

China-Japan collaboration workshop on
“Nuclear mass and life for unravelling mysteries of r-process”

Deformed Halo Structure in ^{22}C with Deformed Relativistic Hartree-Bogoliubov Model

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06-27-2017

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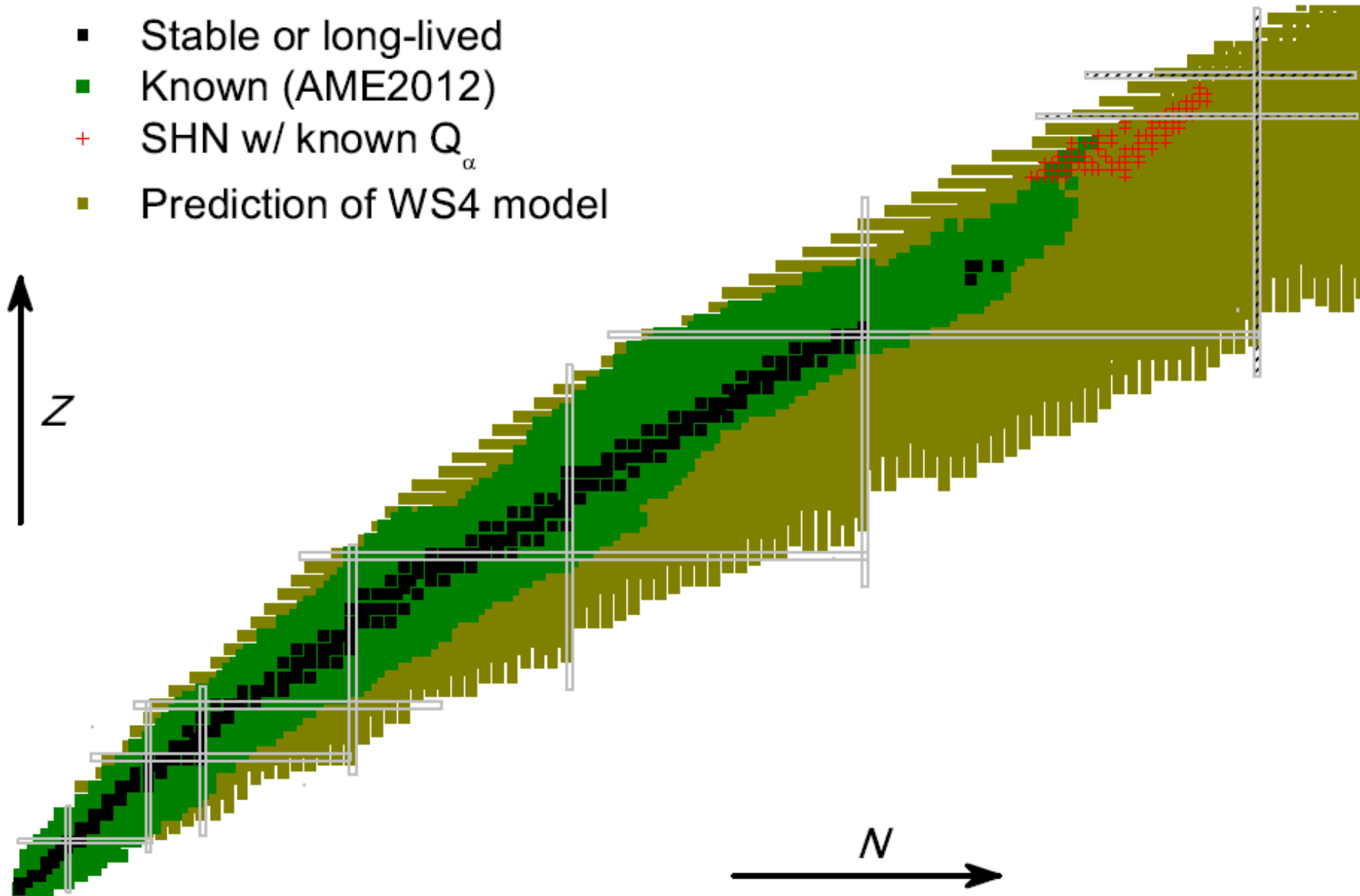
- 1 Background
- 2 Deformed relativistic Hartree-Bogoliubov theory in continuum
- 3 Preliminary results and discussions
 - Carbon isotopes $^{10-22}\text{C}$ properties
 - Halo structure: ^{22}C
- 4 Summary

OUTLINE

- 1 Background
- 2 Deformed relativistic Hartree-Bogoliubov theory in continuum
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Background

- Stable or long-lived
- Known (AME2012)
- + SHN w/ known Q_α
- Prediction of WS4 model



Background

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① In carbon isotopes, ^{15}C , ^{19}C and ^{22}C are halo nuclei, ^{22}C exhibits a Borromean structure.

📄 Isao Tanihata, Herve Savajols and Rituparna Kanungo, *Prog. Part. Nucl. Phys.* **68**, 215-313 (2013);

📄 Y. Togano et al., *Phys. Lett. B* **761**, 412-418 (2016);

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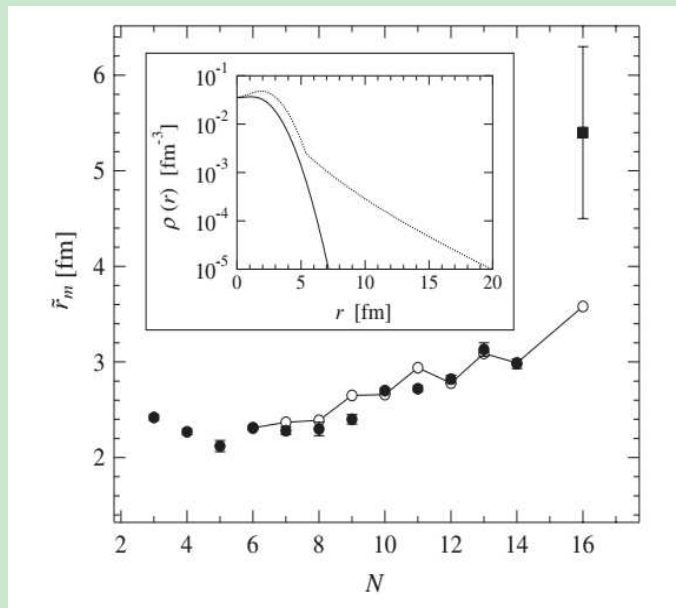
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$$R_m = 5.4 \pm 0.9 \text{ fm}$$

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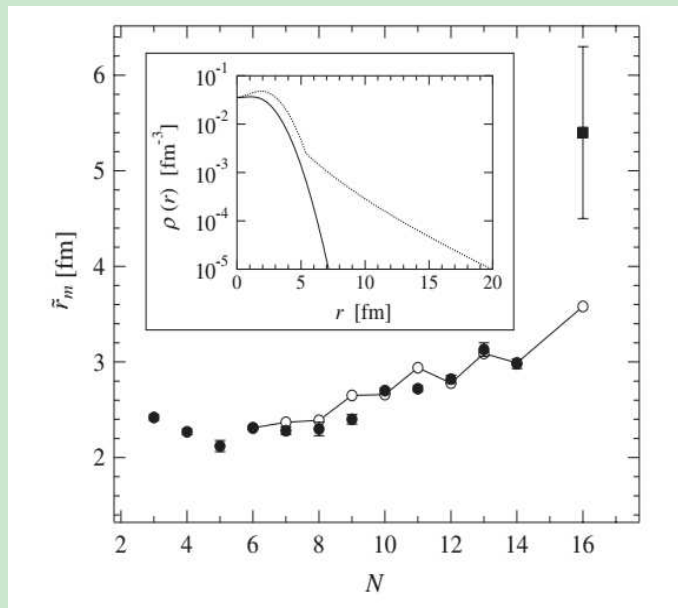
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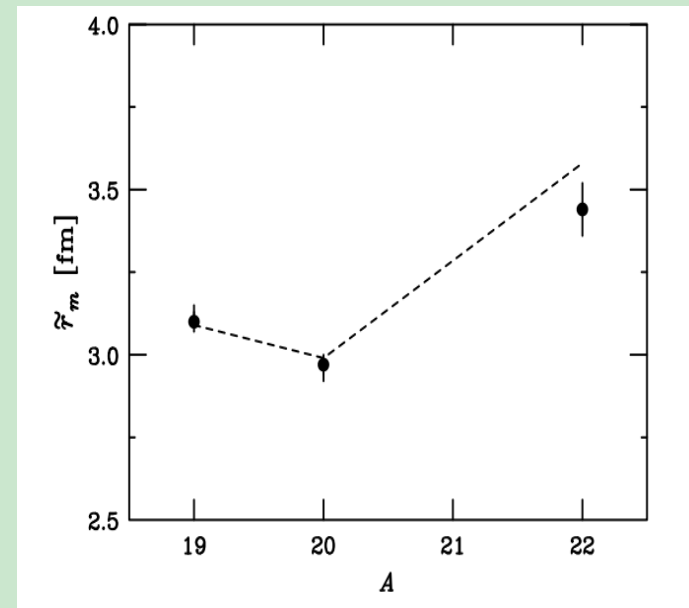
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$$R_m = 3.44 \pm 0.08 \text{ fm}$$

