

Constraints on saturation properties by using neutron star observations

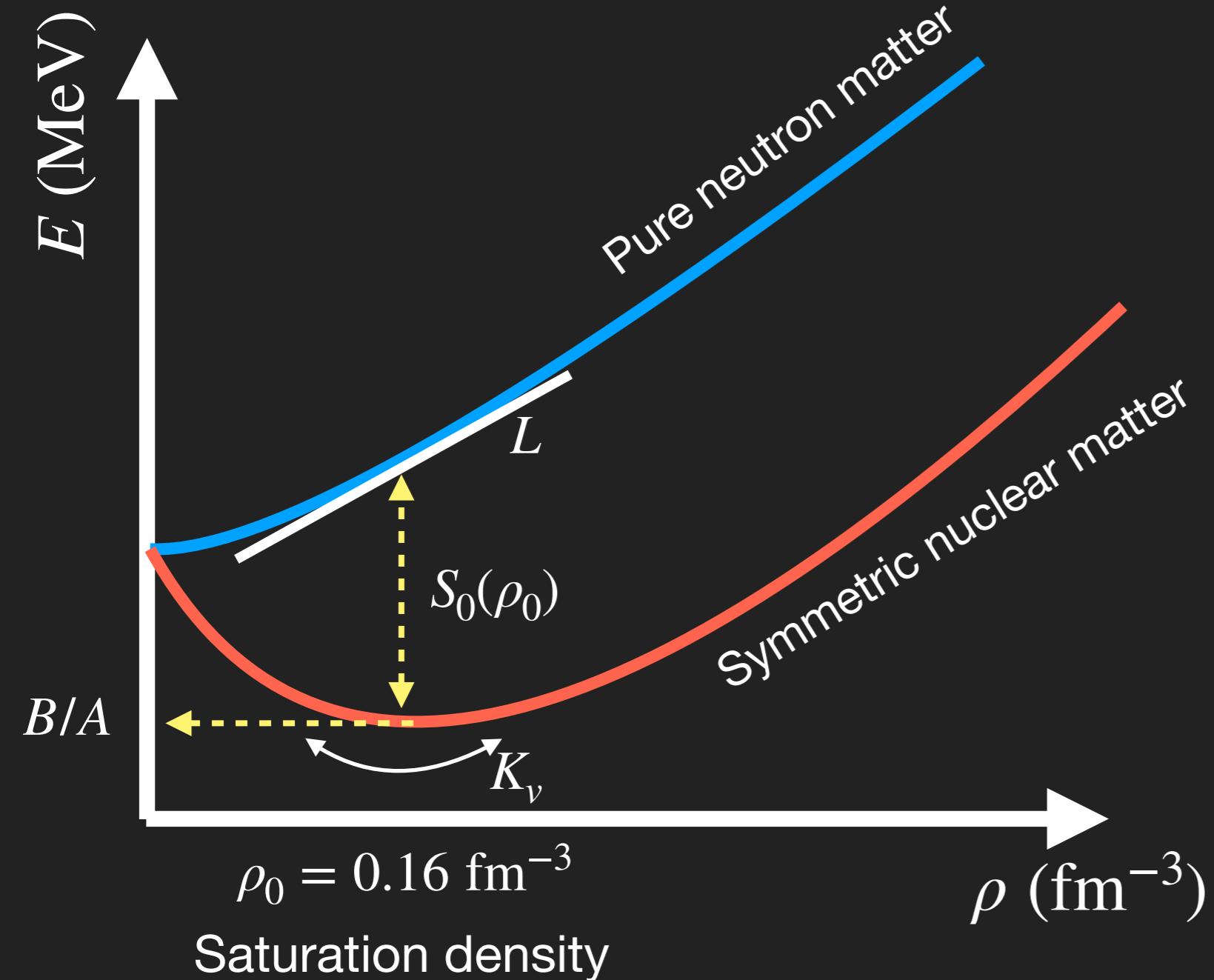
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Soongsil University

Saturation properties



Binding energy

$$B/A \approx -16.0 \text{ MeV}$$

Symmetry energy

$$S_0(\rho_0) = 32.5 \pm 0.5 \text{ MeV} \quad [1]$$

Slope parameter

$$L = 55 - 85 \text{ MeV} \quad [1]$$

Incompressibility

$$K = 180 - 260 \text{ MeV} \quad [2]$$

Effective mass

$$m^*/m = 0.7 - 0.8 \quad [3]$$

[1]PRL 108 052501 (2012)



