



# Activities and Collaborations

Nuclear Theory Group

Division of Astrophysics and Nuclear Physics

K. YABANA

Group Leader of Nuclear Physics Group and Quantum Condensed Matter Physics

T. NAKATSUKASA

RIKEN Nishina Center, CCS (2014.4-)

## Faculty members of Nuclear Theory Group

Kazuhiro YABANA (professor, group leader)

Jun TERASAKI (assoc. professor, HPCI project, 2011.5-)

Yukio HASHIMOTO (lecturer)

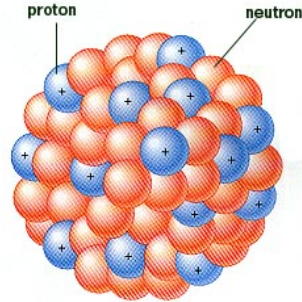
Takashi NAKATSUKASA (2014. 4- , professor, new group leader)

All members affiliated also to Dept. of Physics,  
Graduate School of Pure and Applied Sciences.

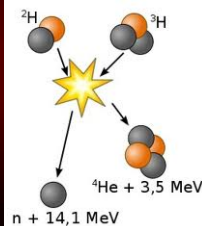
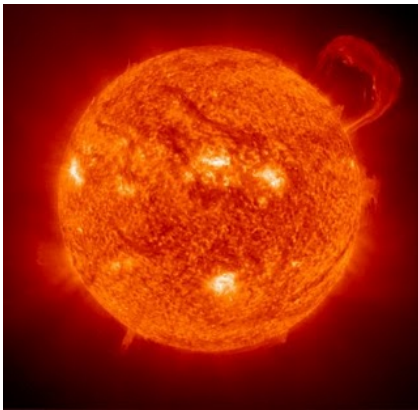
# Atomic nuclei

Quantum many-body system of protons and neutrons  
described by Schrödinger equation

$$\left[ \sum_{i=1}^N -\frac{\hbar^2}{2m} \Delta_i + \sum_{i<j}^N v(x_i, x_j) \right] \Psi(x_1, x_2, \dots, x_N, t) = i\hbar \frac{\partial}{\partial t} \Psi(x_1, x_2, \dots, x_N, t) \quad x = (\vec{r}, \sigma)$$