Y. Togano, et al, *Phys. Lett. B* **761**, 412-418 (2016)

The analyzing of those two papers show the valence neutron of ^{22}C is dominated by $2s_{1/2}$.

Background

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① Theoretical prediction: three-body model, shell model approach, effective field theory: $2s_{1/2}$.

- 📄 W. Horiuchi and Y. Suzuki, *Phys. Rev. C* **72**, 034311 (2006); H. T. Fortune and R. Sherr, *Phys. Rev. C* **85**, 027303 (2012);
- 📄 K. Tanaka, et al, *Phys. Rev. Lett.* **104**, 062701 (2010); T. Inakura, et al, *Phys. Rev. C* **89**, 064316 (2014);
- 📄 L. A. Souza, E. Garrido, and T. Frederico, *Phys. Rev. C* **94**, 064002 (2016).

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② Halo nuclei: large spatial distributions, contribution of continuum states and deformation effects. A self-consistent method to describe halo structure: DRHBc model.

- 📄 Jie Meng, Shan-Gui Zhou, *J. Phys. G: Nucl. Phys.* **42**, 093101 (2015);
- 📄 Jie Meng and Peter Ring, *Phys. Rev. Lett.* **77**, 3396 (1996); Jie Meng, *Nucl. Phys. A* **635**, 3 (1998);
- 📄 Shan-Gui Zhou, Jie Meng, Peter Ring, *Phys. Rev. C* **68**, 034323 (2003);
- 📄 Shan-Gui Zhou, Jie Meng Reter Ring and En-Guang Zhao, *Phys. Rev. C* **82**, 011301 (2010)(R);
- 📄 Lu-Lu Li, Jie Meng, En-Guang Zhao and Shan-Gui Zhou, *Phys. Rev. C* **85**, 024312 (2012);

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Covariant density functional theory

⊙ Lagrange density:

$$\begin{aligned}
 \mathcal{L} &= \mathcal{L}_N + \mathcal{L}_\sigma + \mathcal{L}_\omega + \mathcal{L}_\rho + \mathcal{L}_A + \mathcal{L}_I \\
 &= \bar{\psi}(i\gamma^\mu \partial_\mu - M)\psi + \frac{1}{2}\partial_\mu \sigma \partial^\mu \sigma - U(\sigma) - g_\sigma \bar{\psi} \sigma \psi \\
 &\quad - \frac{1}{4}\Omega_{\mu\nu} \Omega^{\mu\nu} + \frac{1}{2}m_\omega^2 \omega_\mu \omega^\mu - g_\omega \bar{\psi} \gamma^\mu \omega_\mu \psi \\
 &\quad - \frac{1}{4}\vec{R}_{\mu\nu} \vec{R}^{\mu\nu} + \frac{1}{2}m_\rho^2 \vec{\rho}_\mu \vec{\rho}^\mu - g_\rho \bar{\psi} \gamma^\mu \vec{\rho}_\mu \vec{\tau} \psi \\
 &\quad - \frac{1}{4}F_{\mu\nu} F^{\mu\nu} - e\bar{\psi} \frac{1 - \tau_3}{2} \gamma^\mu A_\mu \psi.
 \end{aligned}$$

$$U(\sigma) = \frac{1}{2}m_\sigma^2 \sigma^2 + \frac{g_2}{3} \sigma^3 + \frac{g_3}{4} \sigma^4.$$

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$$U(\sigma) = \frac{1}{2}m_\sigma^2\sigma^2 + \frac{g_2}{3}\sigma^3 + \frac{g_3}{4}\sigma^4.$$

Equation of motion (with time reversal invariance):

$$[-\Delta + \partial_\sigma U(\sigma)] = -g_\sigma\rho_s;$$

$$(-\Delta + m_\omega^2)\omega^0 = g_\omega\rho_\nu;$$

$$(-\Delta + m_\rho^2)\rho_3^0 = g_\rho\rho_3;$$

$$-\Delta A^0 = e\rho_c;$$

Density and current:

$$\rho_s(\mathbf{r}) = \bar{\psi}\psi, \rho_\nu(\mathbf{r}) = \bar{\psi}\gamma_\nu\psi,$$

$$\rho_3(\mathbf{r}) = \bar{\psi}\gamma_\nu\tau_3\psi, \rho_c(\mathbf{r}) = \bar{\psi}\frac{1-\tau_3}{2}\gamma_\nu\psi.$$

$$(\boldsymbol{\alpha} \cdot \mathbf{p} + \beta(M + S) + V)\psi_i(\mathbf{x}) = \varepsilon_i\psi_i(\mathbf{x}).$$

Deformed relativistic Hartree-Bogoliubov model

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- Dirac Hartree-Bogoliubov equation:

$$\int d^3\mathbf{r}' \begin{pmatrix} h_D - \lambda & \Delta \\ -\Delta^* & -h_D + \lambda \end{pmatrix} \begin{pmatrix} U_k \\ V_k \end{pmatrix} = E_k \begin{pmatrix} U_k \\ V_k \end{pmatrix}.$$

Dirac Hamiltonian: $h_D(\mathbf{r}, \mathbf{r}') = \boldsymbol{\alpha} \cdot \mathbf{p} + V(r) + \beta[M + S(r)]$.

Scalar and vector potential: $S(\mathbf{r}) = g_\sigma \sigma(\mathbf{r})$; $V(\mathbf{r}) = g_\omega \omega^0 + g_\rho \tau_3 \rho^0 + e \frac{1-\tau_3}{2} A^0$.

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- Quasi particle wave function (Dirac spinor) is extended in terms of spherical Dirac spinors,

$$U_k(\mathbf{r}sp) = \sum_{n\kappa} u_{k,(n\kappa)}^{(m)} \phi_{n\kappa m}(\mathbf{r}sp), \quad V_k(\mathbf{r}sp) = \sum_{n\kappa} v_{k,(n\kappa)}^{(m)} \bar{\phi}_{n\kappa m}(\mathbf{r}sp).$$

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- For axially deformed nuclei with spatial reflection symmetry, we represent the potential and densities in terms of Legendre polynomials,

$$f(\mathbf{r}) = \sum_{\lambda} f_{\lambda}(r) P_{\lambda}(\cos \theta), \quad f_{\lambda}(r) = \frac{2\lambda + 1}{2} \int_{-1}^1 d(\cos \theta) f(\mathbf{r}) P_{\lambda}(\cos \theta), \quad \lambda = 0, 2, 4, \dots$$

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- Density dependent pairing force of zero range:

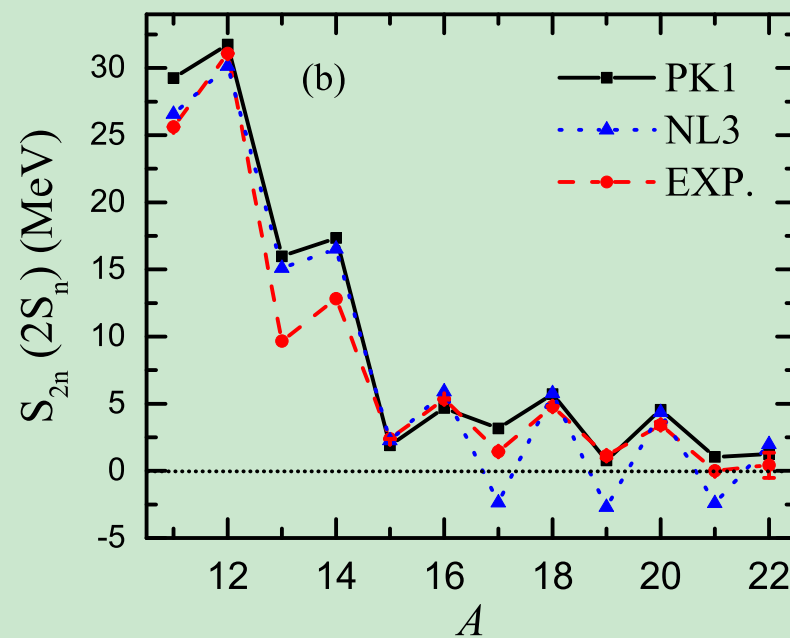
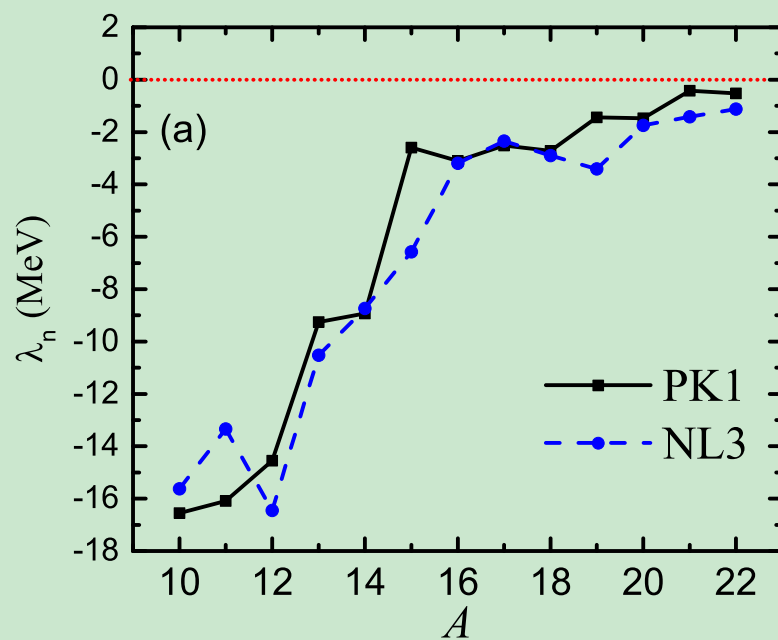
$$V^{\text{pp}}(\mathbf{r}_1, \mathbf{r}_2) = \frac{1}{2} V_0 (1 - P^{\sigma}) \delta(\mathbf{r}_1 - \mathbf{r}_2) \left(1 - \frac{\rho(\mathbf{r}_1)}{\rho_{\text{sat}}} \right).$$

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Carbon isotopes $^{10-22}\text{C}$ properties

Fermi level and neutron separation energy are plotted as a function of mass number.

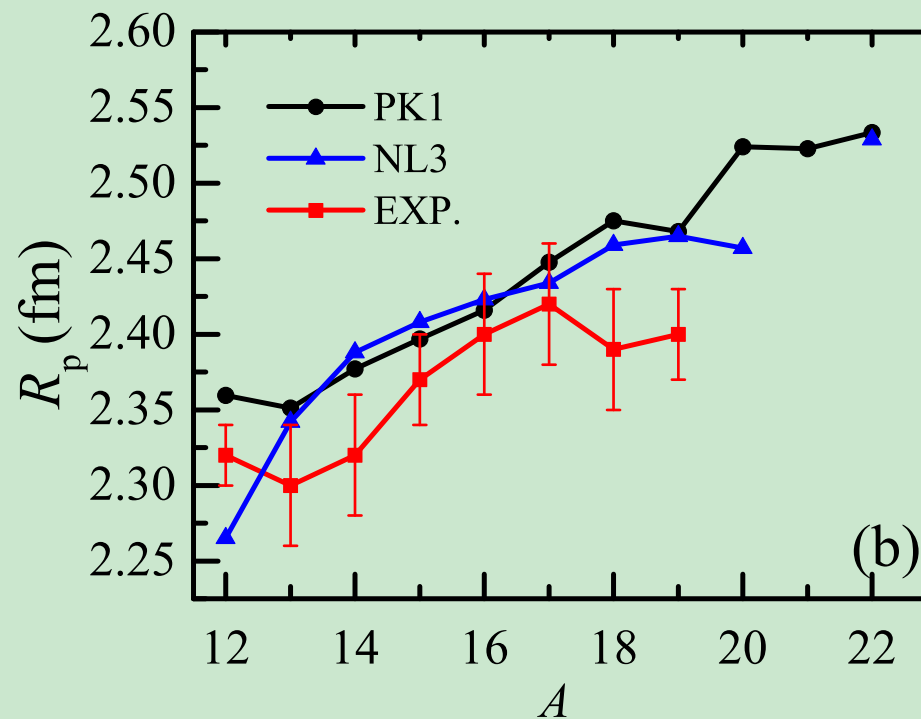
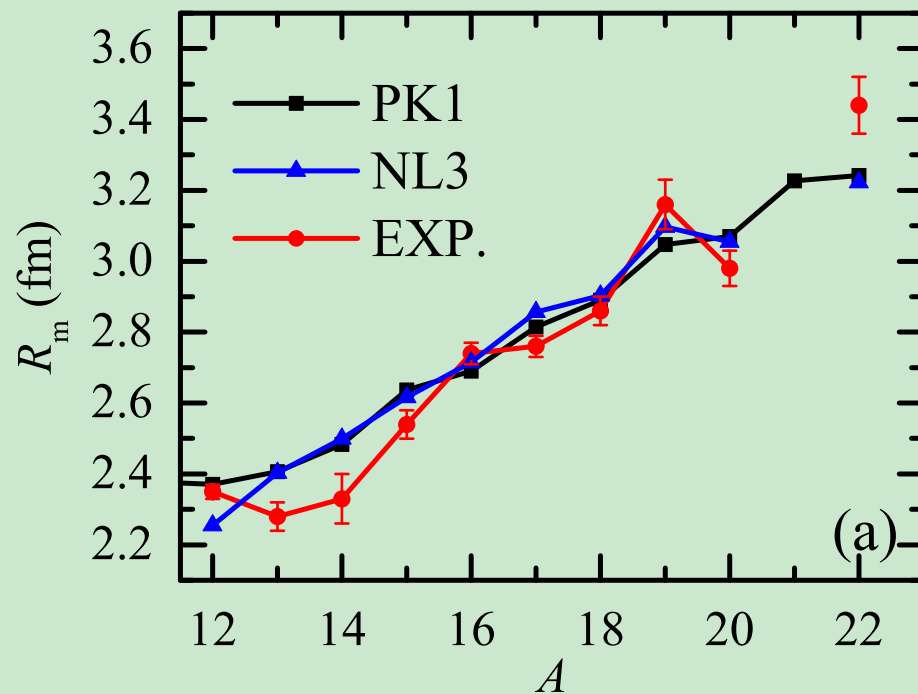


Experimental data are taken from

 G. Audi, M. Wang et al. *China Physics C* **36**, 1287 (2012).

Carbon isotopes $^{10-22}\text{C}$ properties

Root mean square radii R_m and proton radii R_p are plotted as a function of nucleon number A .