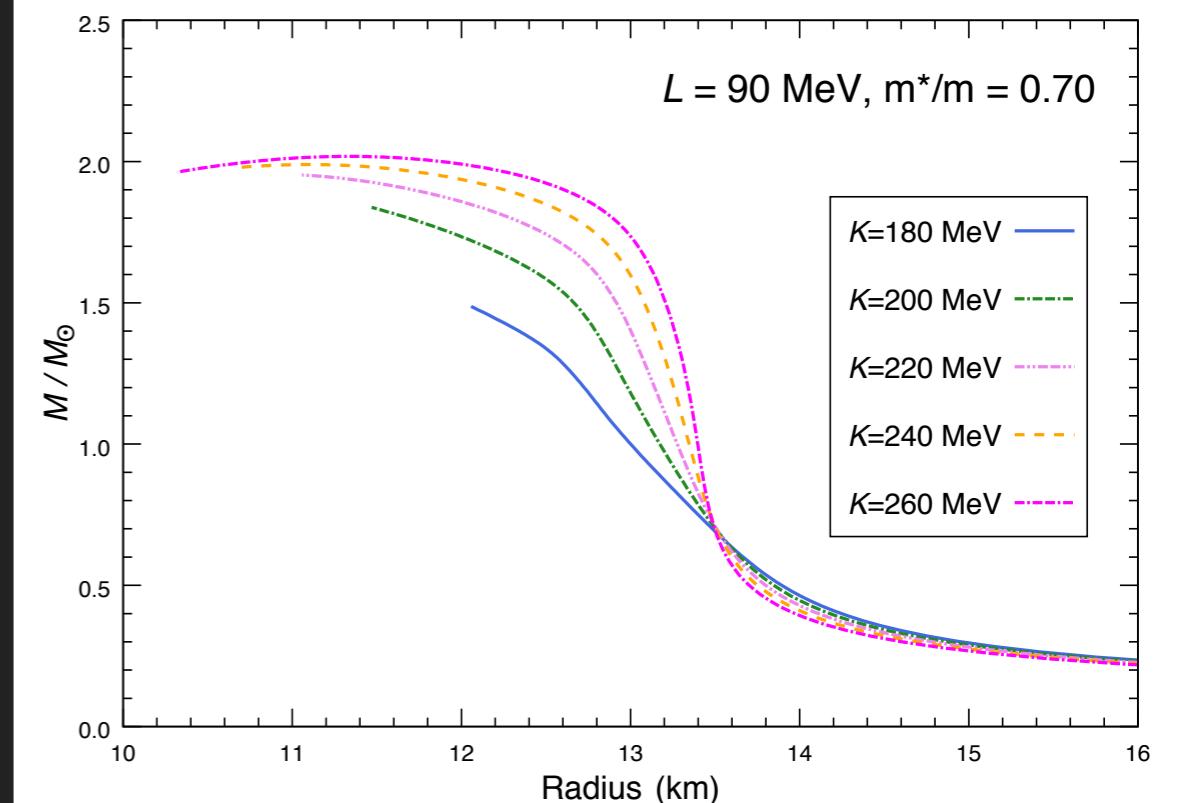
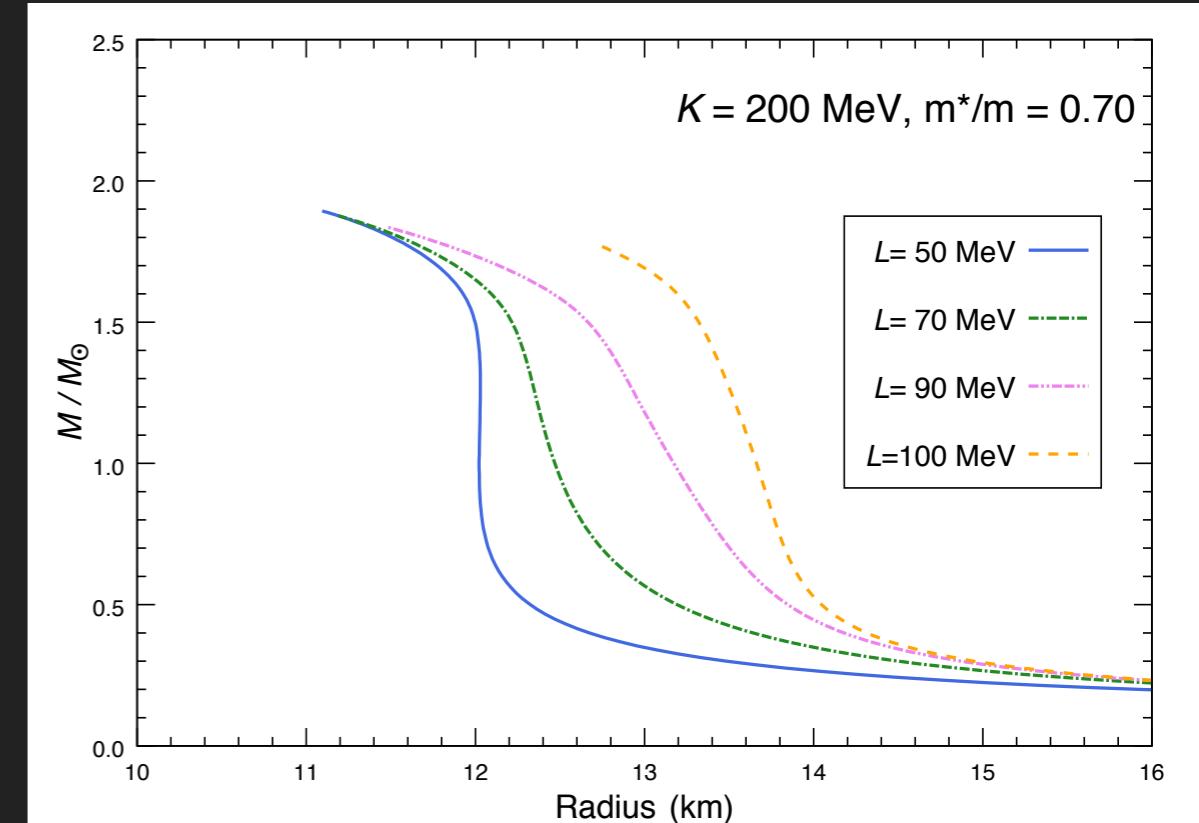
[2]PLB 778 207212 (2018) [3]Nucl. Phys. A 950 64109 (2016)

The effect of L and K on neutron stars

Neutron stars strongly depend on slope parameter and incompressibility

$R(1.4M_{\odot})$: 12 – 14 km

Maximum mass : $1.5 - 2.1M_{\odot}$



A two-solar-mass neutron star measured using Shapiro delay

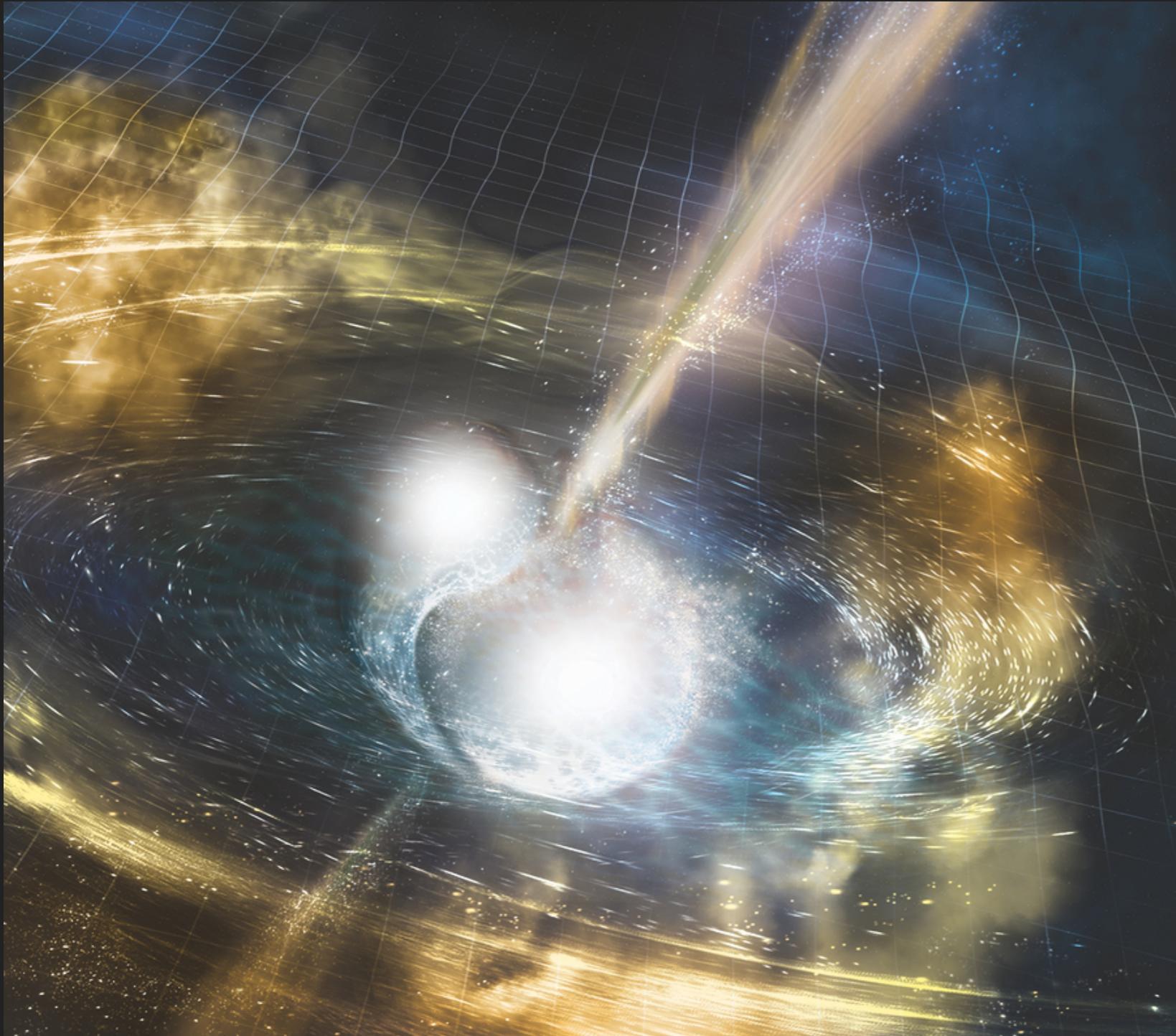
P. B. Demorest¹, T. Pennucci², S. M. Ransom¹, M. S. E. Roberts³

