

# Activities and Collaborations of Division of Particle Physics

CCS at U. Tsukuba / RIKEN AICS

Yoshinobu Kuramashi



# Plan of Talk

- Members
- Machines in CCS
- Introduction to Lattice QCD
- Hadron Mass Calculation
- Two Approaches for Nuclei in Lattice QCD
- Other Primary Research Subjects
- Collaborations
- Future Plan
- Summary



# Members

- Yoshinobu Kuramashi [P], Leader
- Naruhito Ishizuka [AP]
- Tomoteru Yoshié 【AP】
- Noriyoshi Ishii [AP]
- Hidekatsu Nemura [AP]
- Yusuke Taniguchi [L]
- + 3 postdocs
- Sinya Aoki [Visiting Professor]
- Kazuyuki Kanaya [P(Collaborative Fellow)]



# Machines in CCS





What is Elementary Particle Physics?

Questions in history of mankind

- What is the smallest component of matter?
- What is the most fundamental interaction?



### Elementary Particle Known to Date





### **Fundamental Interactions**

### force relative strength gauge boson quantum theory

Strong	1	Gluon	QCD	
EM	0.01	Photon	QED	
Weak	0.00001	Weak Boson	Weinberg-Salam	
Gravity	10 <sup>-40</sup>	Graviton	Superstring(?)	

What is strong interaction?



### **Strong Interaction**





### Lattice QCD

QCD Lagrangian = first principle

$$\mathcal{L} = \frac{1}{4} F_{\mu\nu} F_{\mu\nu} + \sum_{q=u,d,s,c,b,t} \bar{q} \left[ \gamma_{\mu} (\partial_{\mu} - igA_{\mu}) + m_{q} \right] q$$

Only coupling const. g and quark masses m<sub>a</sub> are free parameters



Too strong to investigate with perturbative analysis

⇒ nonperturbative analysis with numerical method based on first pringiple



### **Numerical Method**

Path integral on discretized 4D (3D-space + 1D-time) lattice

$$\langle \mathcal{O}[A_{\mu}, q, \bar{q}] \rangle = \frac{1}{Z} \int \mathcal{D}A_{\mu} \mathcal{D}q \mathcal{D}\bar{q} \ \mathcal{O}[A_{\mu}, q, \bar{q}] \ \exp\left\{-\int d^4x \mathcal{L}[A_{\mu}, q, \bar{q}]\right\}$$

Similar to partition function in stat. mechanics  $\Rightarrow$  Monte Carlo method

Average over configs. gives expectation value

o quark ▲ gluon

$$\left\langle \mathcal{O}[A_{\mu}, q, \bar{q}] \right\rangle = \frac{1}{N} \sum_{i=1}^{N} \mathcal{O}[A_{\mu}^{(i)}, q^{(i)}, \bar{q}^{(i)}] + O\left(\frac{1}{\sqrt{N}}\right)$$

Statistical error



### **Physical Parameters**

#### Small number of parameters

- 4D volume: V=NX•NY•NZ•NT
- lattice spacing: a (function of g)
- quark mass: m<sub>u</sub>,m<sub>d</sub>,m<sub>s</sub>,...





# Major Systematic Errors

- Finite volume effects
  - ⇒ Enlarge V=NX•NY•NZ•NT
- Finite lattice spacing effects
  - $\Rightarrow$  smaller a
- Quenched approximation (Partial inclusion of weight exp(-∫d<sup>4</sup>xL<sub>QCD</sub>))
  ⇒ 2+1 (m<sub>u</sub>=m<sub>d</sub>≠m<sub>s</sub>) flavor QCD simulation CP-PACS/JLQCD project 00~05
- Chiral extrapolation with artificially heavier m<sub>ud</sub> quark masses (※ Computational cost becomes cheaper for heavier m<sub>ud</sub>)
  - ⇒ Physical point simulation PACS-CS project 06~



One may think of ...

Chiral extrapolation with artificially heavier  $m_{ud}$  quark masses should be a good idea, because computational cost is much cheaper



### **Quark Mass dependence**

PACS-CS 09



Non-trivial curvature toward physical point ⇒ Physical point simulation is necessary



### Various Hadrons

#### Confinement : quark can never be retrieved by itself





### Hadron Mass Calculation

#### Fundamental quantities both in physical and technical senses

#### Physical side

#### Technical side

Hadron correlators in terms of quark fields

 $\left\langle \mathcal{O}_{h}(t)\mathcal{O}_{h}^{\dagger}(0)\right\rangle \overset{t\gg0}{\sim} C\exp\left(-m_{h}t\right) \Rightarrow \operatorname{Extract} \operatorname{m_{h}} \operatorname{by} \operatorname{fit}$ 

Quark line diagrams from Wick contractions





### Hadron Masses in 2+1 Flavor QCD

#### PACS-CS 09

input  $m_{\pi}, m_{K}, m_{\Omega} \Rightarrow m_{u}=m_{d}, m_{s}, a$ 



Consistent within  $2 \sim 3\%$  error bars



# What's Next?

- 1+1+1 ( $m_u \neq m_d \neq m_s$ ) flavor QCD+QED simulation at physical point
  - Electromagnetic (EM) interactions
  - u-d quark mass defferenceK°(ds) —<br/>497.6MeV1%Multi-physics toward precision measurementK⁺(us)
- Hadron-Hadron interactions



493.7MeV



### 1+1+1 Flavor QCD+QED

PACS-CS 12

Isospin symmetry breaking

EM interaction

u-d quark mass difference

 $m_u = m_d \neq m_s \text{ (2+1 flavor)} \Rightarrow m_u \neq m_d \neq m_s \text{ (1+1+1 flavor)}$ 





