An_{AZ})$$

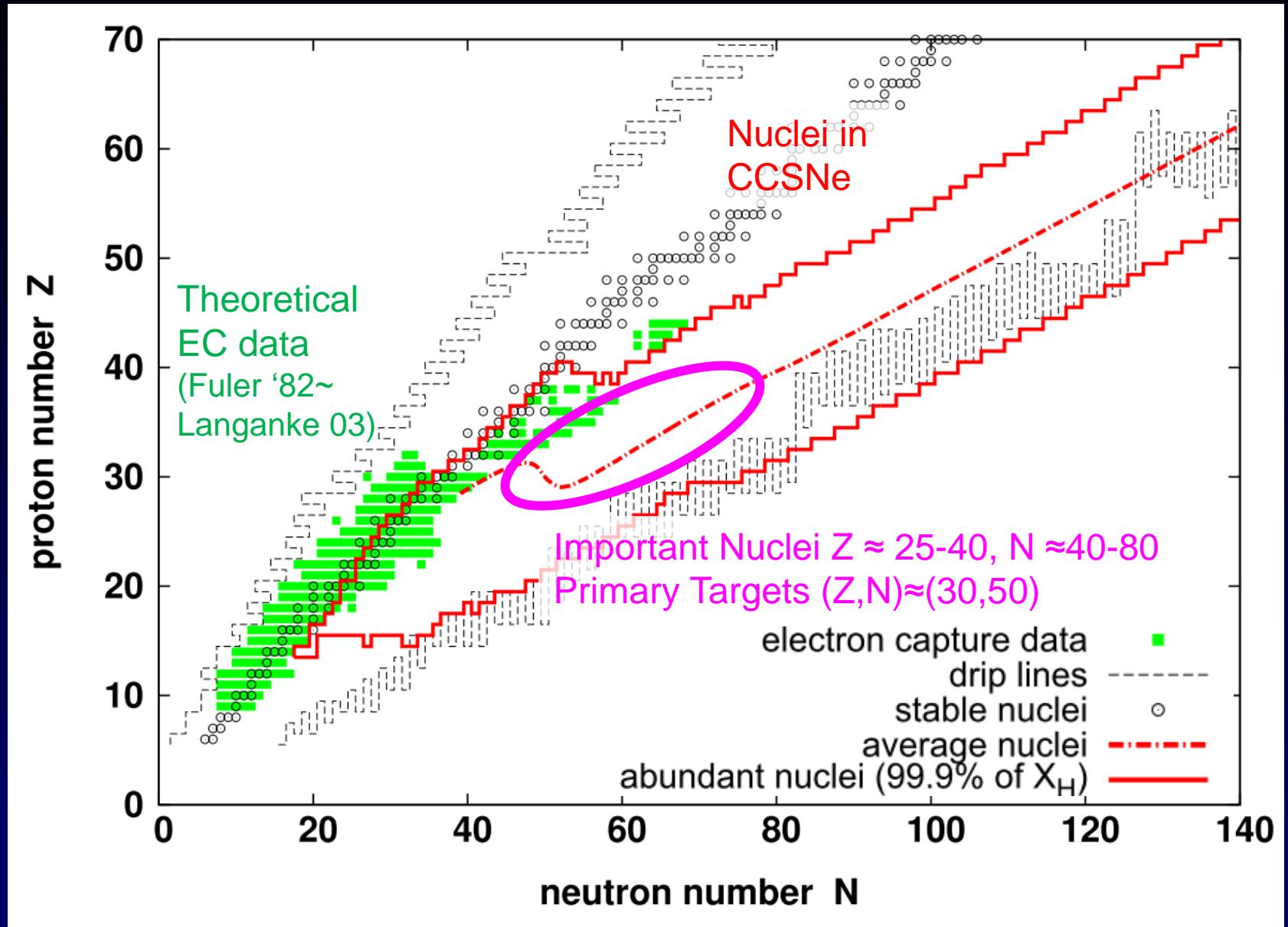


Mass fraction at $\rho = 2.0 \times 10^{12} \text{ g/cc}$, $T = 1.8 \text{ MeV}$, $Y_e = 0.28$



- Nuclei with $(N,Z)=(40-80,25-40)$
- Sensitive to choice of excitation models
- Nuclei with $(N,Z) \approx (50,30)$ are commonly abundant in all models

Lack of Electron Capture Data $(N, Z) + e^- \rightarrow (N + 1, Z - 1) + \nu_e$
(+ partition function level densities for Equation of State)