Neutron stars are composed of the densest form of matter known to exist in our Universe, the composition and properties of which are still theoretically uncertain. Measurements of the masses or radii of these objects can strongly constrain the neutron star matter equation of state and rule out theoretical models of their composition^{1,2}. The observed range of neutron star masses, however, has hitherto been too narrow to rule out many predictions of ‘exotic’ non-nucleonic components^{3–6}. The Shapiro delay is a general-relativistic increase in light travel time through the curved space-time near a massive body⁷. For highly inclined (nearly edge-on) binary millisecond radio pulsar systems, this effect allows us to infer the masses of both the neutron star and its binary companion to high precision^{8,9}. Here we present radio timing observations of the binary millisecond pulsar J1614-2230^{10,11} that show a strong Shapiro delay signature. We calculate the pulsar mass to be $(1.97 \pm 0.04)M_{\odot}$, which rules out almost all currently proposed^{2–5} hyperon or boson condensate equations of state (M_{\odot} , solar mass). Quark matter can support a star this massive only if the quarks are strongly interacting and are therefore not ‘free’ quarks¹².

Table 1 | Physical parameters for PSR J1614-2230

Parameter	Value
Ecliptic longitude (λ)	245.78827556(5) $^{\circ}$
Ecliptic latitude (β)	-1.256744(2) $^{\circ}$
Proper motion in λ	9.79(7) mas yr $^{-1}$
Proper motion in β	-30(3) mas yr $^{-1}$
Parallax	0.5(6) mas
Pulsar spin period	3.1508076534271(6) ms
Period derivative	9.6216(9) $\times 10^{-21}$ ss $^{-1}$
Reference epoch (MJD)	53,600
Dispersion measure*	34.4865 pc cm $^{-3}$
Orbital period	8.6866194196(2) d
Projected semimajor axis	11.2911975(2) light s
First Laplace parameter ($e \sin \omega$)	1.1(3) $\times 10^{-7}$
Second Laplace parameter ($e \cos \omega$)	-1.29(3) $\times 10^{-6}$
Companion mass	0.500(6) M_{\odot}
Sine of inclination angle	0.999894(5)
Epoch of ascending node (MJD)	52,331.1701098(3)
Span of timing data (MJD)	52,469–55,330
Number of TOAs†	2,206 (454, 1,752)
Root mean squared TOA residual	1.1 μ s
Right ascension (J2000)	16 h 14 min 36.5051(5)s
Declination (J2000)	-22° 30' 31.081(7)'
Orbital eccentricity (e)	1.30(4) $\times 10^{-6}$
Inclination angle	89.17(2) $^{\circ}$
Pulsar mass	1.97(4) M_{\odot}
Dispersion-derived distance‡	1.2 kpc
Parallax distance	>0.9 kpc
Surface magnetic field	1.8 $\times 10^{8}$ G
Characteristic age	5.2 Gyr
Spin-down luminosity	1.2 $\times 10^{34}$ erg s $^{-1}$
Average flux density* at 1.4 GHz	1.2 mJy
Spectral index, 1.1–1.9 GHz	-1.9(1)
Rotation measure	-28.0(3) rad m $^{-2}$

Tidal deformability



Mass

$$m_1 = 1.36 - 1.60 M_{\odot}$$
$$m_2 = 1.17 - 1.36 M_{\odot}$$

Distance

$$40^{+8}_{-14} \text{ Mpc}$$

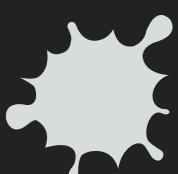
Dimensionless
tidal deformability

$$70 \leq \Lambda(1.4M_{\odot}) \leq 580$$

NSF/LIGO/Sonoma State University/A. Simonnet
<https://www.ligo.caltech.edu/image/ligo20171016d>

Tsukuba-CCS workshop

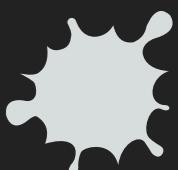
PRL 121 161101 (2018)



Tidal deformability

If we consider a static, spherically symmetric star of mass (m) placed in a time-independent external quadrupole tidal field.

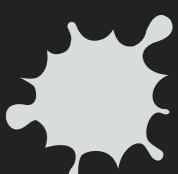
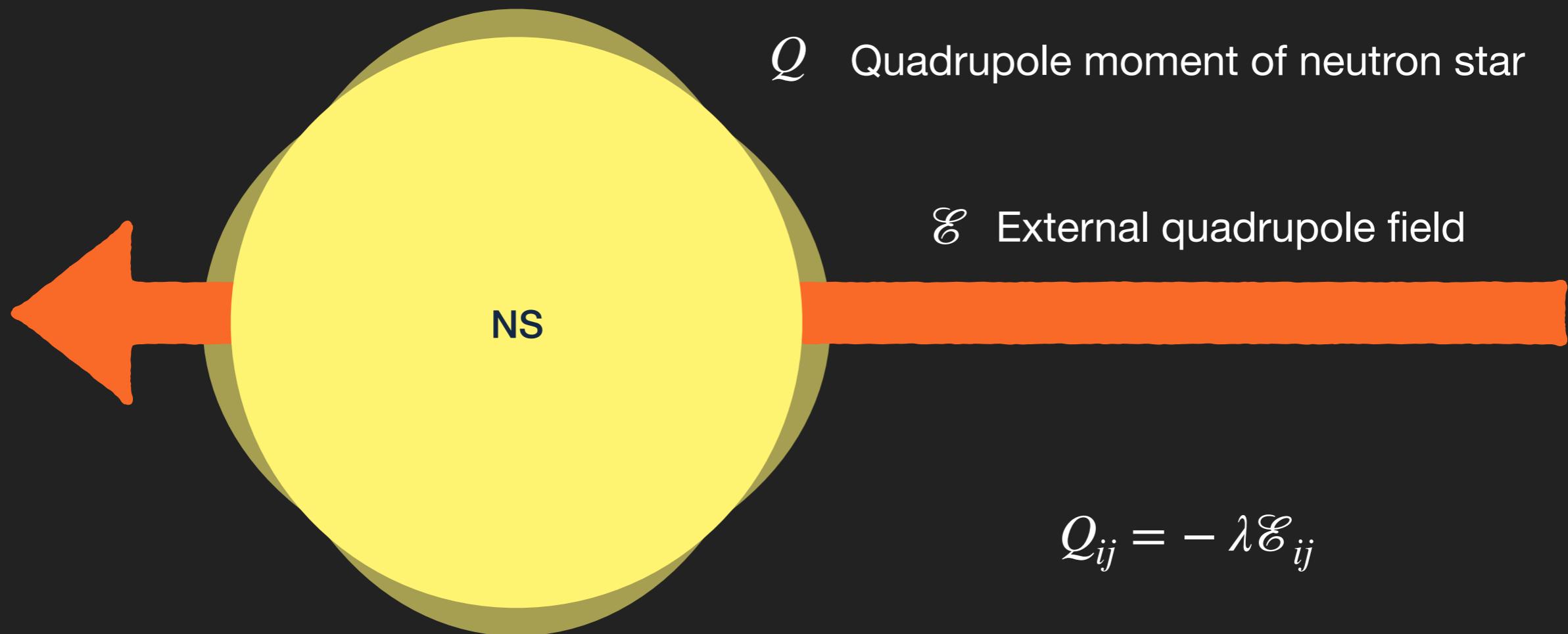
The star will develop in response a quadrupole moment