Fuel of Stars

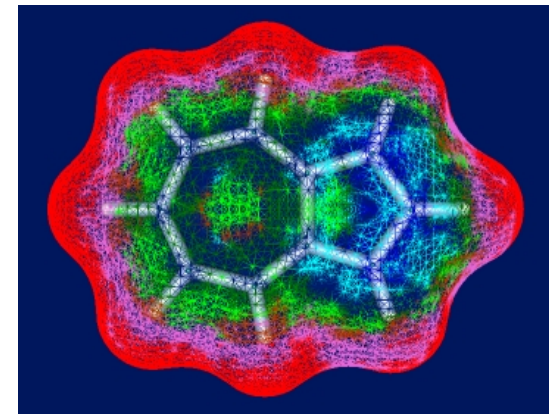


Origin of elements

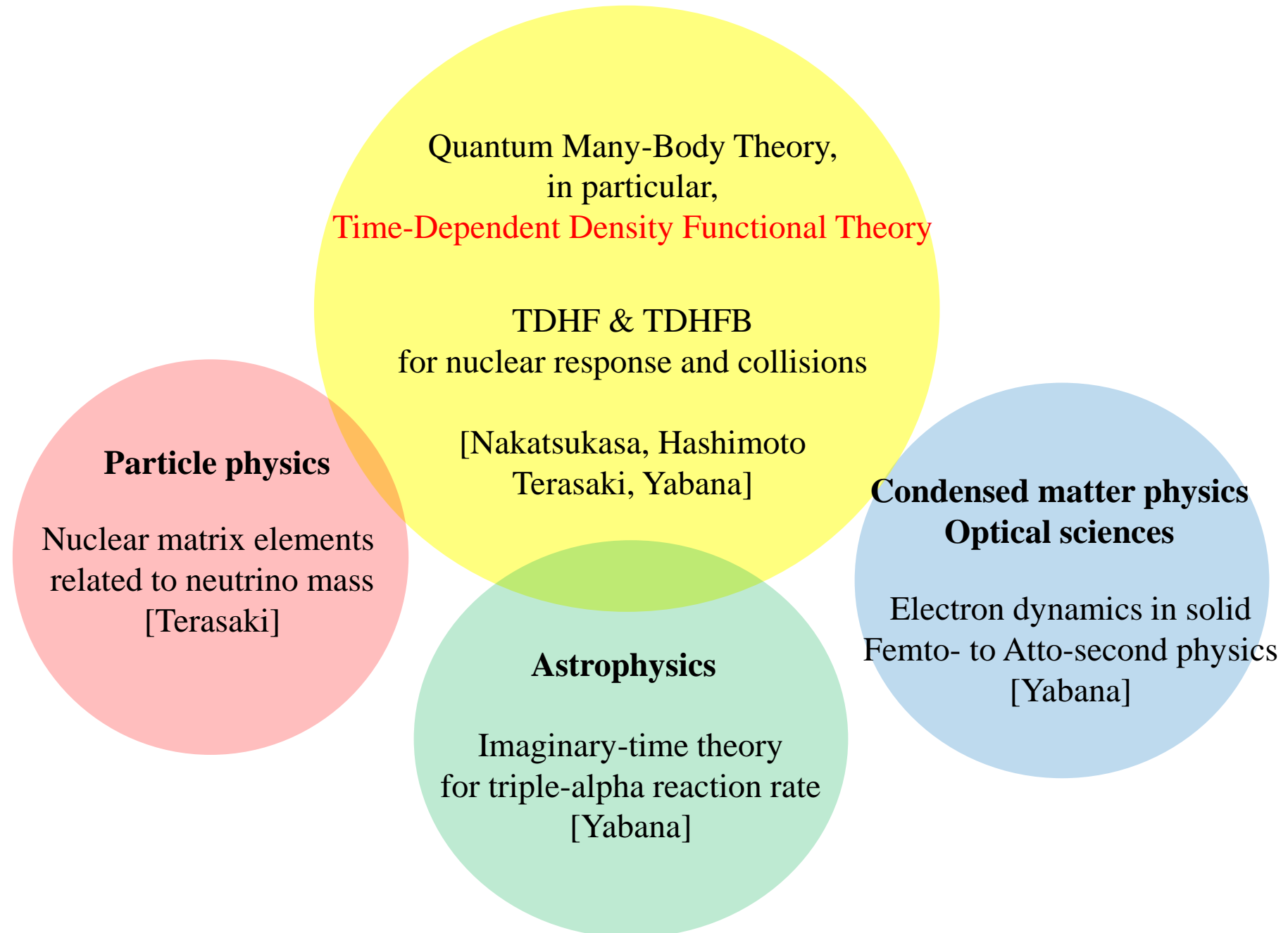
Crab nebula (1054)



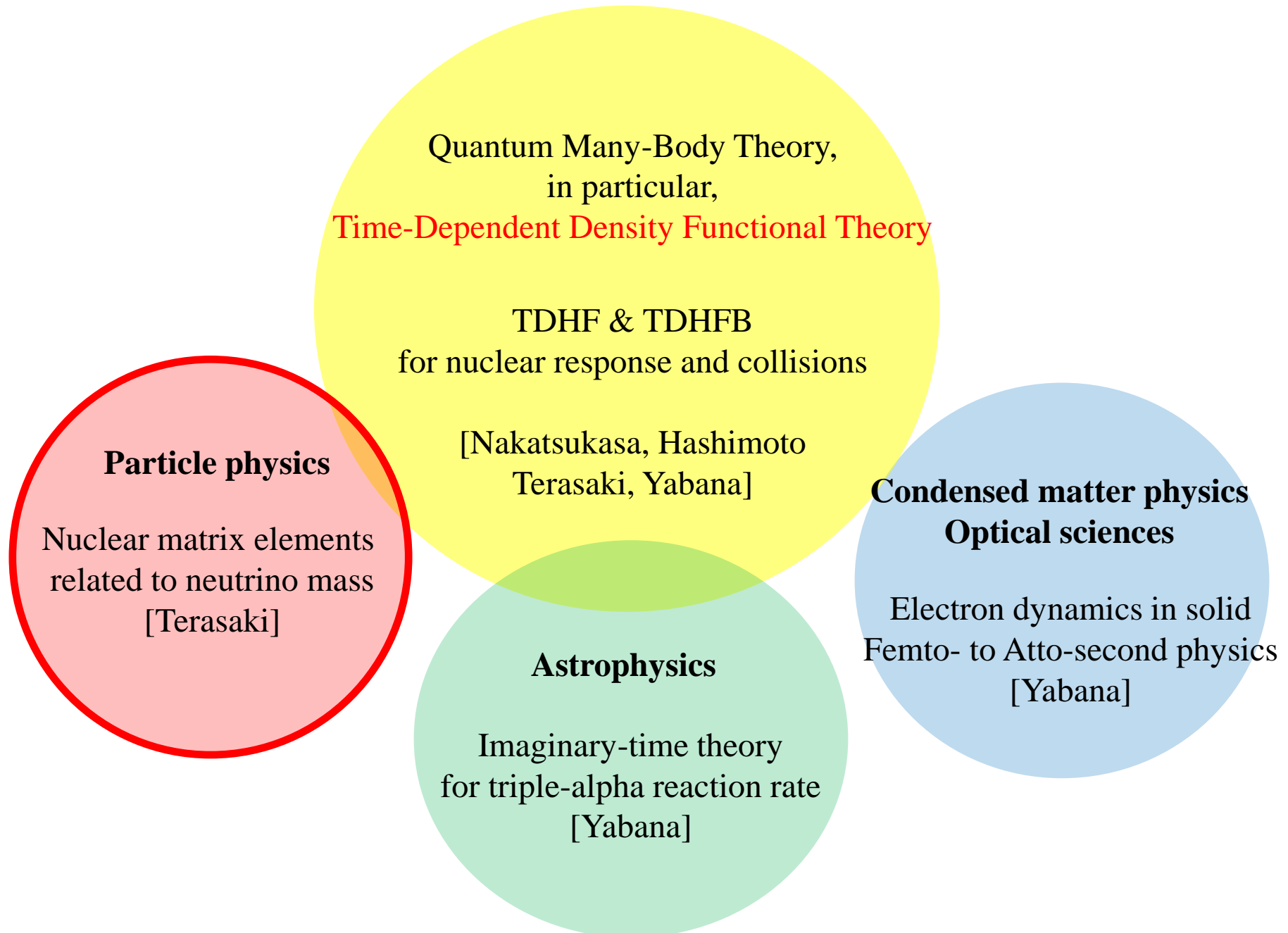
Common features with  
Atoms, molecules, solids as  
Quantum many-body systems