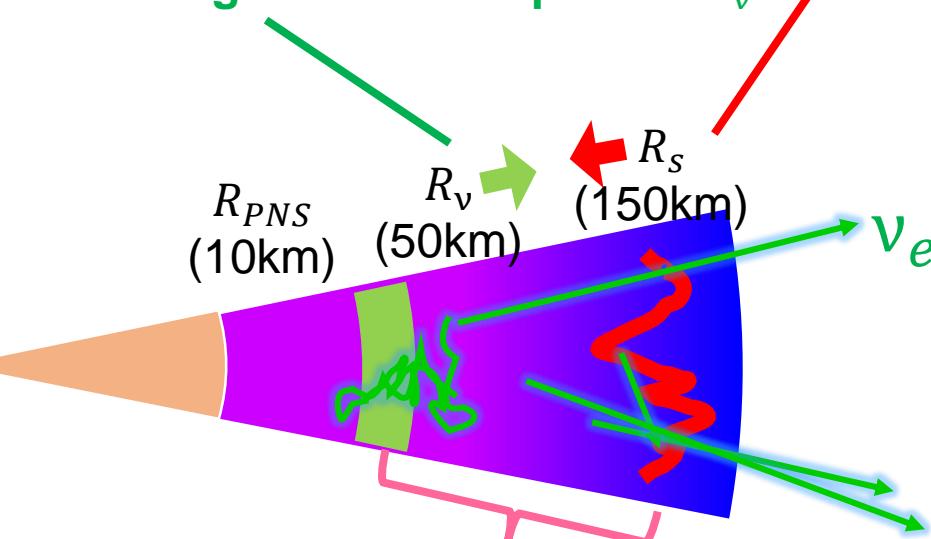


Electron captures on nuclei reduce neutrino bursts

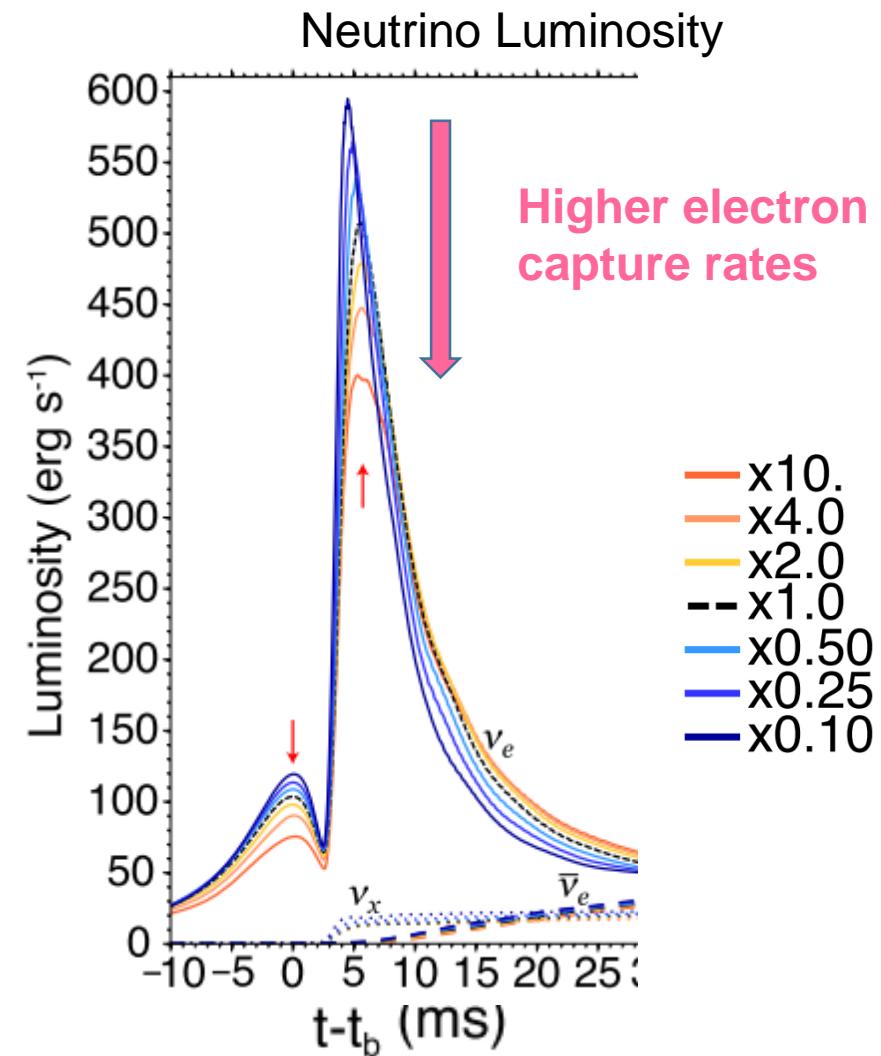
(Sullivan et al.16, see also Hix '03, Lentz '13)

More electron captures on nuclei

- ⇒ ① fewer leptons
- ⇒ smaller proto NS
- ⇒ **smaller shock radius R_s**
- ⇒ ② more neutrino captures
- ⇒ **larger neutrino spheres R_ν**



⇒ **smaller neutrino emissions**



Summary

- Core-Collapse Supernovae greatly depends on weak rates and nuclear statistical equilibrium (NSE).
- NSE EOS requires ① bulk matter calculation,
② mass data, and
③ nuclear excitation model
(the most ambiguous part).
- Nuclei with $(N,Z)=(40-80,25-40)$ appear at $\rho \sim 10^{11-12} \text{ g/cc}$.
- Primary targets are nuclei with $(N,Z) \approx (50,30)$
- We lack in their model or data of
Electron Captures (β^+ strength distribution)
and nuclear excitations (level density).