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The star will develop in response a quadrupole moment



What do we use?

λ : a constant which is related to the tidal deformability Λ

$$\Lambda = \frac{5}{2} \lambda \frac{1}{M} \left(\frac{c^2}{G} \right)^5 \quad G : \text{Gravitational coefficient}$$

$$70 \leq \Lambda(1.4M_{\odot}) \leq 580$$

PRL 121 161101 (2018)

$$1.94 M_{\odot} \leq M_{\text{NS}} \leq 2.33 M_{\odot}$$

Nature 467 1081-1083 (2010)
APJL 852 L25 (2018)

By using these observation data,
we can constraint on slope parameter and incompressibility.



Relativistic mean field model

Lagrangian density for static uniform nuclear matter :

$$B = N, \Lambda, \Sigma^{-,0,+}, \Xi^{-,0}$$

$$\begin{aligned} \mathcal{L} = & \sum_B \bar{\psi}_B [i\gamma_\mu \partial^\mu - M_B^*(\sigma_0, \sigma_0^*) - g_{\omega B} \gamma_0 \omega_0 - g_{\phi B} \gamma^0 \phi^0 - g_{\rho B} \gamma^0 \rho_0 I_{3B}] \psi_B \\ & - \frac{1}{2} m_\sigma^2 \sigma_0^2 - \frac{1}{2} m_{\sigma^*}^2 \sigma_0^{*2} + \frac{1}{2} m_\omega^2 \omega_0^2 + \frac{1}{2} m_\phi^2 \phi_0^2 + \frac{1}{2} m_\rho^2 \rho_0^2 - U_{NL}(\sigma_0, \omega_0, \rho_0) \end{aligned}$$

The effective baryon mass in matter :

$$M_B^*(\sigma, \sigma^*) = M_B - g_{\sigma B} \sigma - g_{\sigma^* B} \sigma^*$$

The following non-linear term is also introduced in order to reproduce the saturation properties of nuclear matter :

$$U_{NL}(\sigma, \omega^\mu \rho^\mu) = \frac{1}{3} g_2 \sigma^3 + \frac{1}{4} g_3 \sigma^4 - \Lambda_v g_{\omega B}^2 g_{\rho B}^2 (\omega_0^2 \rho_0^2)$$



Coupling constants

Coupling constants, $g_{\sigma N}$, $g_{\omega N}$, and $g_{\rho N}$ are determined so as to reproduce the binding energy per nucleon, and symmetry energy at saturation density.

$$B/A = -16.0 \text{ MeV}$$

$$S_0(\rho_0) = 32.5 \text{ MeV}$$

$$\rho_0 = 0.16 \text{ fm}^{-3}$$

The SU(3) symmetry in the vector-meson gives the relations of the coupling constants as

$$g_{\omega\Lambda} = g_{\omega\Sigma} = \frac{1}{1 + \sqrt{3}z \tan \theta_v} g_{\omega N} \quad g_{\rho\Sigma} = 2g_{\rho N}, \quad g_{\rho\Xi} = g_{\rho N} \quad g_{\rho\Lambda} = 0$$

$$g_{\omega\Xi} = \frac{1 - \sqrt{3}z \tan \theta_v}{1 + \sqrt{3}z \tan \theta_v} g_{\omega N} \quad g_{\phi\Lambda} = g_{\phi\Sigma} = -\frac{-\tan \theta_v}{1 + \sqrt{3}z \tan \theta_v} g_{\omega N} \quad g_{\phi\Xi} = -\frac{\sqrt{3}z + \tan \theta_v}{1 + \sqrt{3}z \tan \theta_v} g_{\omega N}$$

$$g_{\phi N} = \frac{\sqrt{3}z - \tan \theta_v}{1 + \sqrt{3}z \tan \theta_v} g_{\omega N}$$

In the present calculation, we refer to the Nijmegen extended-soft-core (ESC) model [1] to fix the mixing angle (θ_v) and z as

$$\theta = 37.50^\circ, \quad z = 0.1949$$



Coupling constants

We need to consider the hyperon coupling. The σ -Y and σ^* -Y are determined as follows. The potential for hyperon Y in symmetric nuclear matter is calculated as

$$U_Y^{(N)} = -g_{\sigma Y}\sigma_0 + g_{\omega Y}\omega_0$$

$$U_\Lambda^{(N)} = -28 \text{ MeV} \quad [1] \quad U_\Sigma^{(N)} = 30 \text{ MeV} \quad [2] \quad U_\Xi^{(N)} = -18 \text{ MeV} \quad [3]$$

The potential for Y in Y-hyperon matter is written as :

$$U_Y^{(Y)} = -g_{\sigma Y}\sigma_0^{(Y)} - g_{\sigma^* Y}\sigma_0^{*(Y)} + g_{\omega Y}\omega^{(Y)} + g_{\phi Y}\phi_0^{(Y)}$$

$$U_\Xi^{(\Xi)} \simeq U_\Lambda^{(\Xi)} \simeq 2U_\Xi^{(\Lambda)} \simeq 2U_\Lambda^{(\Lambda)} \quad [3] \quad U_\Lambda^{(\Lambda)} = -5 \text{ MeV} \quad \text{Nagara event}$$

[¹]PRC 54 1416 (1996), [²]PRC 88 015802 (2013),
[³]PRC 77 025801 (2008)



Coupling constants

We add the following NL potential to the Lagrangian density

$$U_{\text{NL}}(\sigma, \omega^\mu \rho^\mu) = \frac{1}{3}g_2\sigma^3 + \frac{1}{4}g_3\sigma^4 - \Lambda_v g_{\omega B}^2 g_{\rho B}^2 (\omega_0^2 \rho_0^2)$$