# Researches activities of Nuclear Theory Group in Univ. Tsukuba



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# Nuclear matrix element in neutrinoless double-beta decay

J. Terasaki, Univ. of Tsukuba

## Purpose

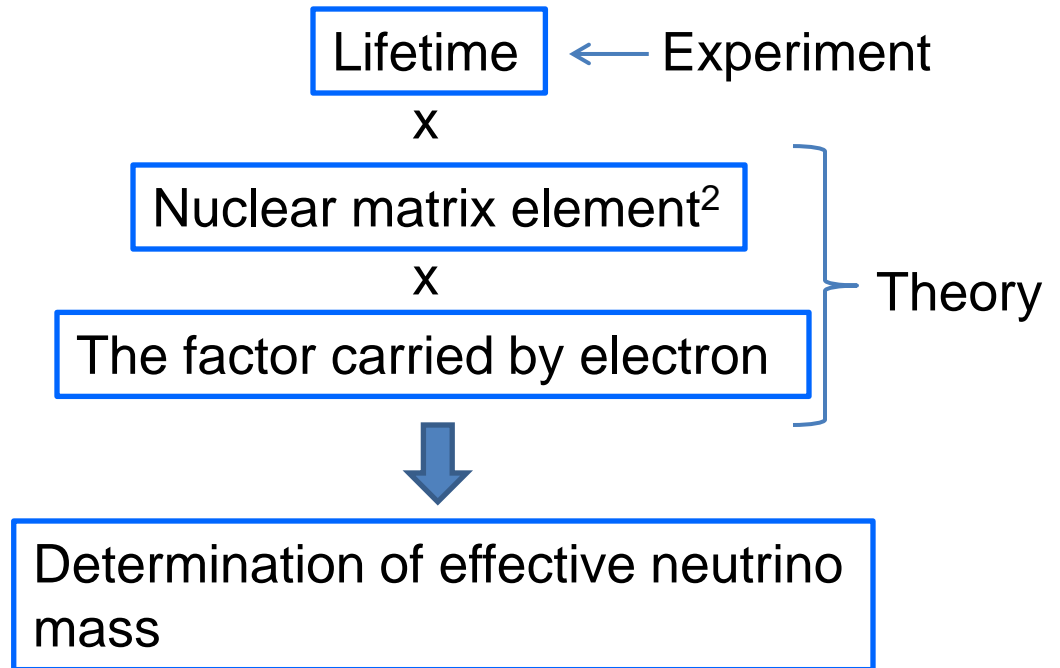
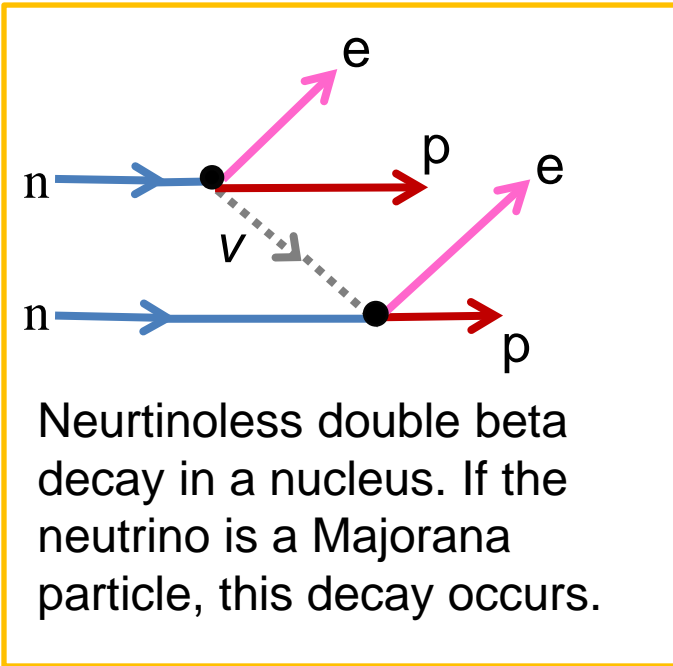
Determination of Effective neutrino mass using the neutrinoless double-beta decay