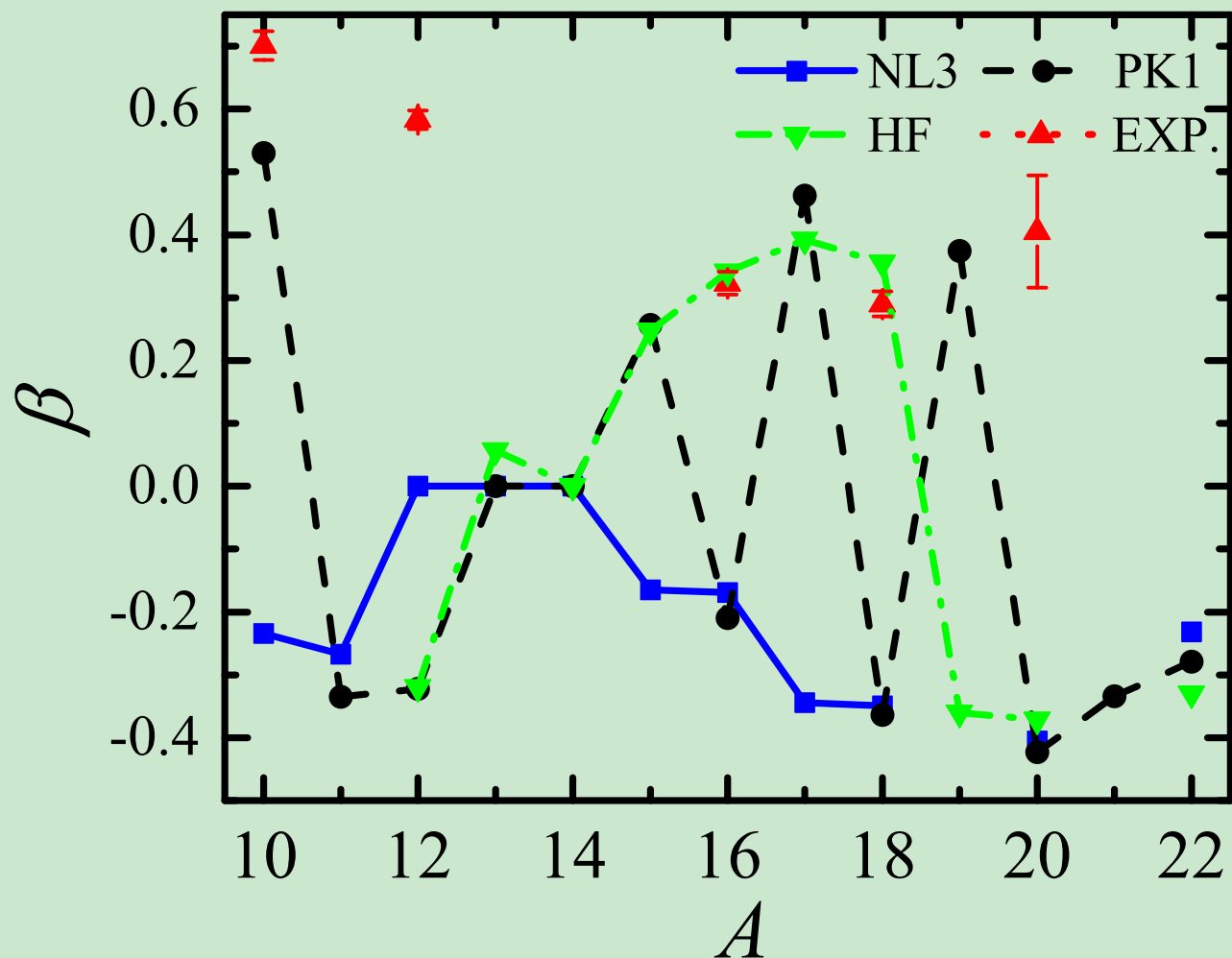


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- 📄 Y. Togano et al., *Phys. Lett. B* **761** 412-418 (2016).
- 📄 H. T. Fortune, *Phys. Rev. C* **94** 064307 (2016).

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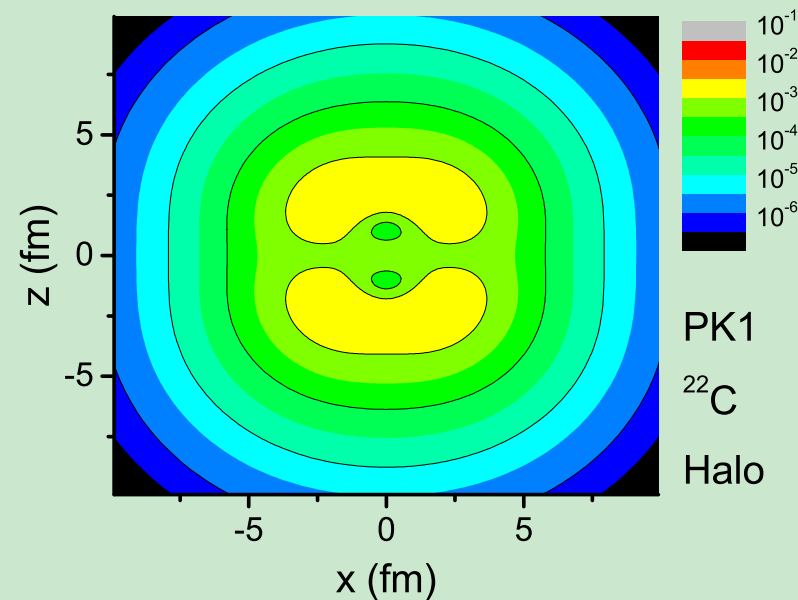
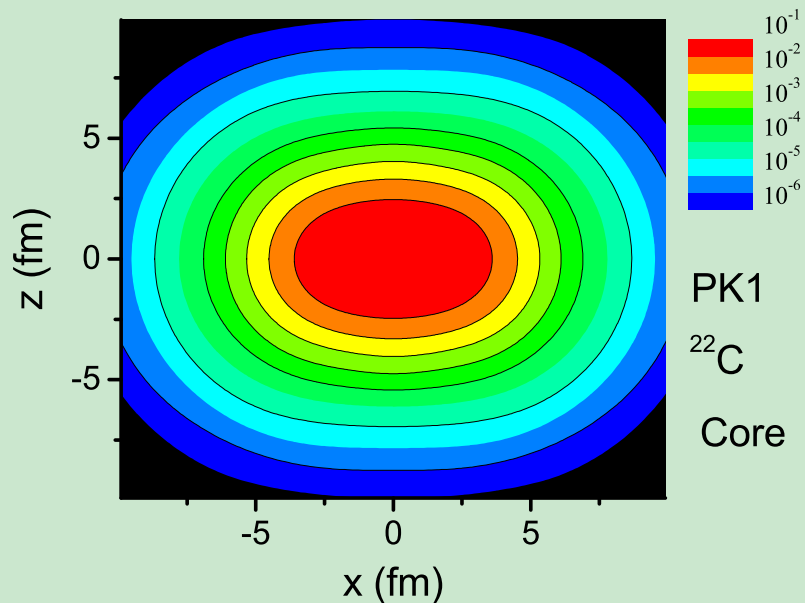
Quadrupole deformation of carbon isotopes:



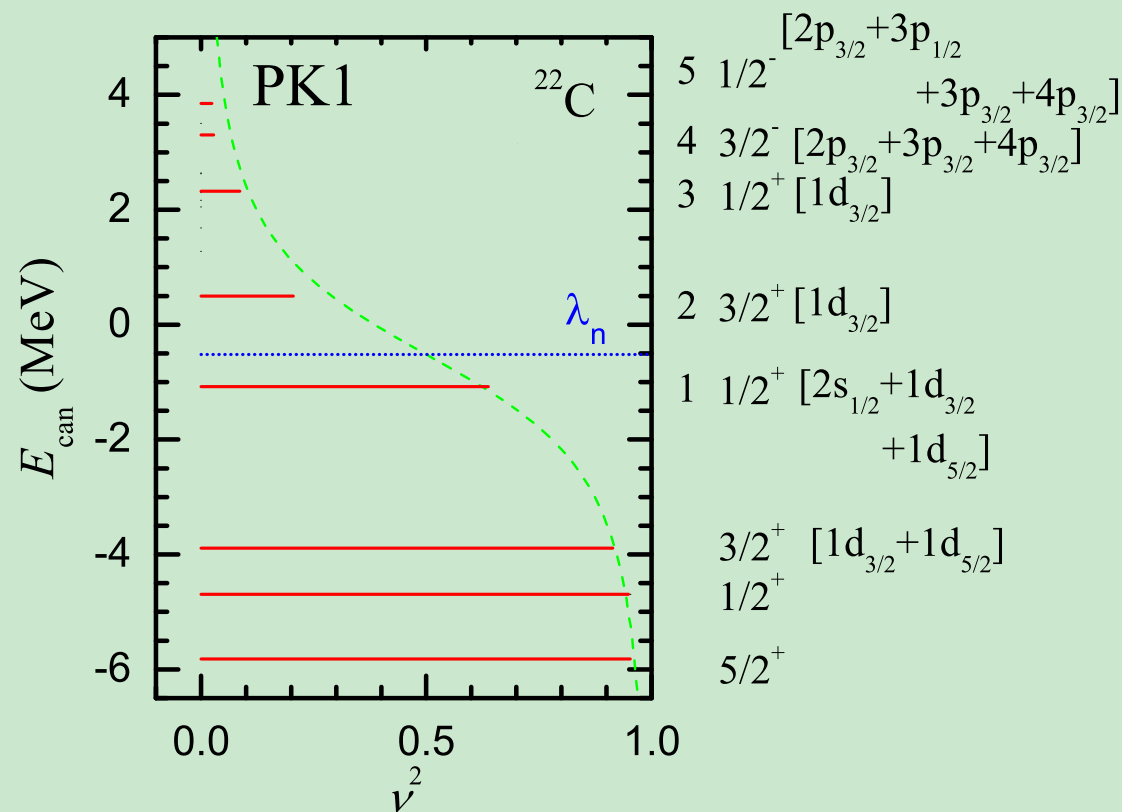
The experimental data are taken from

 B.Pritychenko et al., *Atomic Data and Nuclear Data Tables* **107** 1 (2016).

^{22}C : Halo structure



PK1: $R_m = 3.24$ fm, $\beta_{20} = -0.28$, $S_{2n} = 0.84$ MeV.
Exp.: $R_m = 3.44 \pm 0.08$ fm, $S_{2n} = 0.42 \pm 0.94$ MeV.

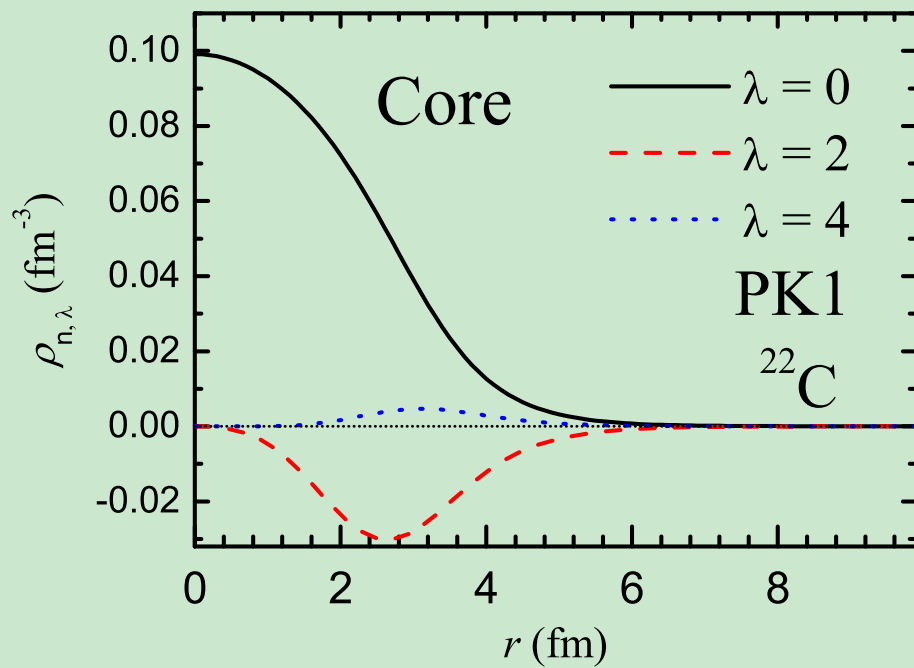


Core: $E_{\text{can}} < -3$ MeV; Halo: $E_{\text{can}} > -2$ MeV.

^{22}C : Halo structure

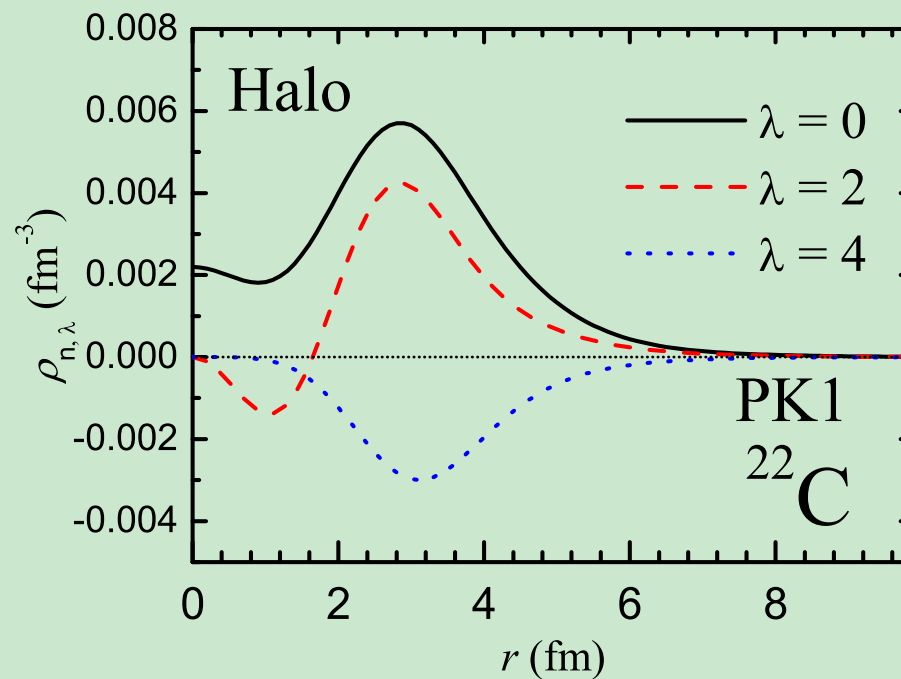
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Spherical, quadrupole and hexadecapole component of core density.



oblate core

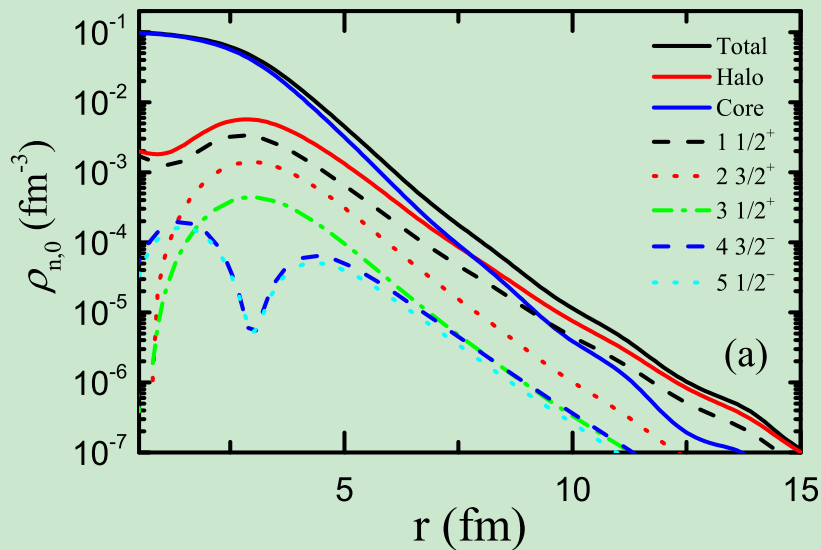
Spherical, quadrupole and hexadecapole component of halo density.