### u, d, s Quark Masses

#### PACS-CS 12

Physical input:  $m_{\pi^+}(ud)=139.7(15.5) [MeV]$   $m_{K0}(ds)=497.6(8.1) [MeV]$   $m_{K^+}(us)=492.4(8.1) [MeV]$  $m_{\Omega}(sss)$  is fixed at exp. value

exp: 139.6 [MeV] exp: 497.6 [MeV] exp: 493.7 [MeV] exp: 1672.5 [MeV]

Quark masses (MSbar scheme at  $\mu$ =2 GeV):  $m_u$ =2.57(26)(07) [MeV]  $m_d$ =3.68(29)(10) [MeV]  $m_s$ =83.60(58)(2.23) [MeV]

1+1+1 flavor QCD+QED allows individual determination of m<sub>u</sub>,m<sub>d</sub>,m<sub>s</sub>

Two Approaches for Nuclei in Lattice QCD

 Direct construction of nuclei
 Fukugita et al. 95
 Measure correlation of nucleus operators ⇔ same as hadron masses ex. <sup>4</sup>He case

 $\langle \mathcal{O}_{4_{\text{He}}}(t) \mathcal{O}_{4_{\text{He}}}^{\dagger}(0) \rangle \stackrel{t \gg 0}{\sim} C \exp\left(-m_{4_{\text{He}}}t\right) \qquad \Delta E_{4_{\text{He}}} = m_{4_{\text{He}}} - 4m_N$ binding energy

Potential approach

Ishii-Aoki-Hatsuda 07

Measure wave-function of two nucleons  $\Phi(r) \Rightarrow$  extract potential V<sub>C</sub>(r)

$$V_C(r) = E + \frac{1}{2\mu} \frac{\vec{\nabla}^2 \phi(r)}{\phi(r)}$$

Solve Schrödinger eq. with  $V_C(r)$  as input



# Direct Construction of A≤4 Nuclei

Yamazaki-YK-Ukawa 12

2+1 flavor QCD,  $m_{\pi}$ =0.5 GeV (0.14 GeV in nature),  $m_N$ =1.32 GeV

	⁴He	<sup>3</sup> He	NN( <sup>3</sup> S <sup>1</sup> )	NN( <sup>1</sup> S <sub>0</sub> )
Binding energy [MeV]	43(12)(8)	20.3(4.0)(2.0)	11.5(1.1)(0.6)	7.4(1.3)(0.6)
Exp. value [MeV]	28.3	7.72	2.22	0

- Successful construction of light nuclei (<sup>4</sup>He, <sup>3</sup>He, NN(3S1))
- Larger binding energies than exp. values

Heavy quark effects?

<sup>1</sup>S<sub>0</sub> channel is also bound

Physical point simulation is necessary



### **NN** Potential

#### HAL QCD@Lattice 2013

2+1 flavor QCD,  $m_{\pi}$ =0.70, 0.57, 0.41 GeV (0.14 GeV in nature)



Attractive phase shift, though the magnitude is just 10% of exp. value No bound state (He, NN)  $\Leftrightarrow$  inconsistency against the direct method Phase shift becomes smaller, as quark mass decreases  $\Rightarrow$  reproduce exp. values at the physical point ?



# **Other Primary Research Subjects**

Details of research results will be explained in parallel track on Wed.

- Dynamical properties of hadrons such as  $\rho{\rightarrow}\pi\pi$  resonance
  - World's first study of  $\rho{\rightarrow}\pi\pi$  decay width based on phase shift in 2007
  - Extended from 2 flavor to 2+1 flavor QCD at  $m_{\pi}$ =0.30, 0.41 GeV
- Nonperturbative renormalization with a finite volume technique
  - Running coupling constant and quark masses in 2+1 flavor QCD
- Lattice QCD at finite temperature and density
  - Phase structure
  - Thermodynamic properties
  - Use of Wilson-type quarks



Expected phase diagram



# Collaborations

- Collaboration with applied mathematicians and computer scientists in Division of High performance Computing Systems
  - mixed precision nested BiCGStab algorithm for PACS-CS machine

 $\Rightarrow$  Double the performance

- block Krylov subspace algorithms with multiple right-hand sides
  - ⇒ Make 1+1+1 flavor QCD+QED simulation possible
- International/Japan Lattice Data Grid (ILDG/JLDG)
  - ⇒ Overview by Yoshié-san this morning
- Joint Institute for Computational Fundamental Science (JICFuS)
  ⇒ Future plan session on Thu.



### Future Plan

#### Future plan session on Thu.

#### HPCI Strategic Field Program (FY2011~FY2015)

- 2+1 flavor QCD  $\Rightarrow$  1+1+1 flavor QCD+QED
- Direct construction of light nuclei
- Determination of baryon-baryon potentials

PACS-CS/T2K-Tsukuba  $\Rightarrow$  K computer Large scale simulation on 40 times larger lattice at the physical point







# Summary

#### Historical role of PACS-CS/T2K-Tsukuba

- Achievement of physical point simulation
- Beginning of precision measurement with EM and u-d quark mass difference
- One-body study of hadron ⇒ Hadron-hadron interaction including Nuclei

Peak	Machine	Scientific Target
<1TF class	CP-PACS	Development of 2+1 flavor QCD simulation
10TFclass	PACS-CS	Physical point simulation
100TFclass	T2K- Tsukuba	Development of 1+1+1flavor QCD+QED simulation Construction of Nuclei with heavy m <sub>ud</sub>
1PF class 10PF class	HA-PACS K computer	Large scale simulation of 1+1+1 flavor QCD+QED Construction of Nuclei at the physical point