Neutrino  $\nu$  : very light particle penetrating materials very easily;



It has been proven recently that the neutrino has a mass, but the value of the mass has yet to be known.

# Neutrinoless double beta-decay



*My mission : to provide the nuclear matrix element and the electron factor*

**Physics needs the neutrino mass.**

J.T. PRC **86**, 021301(R) (2012), **87** 024316 (2013)

What needs much effort is the calculation of the nuclear matrix element :

$$\sum_{b_f b_i} \sum_{\alpha \alpha' : p} \sum_{\beta \beta' : n} \left\langle \alpha \alpha' \left| h_+(r_{12}, \bar{E}_a) \left( \boldsymbol{\sigma}(1) \cdot \boldsymbol{\sigma}(2) - \frac{g_V^2}{g_A^2} \tau^+(1) \tau^+(2) \right) \right| \beta \beta' \right\rangle$$

$$\times \langle 0_f^+ | c_{\alpha'}^+ c_{\alpha}^+ | b_f \rangle \langle b_f | b_i \rangle \langle b_i | c_{\beta} c_{\beta'} | 0_i^+ \rangle$$

$\alpha \alpha' \beta \beta'$ : proton or neutron states

$h_+(r_{12}, \bar{E}_a)$ : neutrino potential

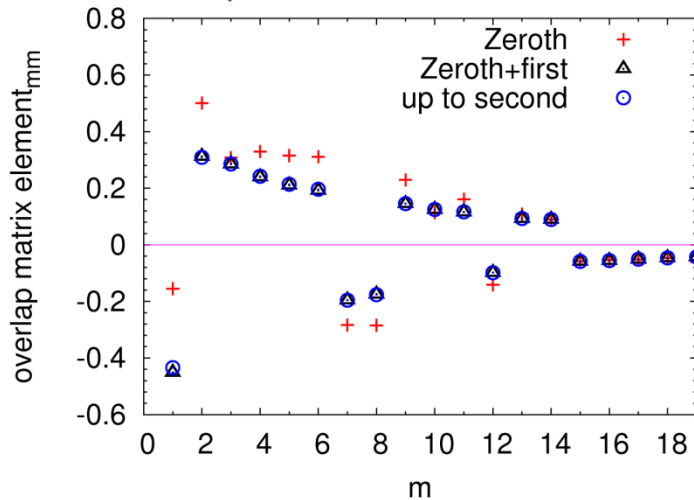
$\bar{E}_a$ : mean energy of the intermediate nuclear states  $b_i$  and  $b_f$