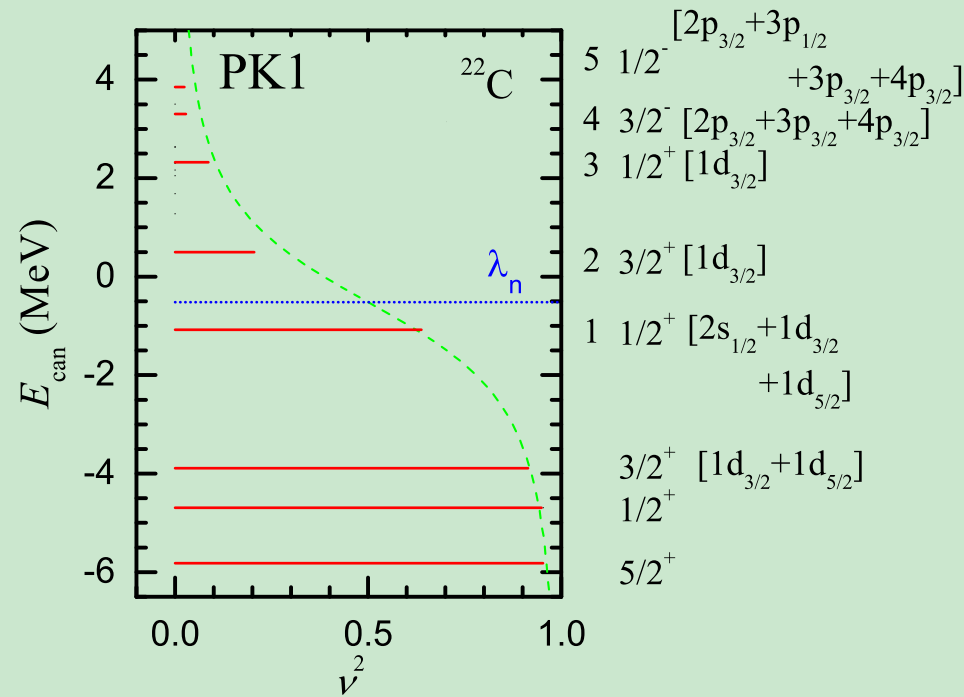
prolate halo

^{22}C : Halo structure

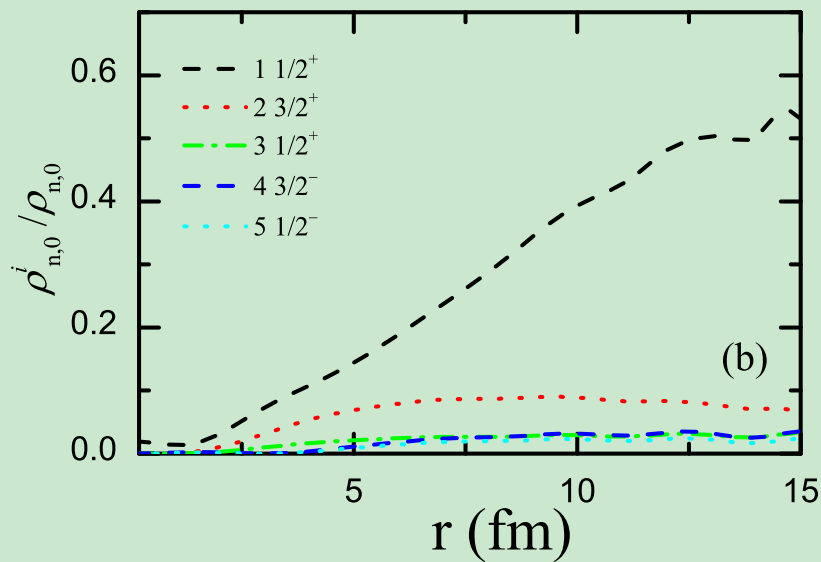
Total density, Core and halo, neutron orbitals.



$(1-\frac{1}{2}^+)$ near the fermi surface gives a most contribution the halo of ^{22}C .



Relative contribution of neutron orbitals to total density.