Investigated range of incompressibility (K), and the slope parameter (L) at saturation density is

$$\begin{aligned} K &= 180 - 300 \text{ MeV} \\ L &= 30 - 100 \text{ MeV}. \end{aligned}$$

We fix the effective mass ratio at saturation density as

$$m^*/m = 0.7$$



Result (dependence on slope parameter)

- The slope parameter does not affect the maximum mass of neutron star.
- Around the 1.3 solar mass neutron star
Large slope parameter



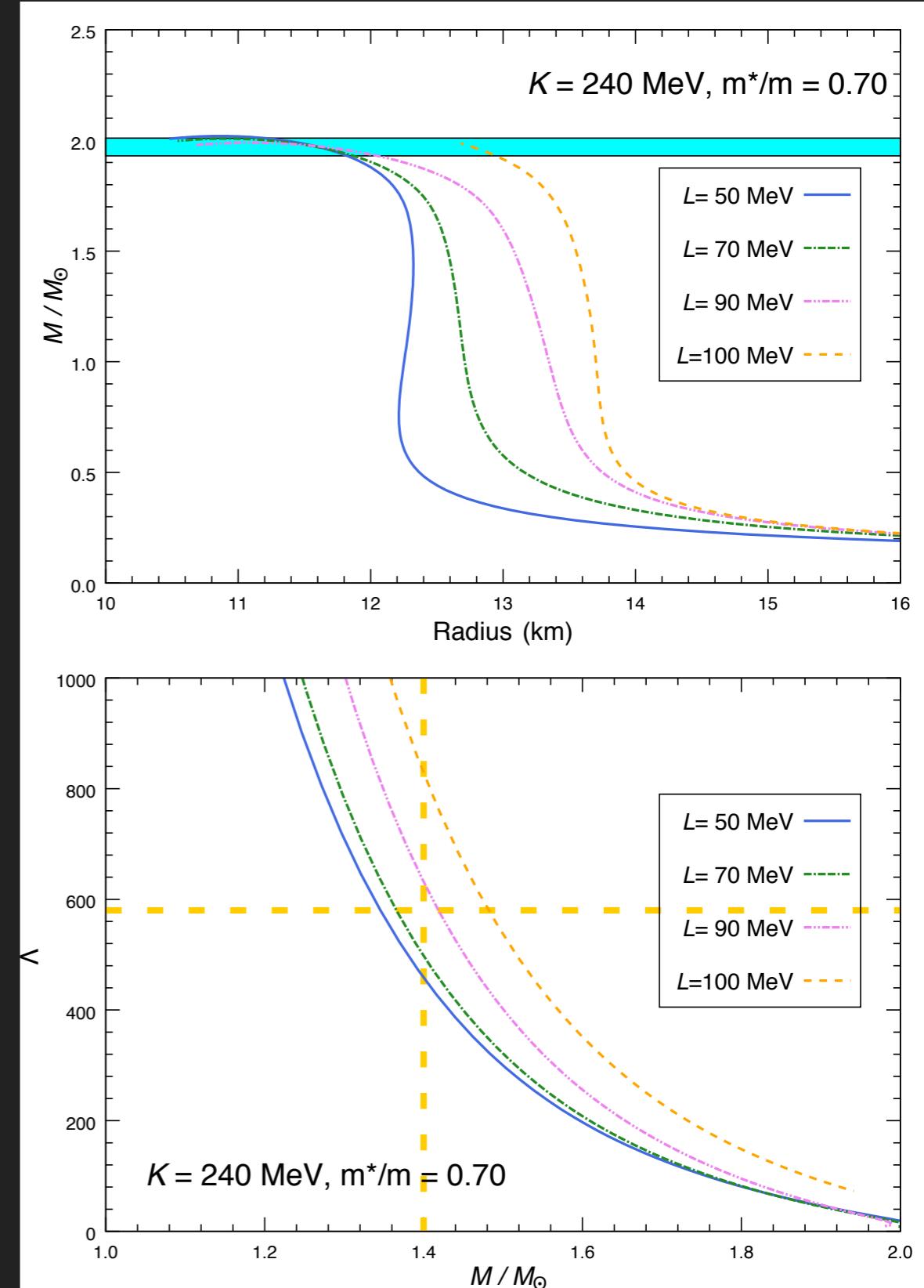
Large radius of neutron star

- In the tidal deformability case, the large slope parameter gives the high tidal deformability.