$g_V, g_A$ : vector and axial-vector strength

$\tau^+$  changes  $n$  to  $p$

$0_f^+, 0_i^+$ : nuclear final and initial states, respectively

NEW



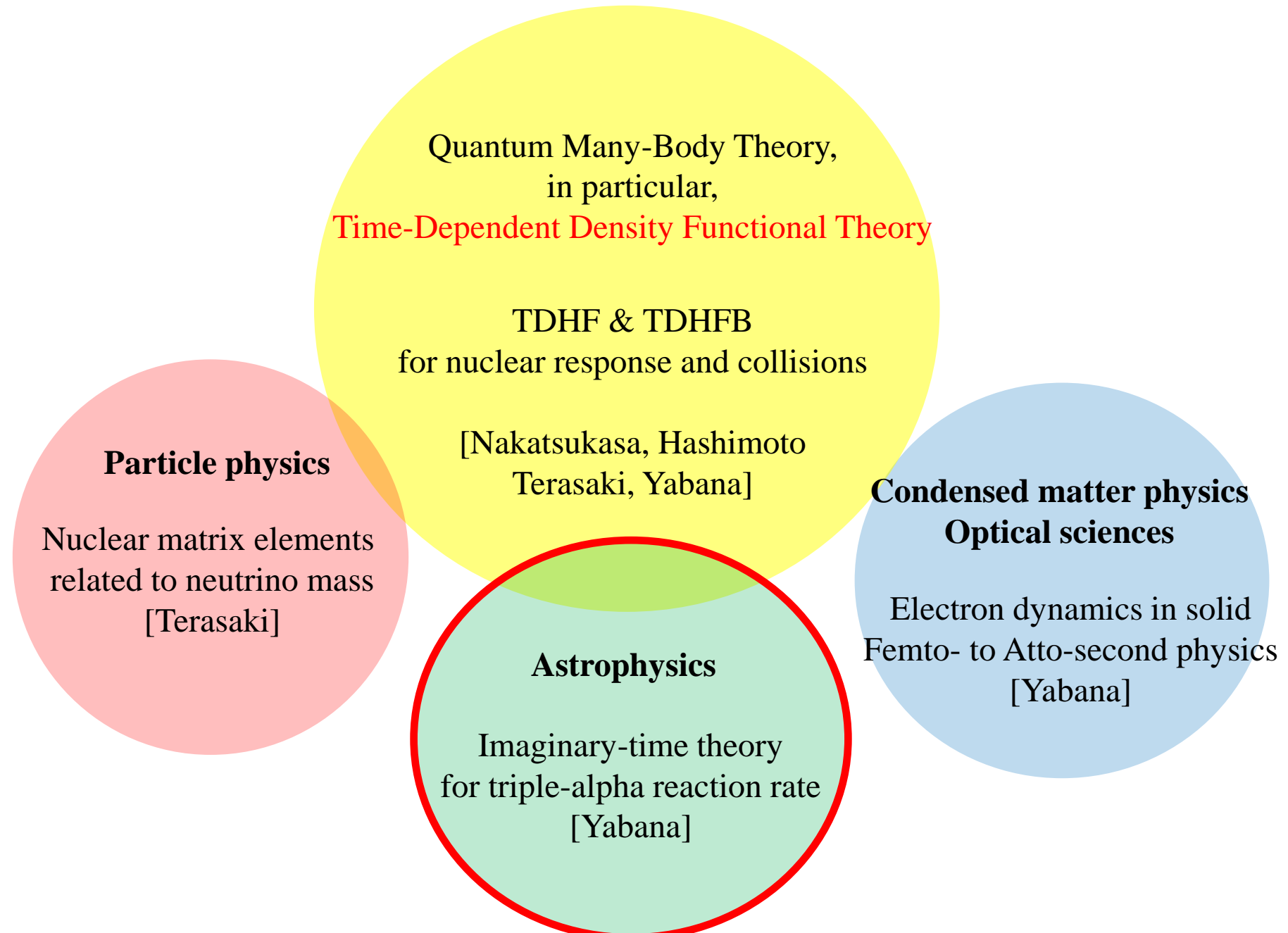
Overlap of two QRPA intermediate states  $\langle b_f | b_i \rangle$  by the expansion method with respect to the operator to bring the QRPA correlations.  $^{26}\text{Mg}$ - $^{26}\text{Si}$  is used for test with SkM\* and the volume pairing.