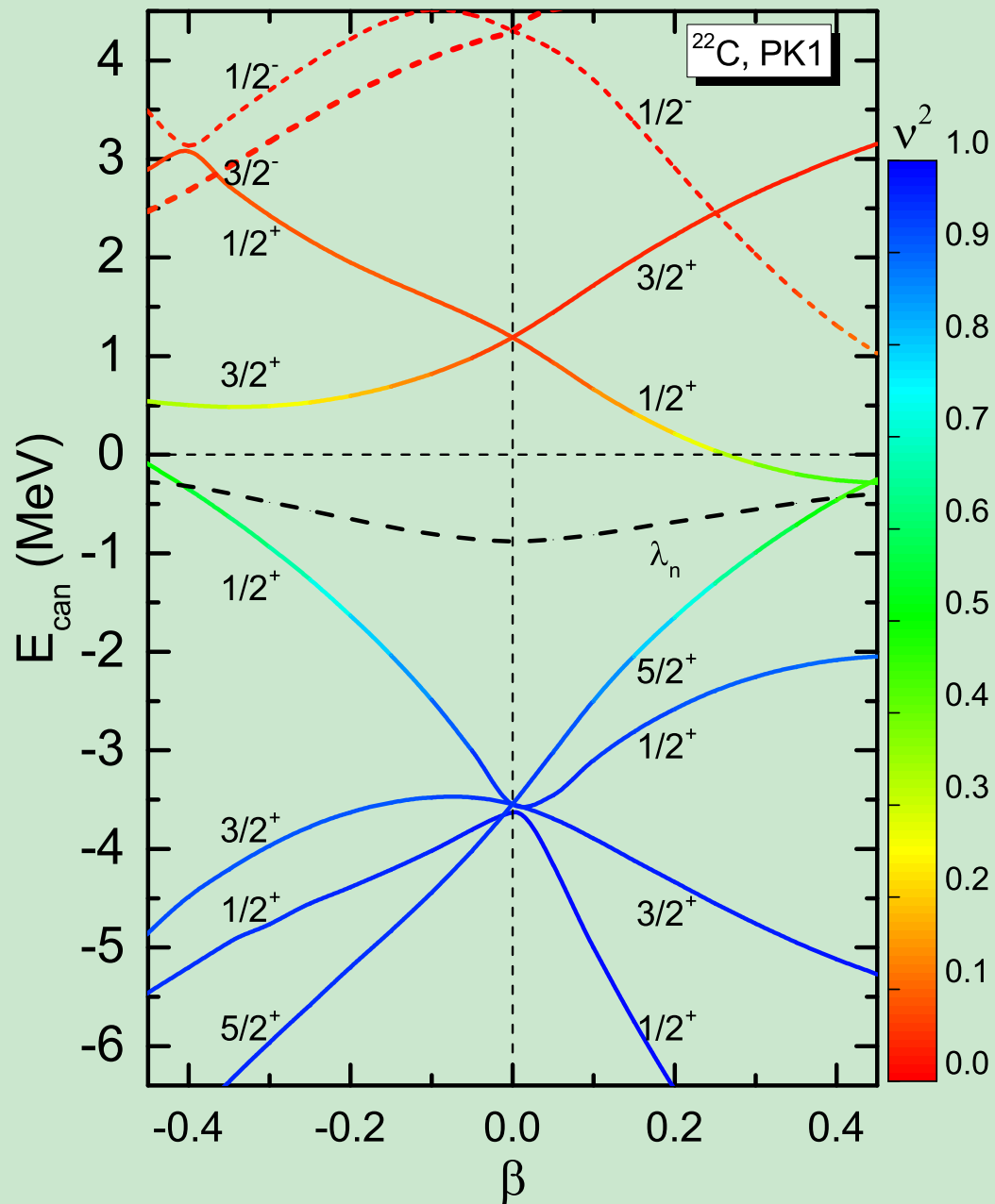


Spherical components low $j(s, p)$ -orbitals

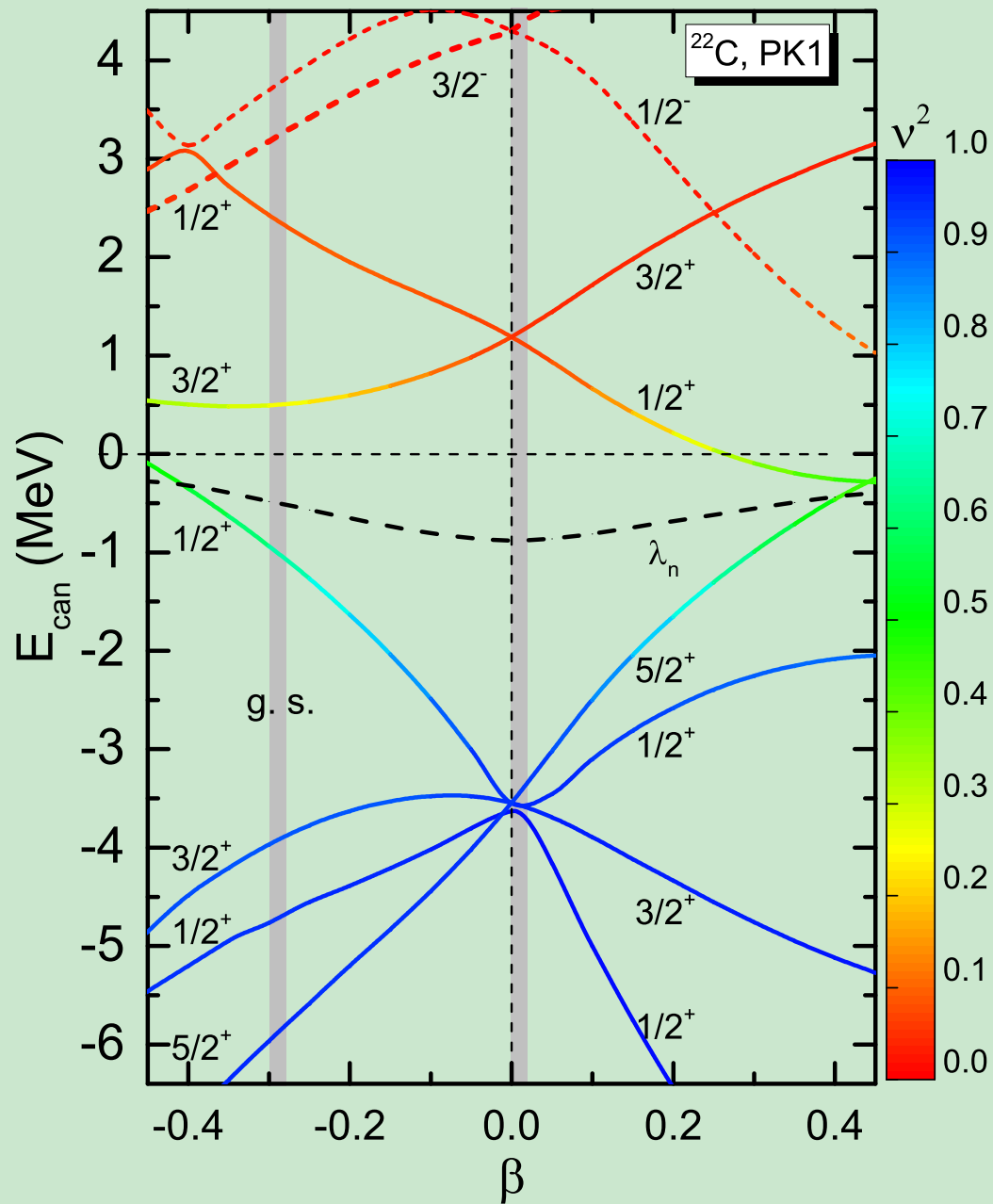
$2s_{1/2}(0.13/0.63)$: spherical halo;

$1d_{5/2}(0.45/0.63)$: prolate shape for halo.