The onset of Lambda particle

$K_v = 240 \text{ MeV}$

	$L = 50 \text{ MeV}$	70 MeV	90 MeV	100 MeV
ρ_Λ	0.450	0.440	0.410	0.380



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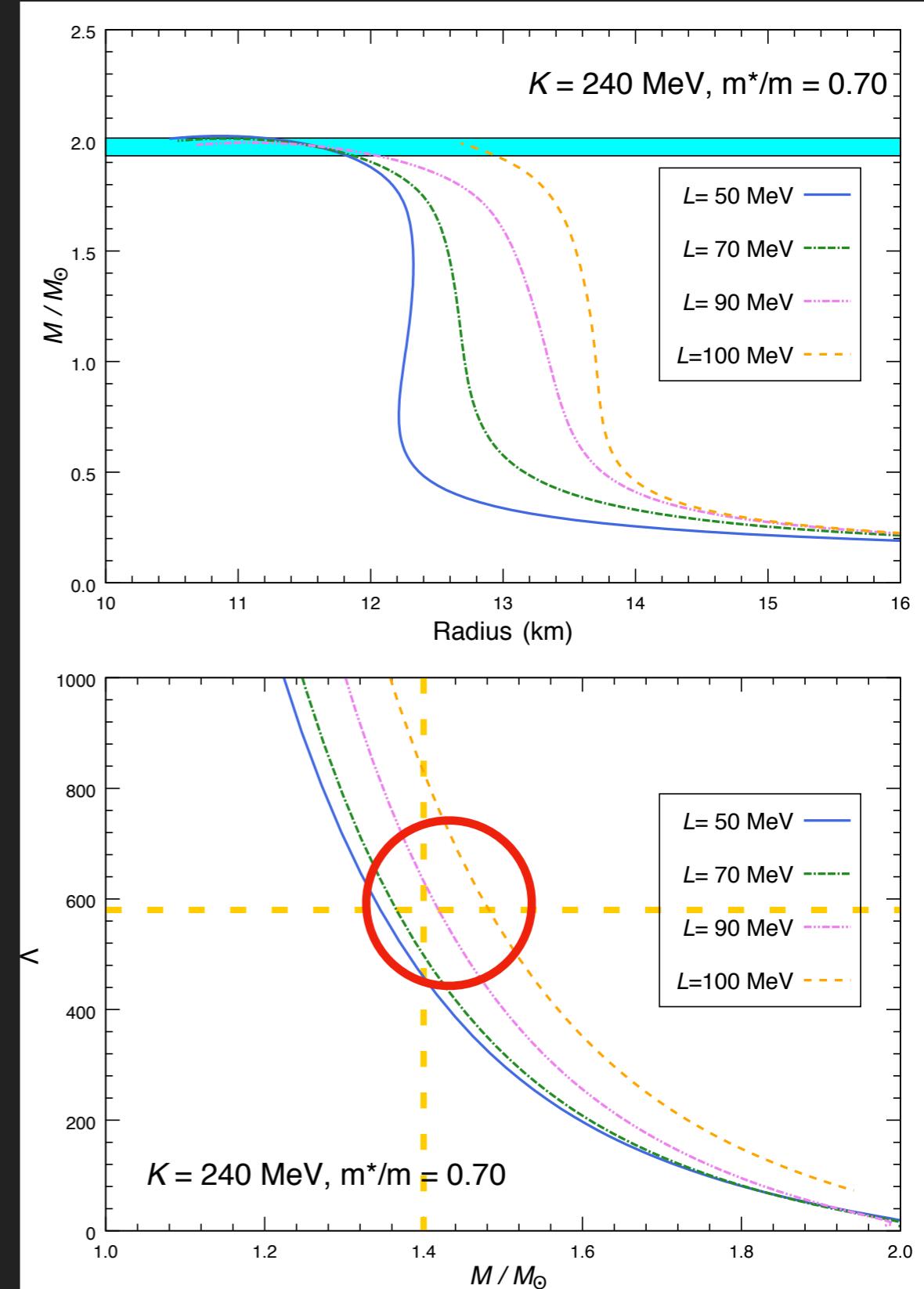
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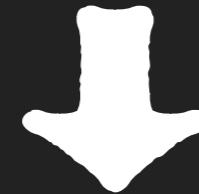
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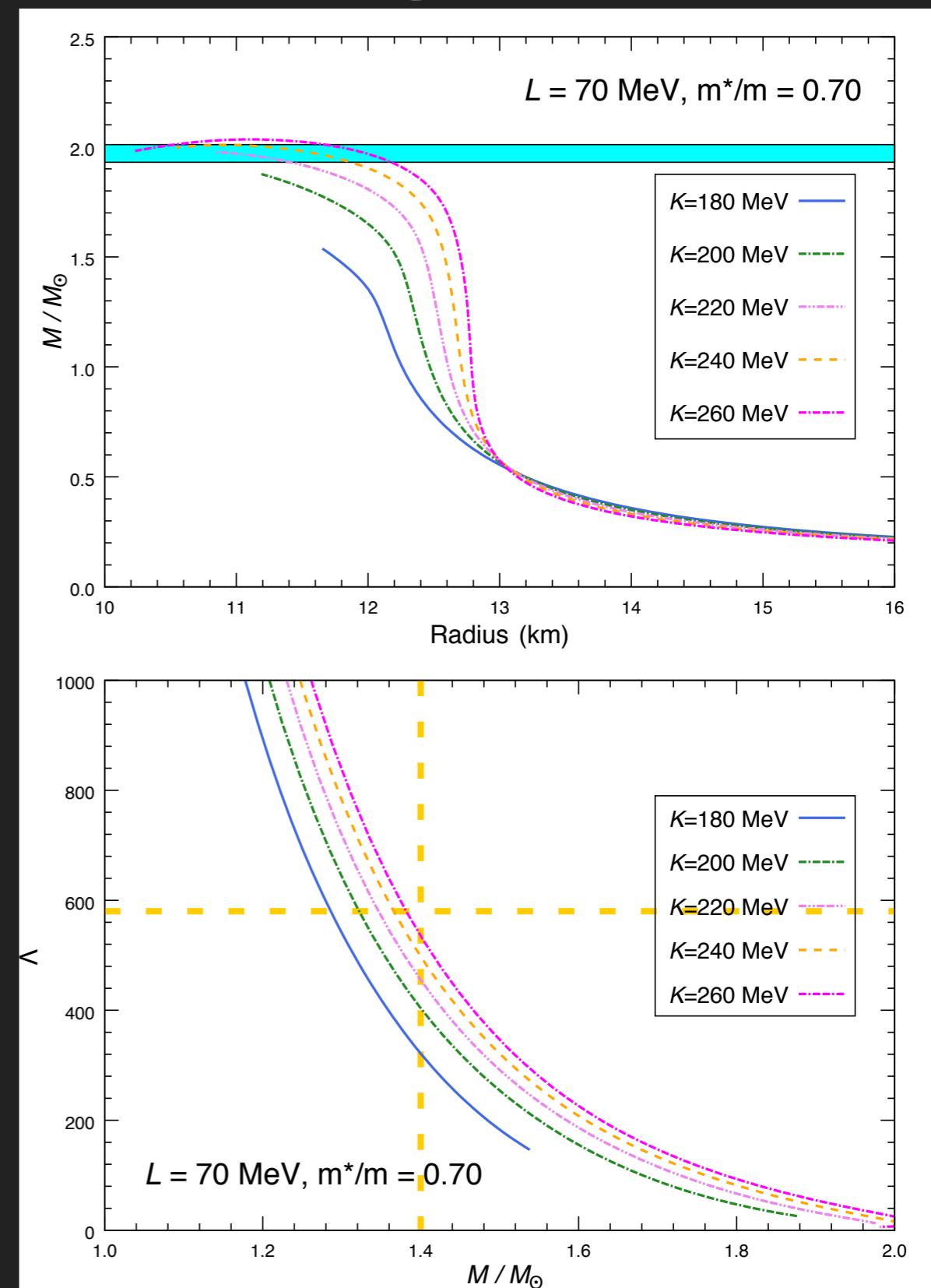
- The incompressibility affect both maximum mass and radius.

Large incompressibility



Large maximum mass

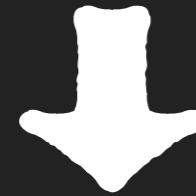
- The effect of incompressibility is around maximum mass of neutron star.
- The two-solar mass neutron star cannot be described in $K = 180$ and 200 MeV cases.