A referee's comment: "*For the first time the calculation within (like) QRPA is pulled through in full.*"

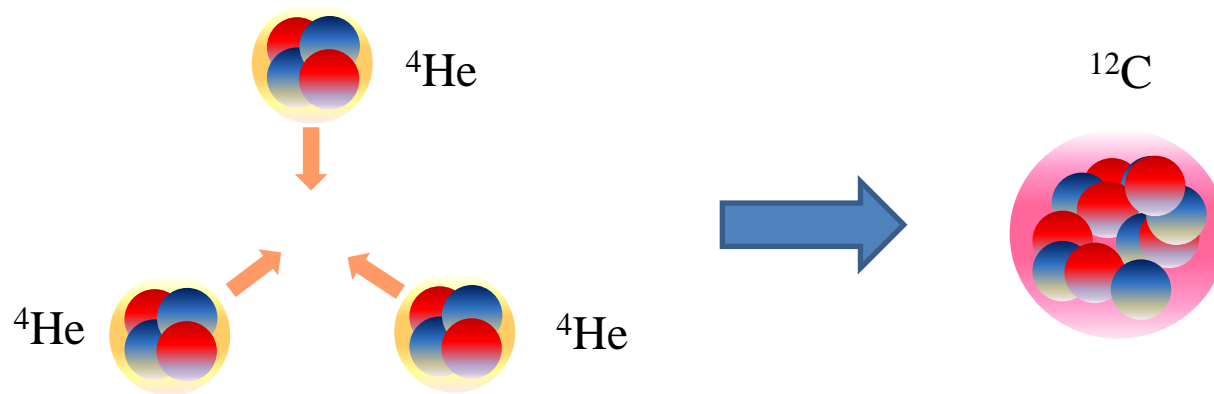
The calculation of the nuclear matrix element of  $^{150}\text{Nd} \rightarrow ^{150}\text{Sm}$  is in progress.



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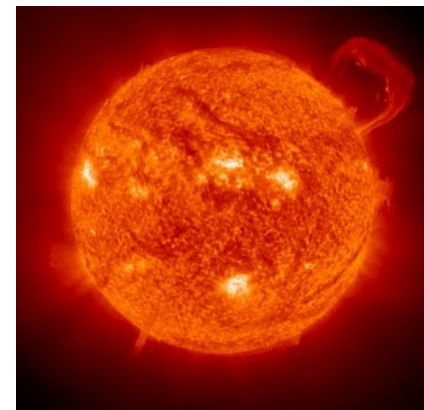
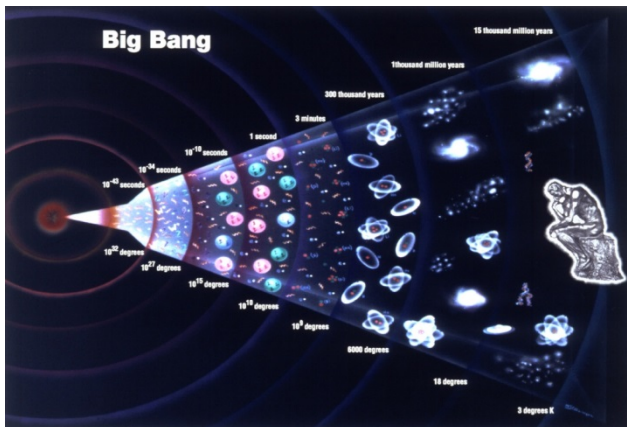


# Triple-alpha reaction to synthesize $^{12}\text{C}$ nucleus



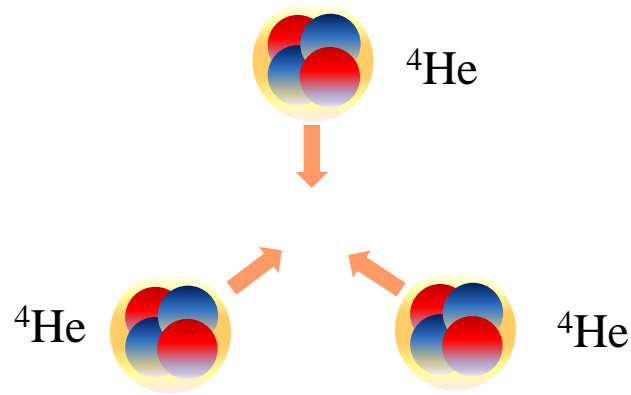
Immediately after the Big Bang, only H, D,  $^3\text{He}$ ,  $^4\text{He}$ , and some Li, Be are synthesized.

All heavy elements are synthesized inside stars through triple-alpha reaction



# Difficulties of triple-alpha reaction rate

- Experiments not possible
- Very small reaction rate due to quantum tunneling nature
- There is no formal scattering theory for charged three particles

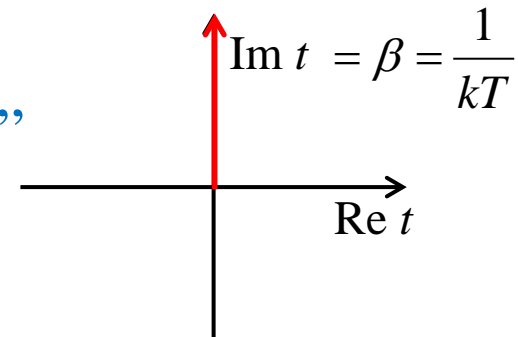


We (believe to) have solved the problem.