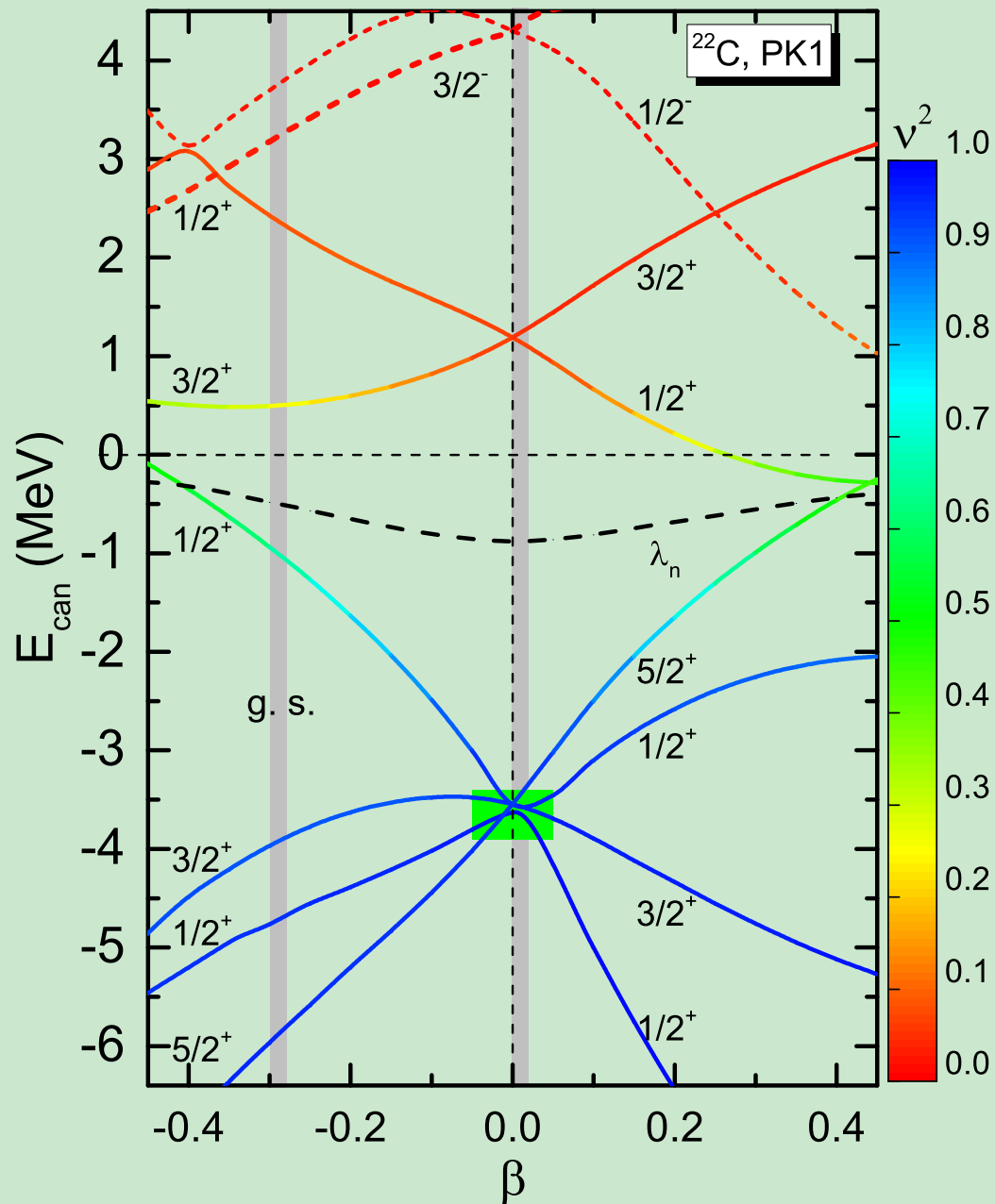
Constraint calculation of ^{22}C



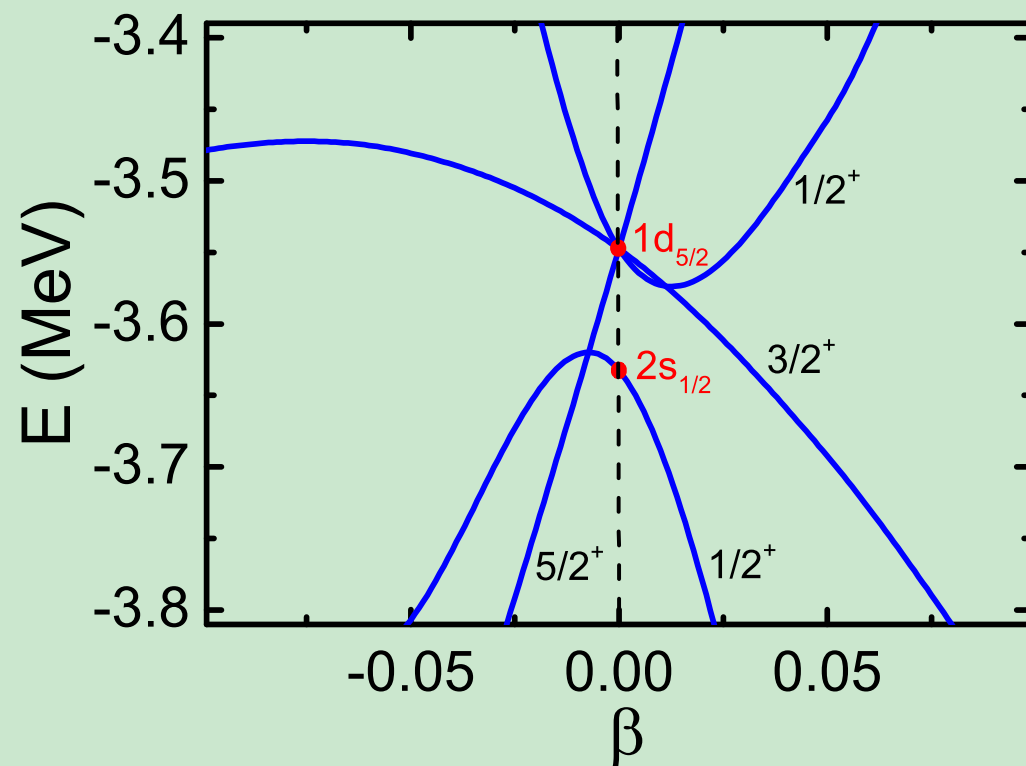
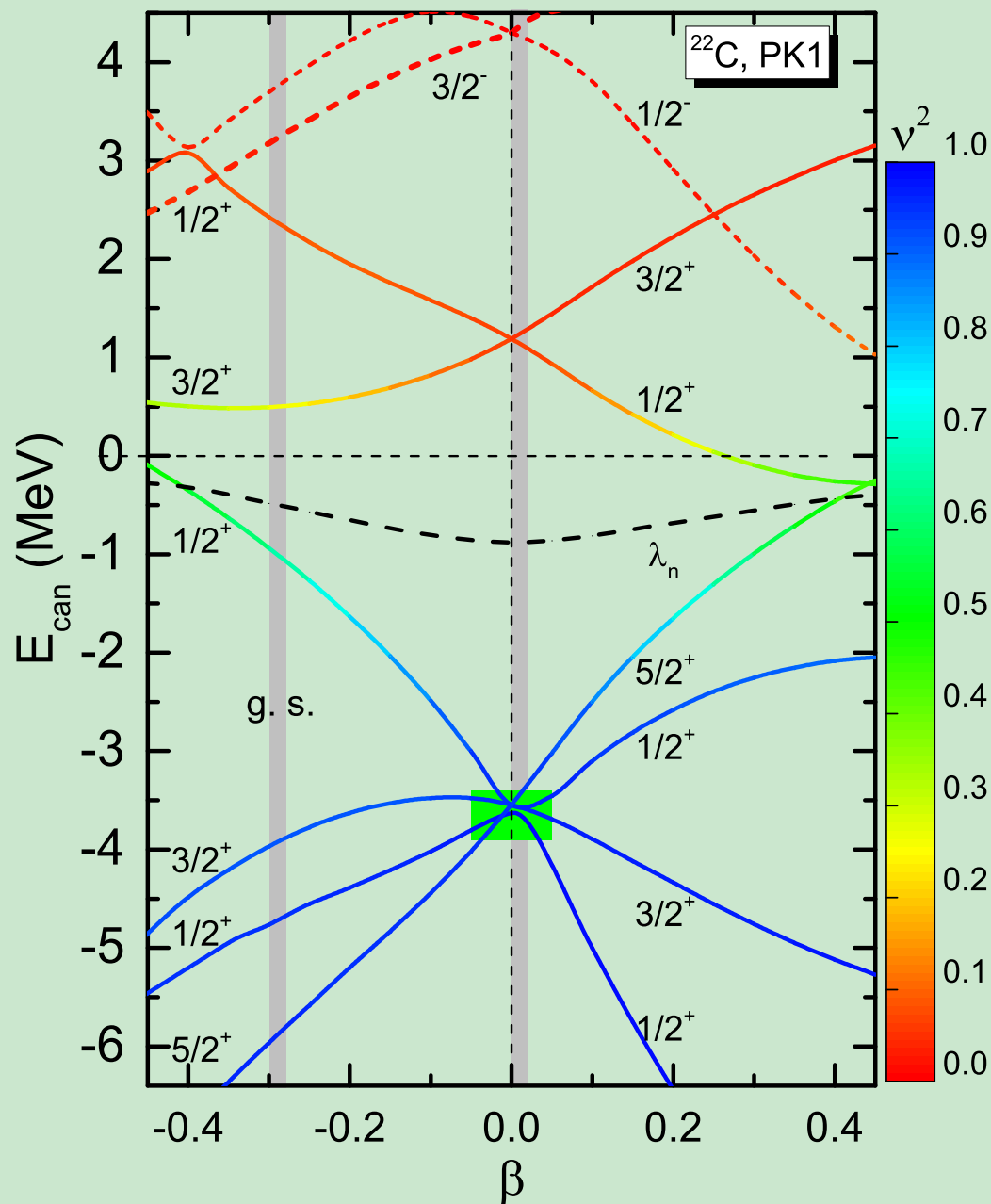
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$2s_{1/2}$ is lower than $1d_{5/2}$. ^{11}Li , ^{11}Be , and ^{14}Be , the mixing of $(2s_{1/2})^2$ and $(1p_{1/2})^2$.

A. Ozawa, et al, *Phys. Rev. Lett.* **84**, 5493 (2000)

Takaharu Otsuka, et al, *Phys. Rev. Lett.* **87**, 082502 (2001)

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Summary

- ① Description of the bulk properties of Carbon isotopes with DRHBc model.
- ② The deformed halo structure of ^{22}C .
 - ① Deformation effect is important for the ^{22}C halo;
 - ② shape decoupling: oblate core and prolate halo;
 - ③ The main contribution of the halo is the $\frac{1}{2}^+$ level close to fermi surface, whose main spherical components are $2s_{1/2}$, $1d_{5/2}$ and $1d_{3/2}$ with the amplitude of 0.14, 0.43, and 0.06;
 - ④ Orbitals with low j orbitals, $2s_{1/2}$ component give a spherical halo, gives the halo structure of ^{22}C , but a large component of $1d_{5/2}$ leads to a prolate shape.
 - ⑤ $2s_{1/2}$ is lower than $1d_{5/2}$, so the percentage of $2s_{1/2}$ is only about 20% for the valence neutron orbitals.

Thanks for your attention.