Result (dependence on incompressibility)

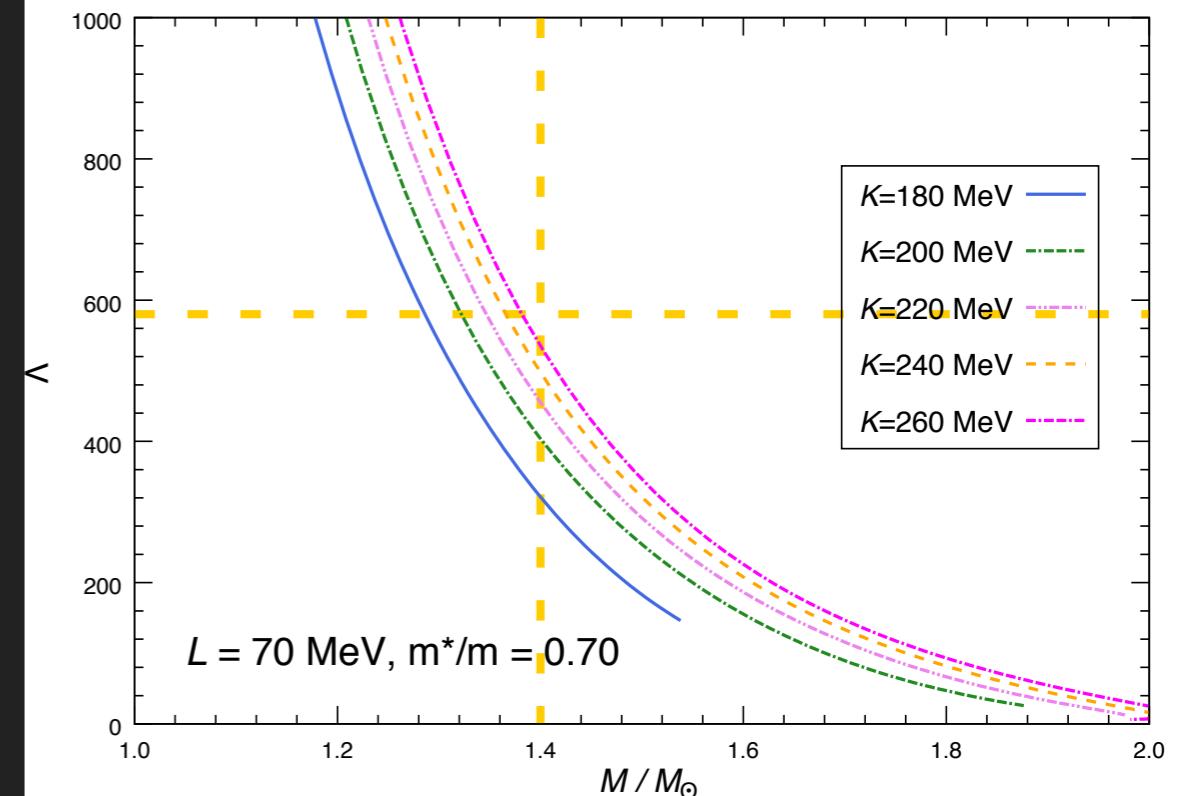
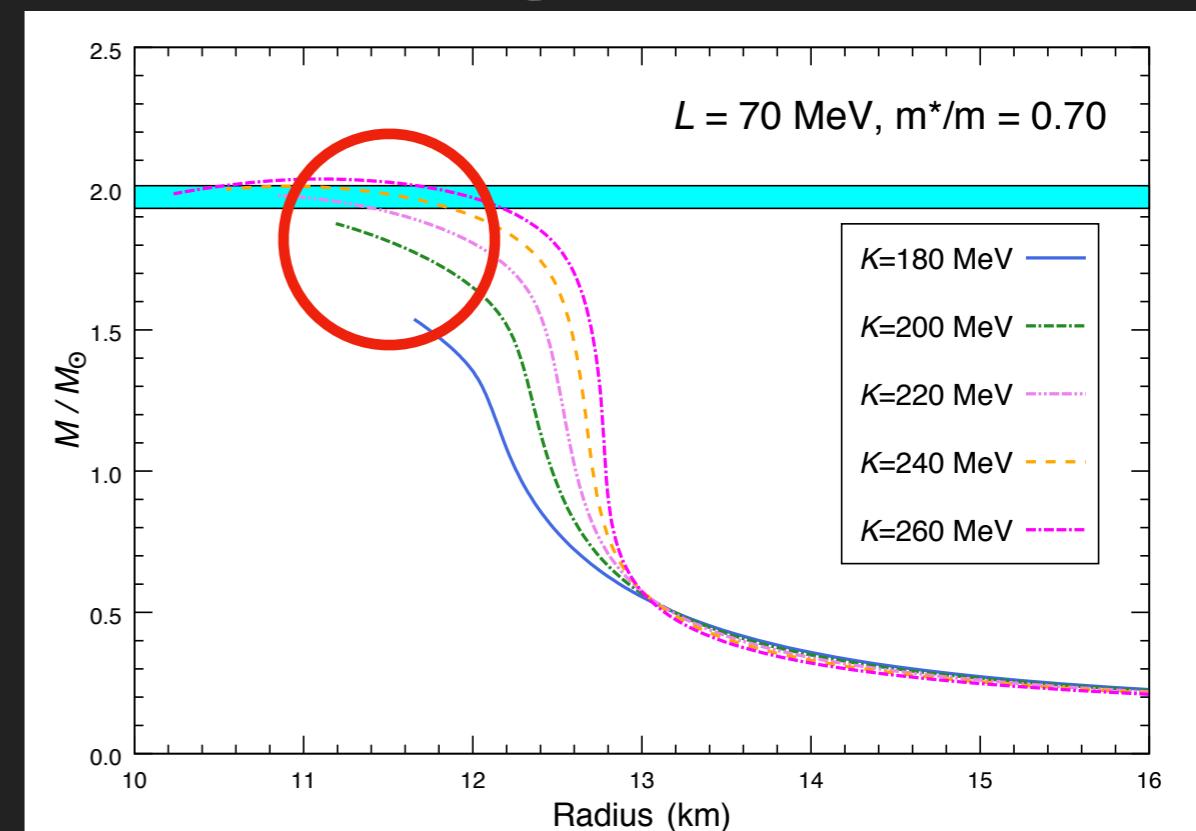
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Large incompressibility