K. Yabana, Y. Funaki, Phys. Rev. C85, 055803 (2012).  
T. Akahori, Y. Funaki, K. Yabana, to be accepted soon.

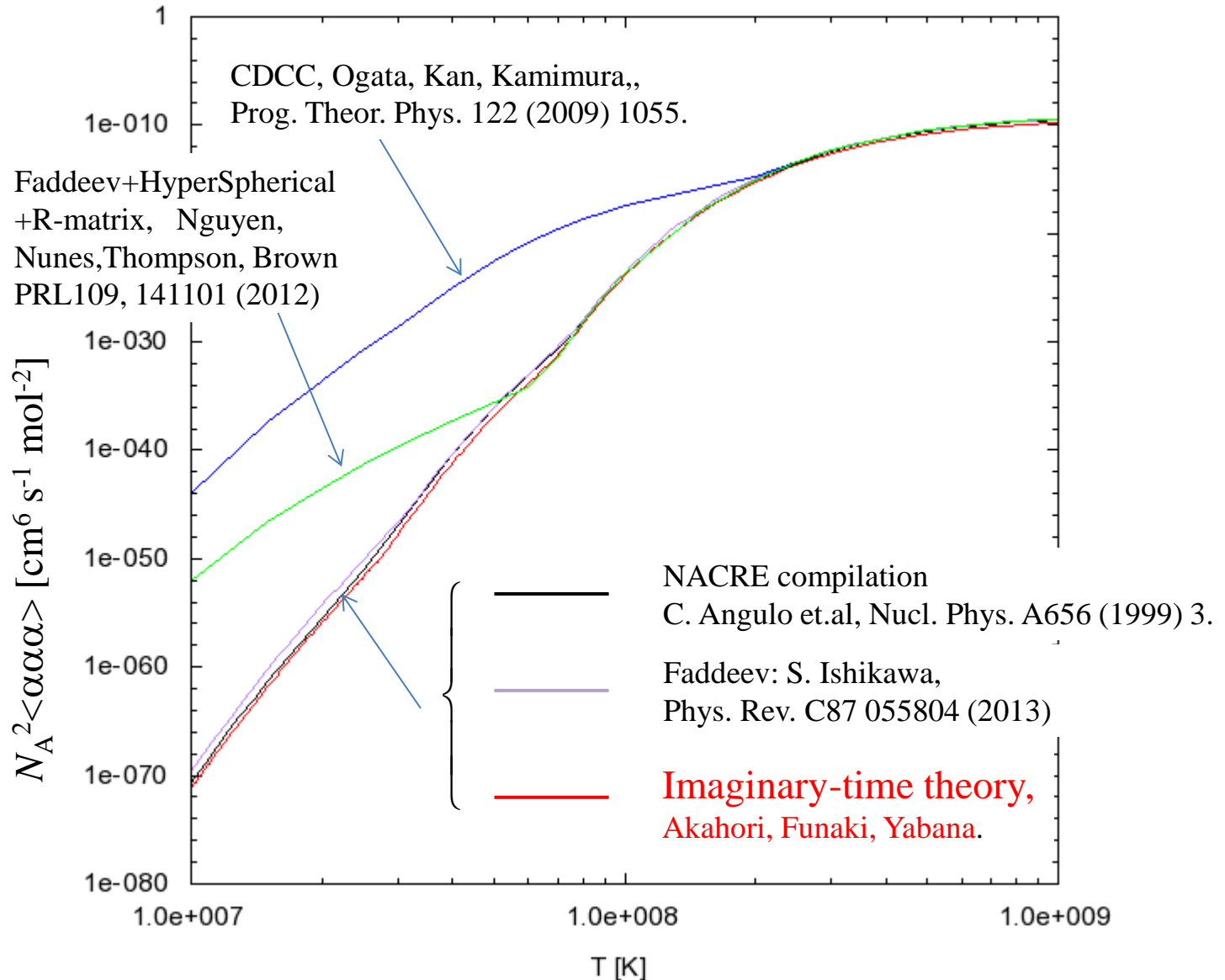
“Imaginary-time theory for triple-alpha reaction rate”

$$-\frac{\partial}{\partial \beta} \psi(\beta) = H \psi(\beta)$$

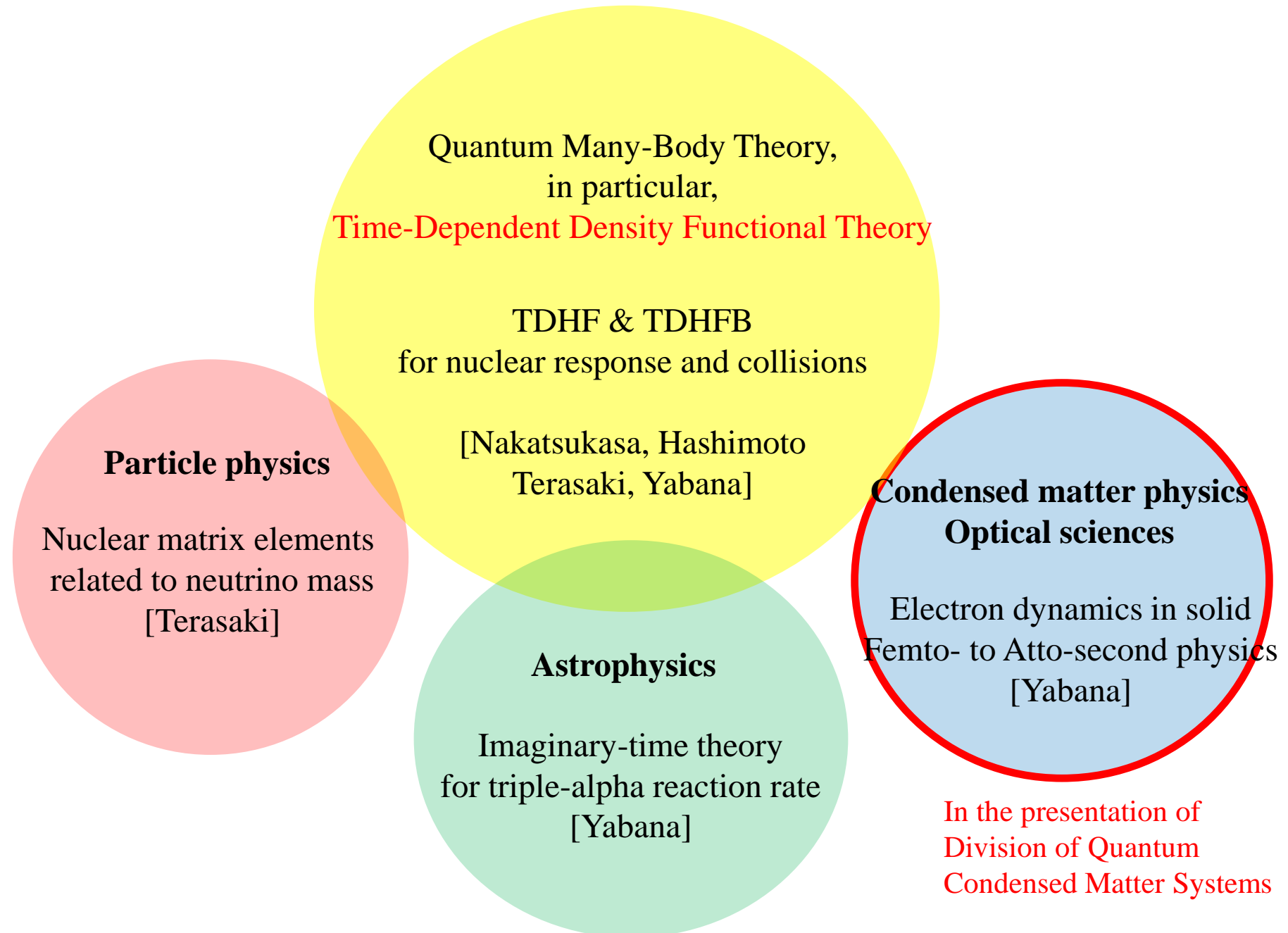


# Recent theoretical Controversy

$10^{26}$  order of magnitude difference at  $10^7$  K



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By Dr. T. Nakatsukasa

Quantum Many-Body Theory,  
in particular,

Time-Dependent Density Functional Theory

TDHF & TDHFB  
for nuclear response and collisions

[Nakatsukasa, Hashimoto  
Terasaki, Yabana]

## Particle physics

Nuclear matrix elements  
related to neutrino mass  
[Terasaki]

## Condensed matter physics Optical sciences

Electron dynamics in solid  
Femto- to Atto-second physics  
[Yabana]

## Astrophysics

Imaginary-time theory  
for triple-alpha reaction rate  
[Yabana]