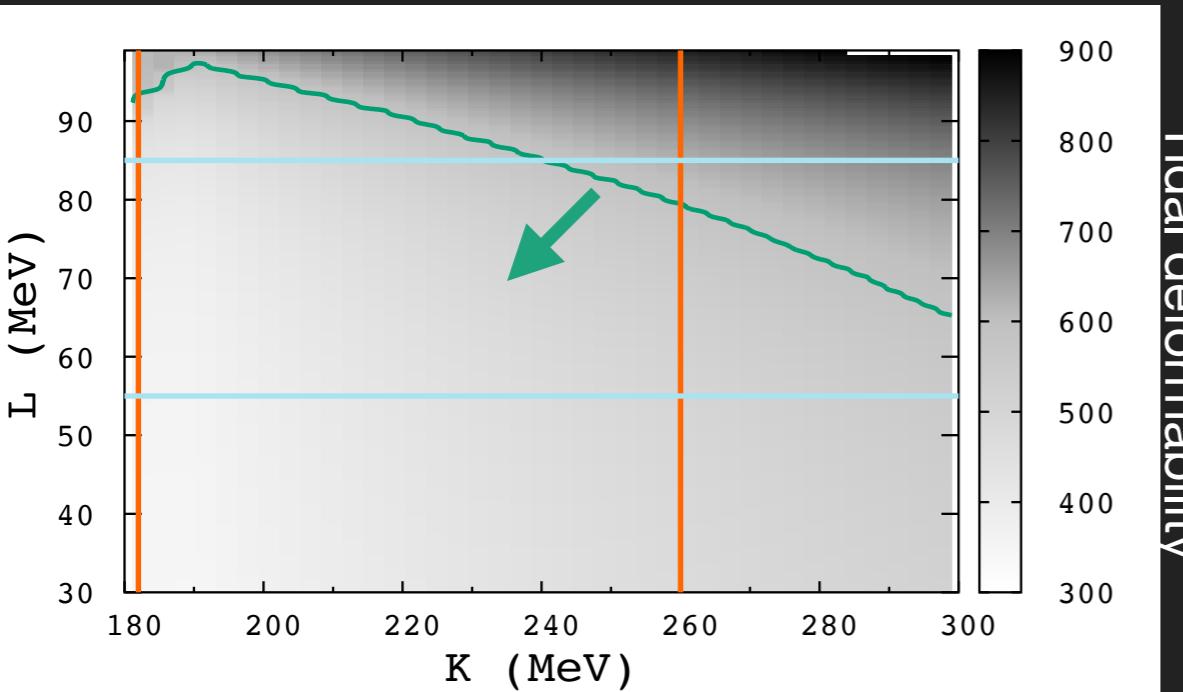


Large maximum mass

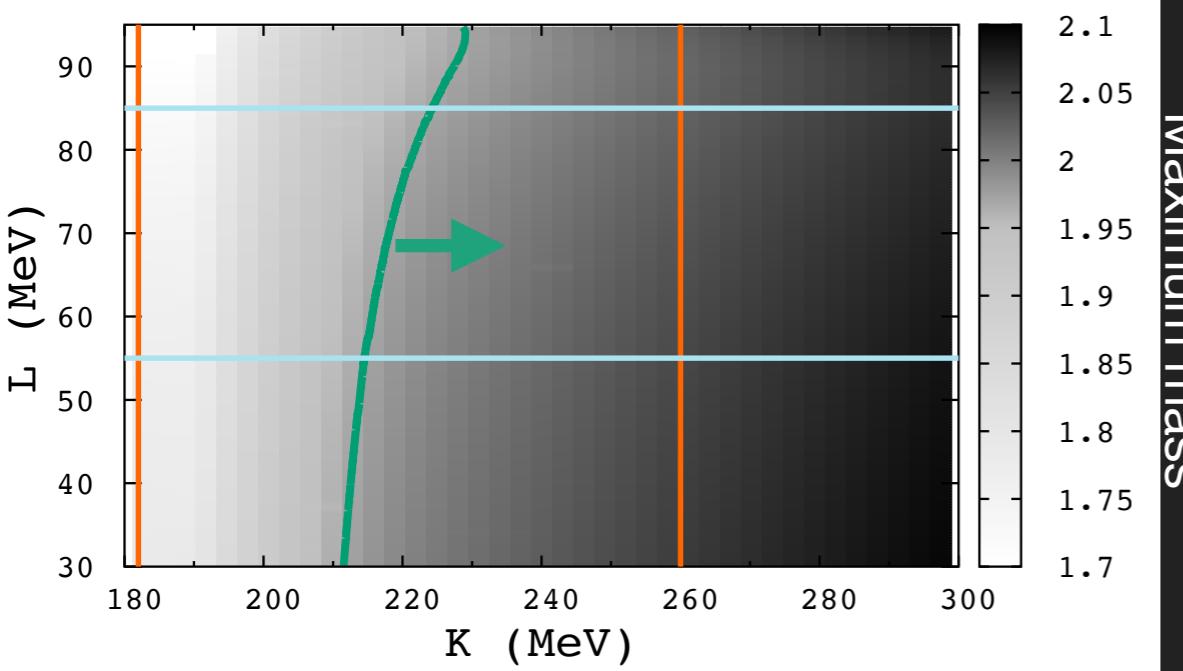
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Summary (contour)



$$L = 55 - 85 \text{ MeV} \quad [1]$$
$$K = 180 - 260 \text{ MeV} \quad [2]$$



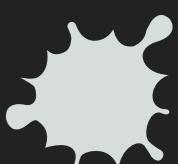
- We changed the slope parameter and incompressibility by using RMF model with non-linear potential
- **We can constrain on slope parameter and incompressibility by using the astronomical observation data**

$$70 \leq \Lambda(1.4M_{\odot}) \leq 580$$

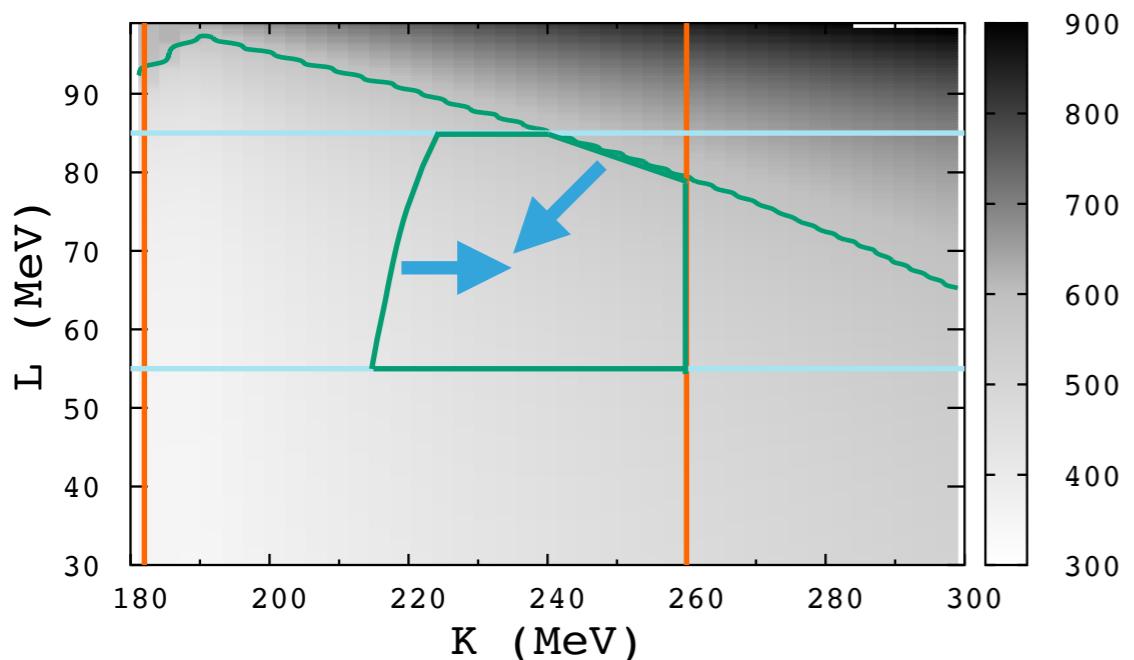
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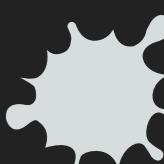
- We changed the slope parameter and incompressibility by using RMF model with non-linear potential
- **We can constrain on slope parameter and incompressibility by using the astronomical observation data**
- **In the ongoing process, we are studying the constraint on these values by using finite-nuclei data.**

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Thank you for your attention

